

# CKM matrix and CP violation in SM (II)

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- Origin of the Cabibbo-Kobayashi-Maskawa Matrix (CKM)
- Overview of the measurements of the CKM elements
- CP violation in the Standard Model
- Overview of the measurements

# *b* Quark is Special !

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- Processes involving *b* quark can be used to measure several CKM element magnitudes
- Large mass of *b* quark allows use of Heavy Quark Effective Theory (HQET) for reliable theoretical calculations
  - Important for interpretation of experimental measurements with B mesons
- B mesons are of particular interest for study of CP violation
  - We will discuss this in detail
- Highlights of *b* quark
  - Heavy mass: big phase space and hence variety of final states to decay to
  - Long lifetime: important for experimental techniques to identify B mesons
  - $B^0$ - $B^0$  oscillation: a fine example of quantum entanglement, important ingredient for CP violation
  - $b \rightarrow u$  transitions: necessary ingredient for CP violation

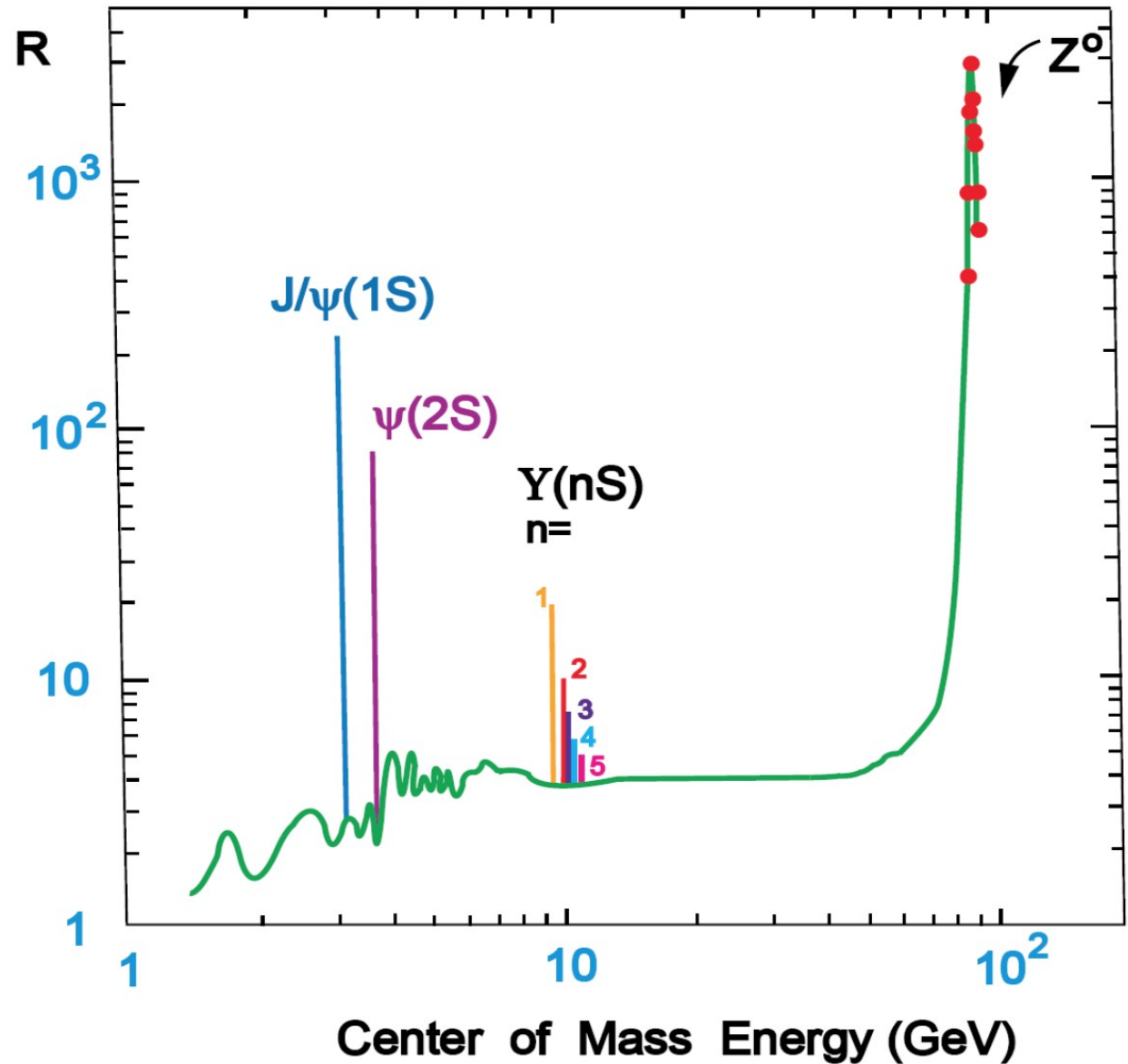
# Summary of B properties

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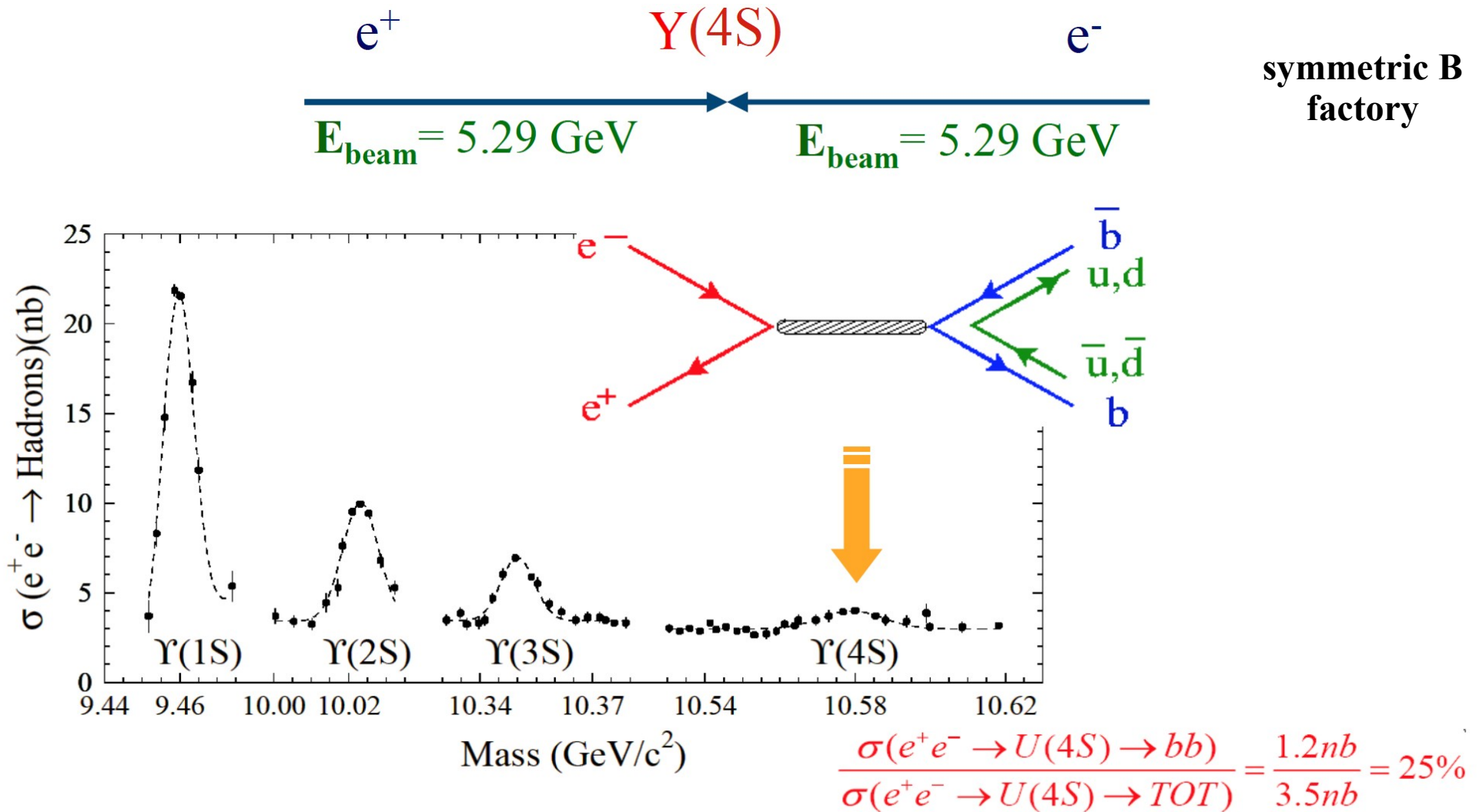
Particle, $I(J^P)$	Mass ( in MeV/c <sup>2</sup> )	Lifetime $\tau = 1/\Gamma$ (in10 <sup>-12</sup> s)
$B^0_d = (bd)$ , $I(J^P)=1/2 (0^-)$	$5279.4 \pm 0.5$	$1.536 \pm 0.014$ & ( $c\tau = 460\mu\text{m}$ )
$B^- = (bu)$ , $I(J^P)=1/2 (0^-)$	$5279.0 \pm 0.5$	$1.671 \pm 0.018$ & ( $c\tau = 501\mu\text{m}$ )
$B^0_s = (bs)$ , $I(J^P)=0(0^-)$	$5369.6 \pm 2.4$	$1.461 \pm 0.057$ & ( $c\tau = 438\mu\text{m}$ )
$\Lambda_b = (bud)$ , $I(J^P)=0(1/2^+)$	$5624.0 \pm 9.0$	$1.229 \pm 0.080$ & ( $c\tau = 368\mu\text{m}$ )

# B production in e<sup>+</sup>e<sup>-</sup> Collisions

$$R = \frac{e^+e^- \rightarrow \text{all}}{e^+e^- \rightarrow \gamma^* \rightarrow \mu^+\mu^-}$$



# B production at Upsilon resonance: B Factory

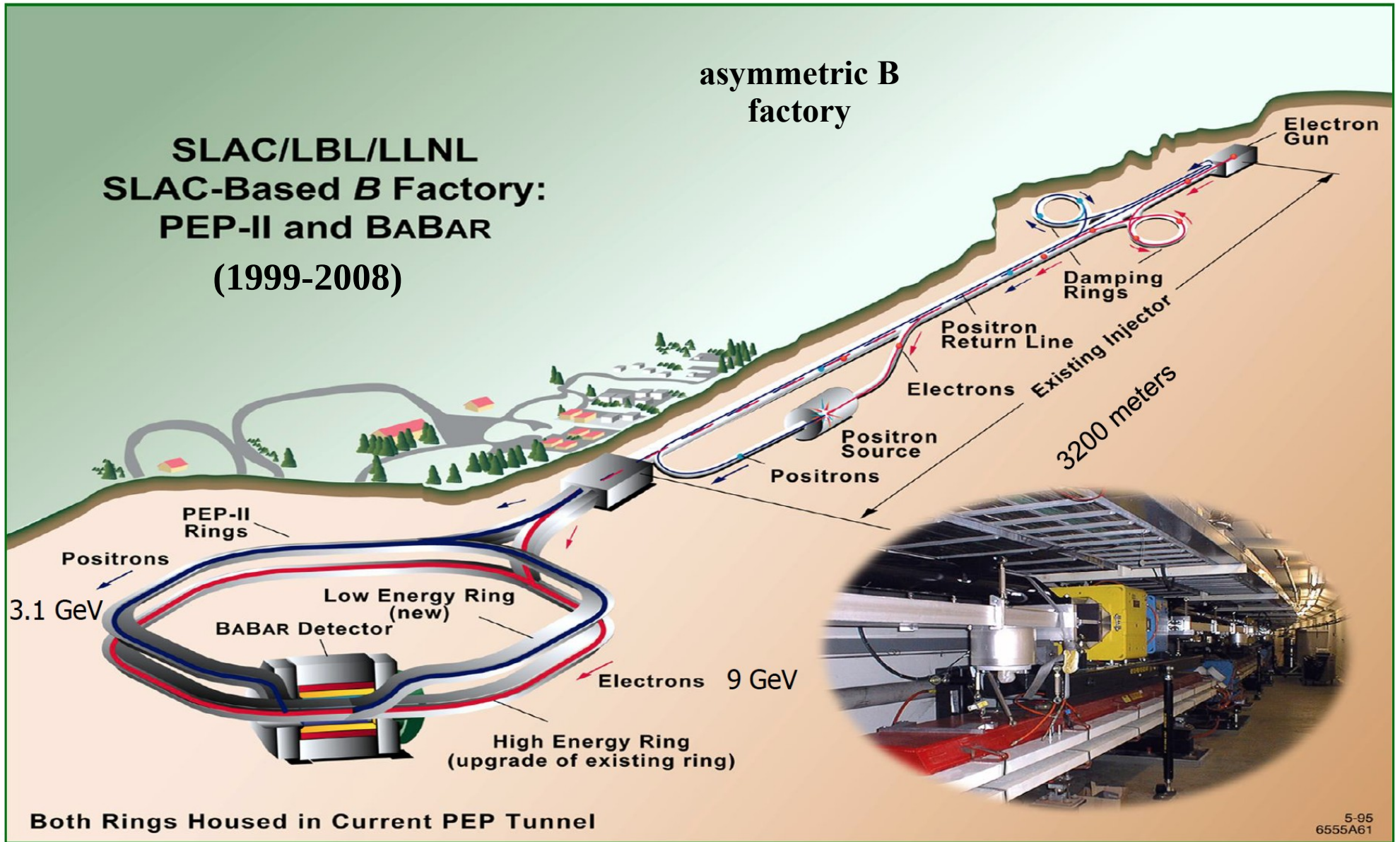


Enough energy to barely produce 2 B mesons, nothing else!

B Mesons produced with  $\sim 300 \text{ MeV}$  momentum

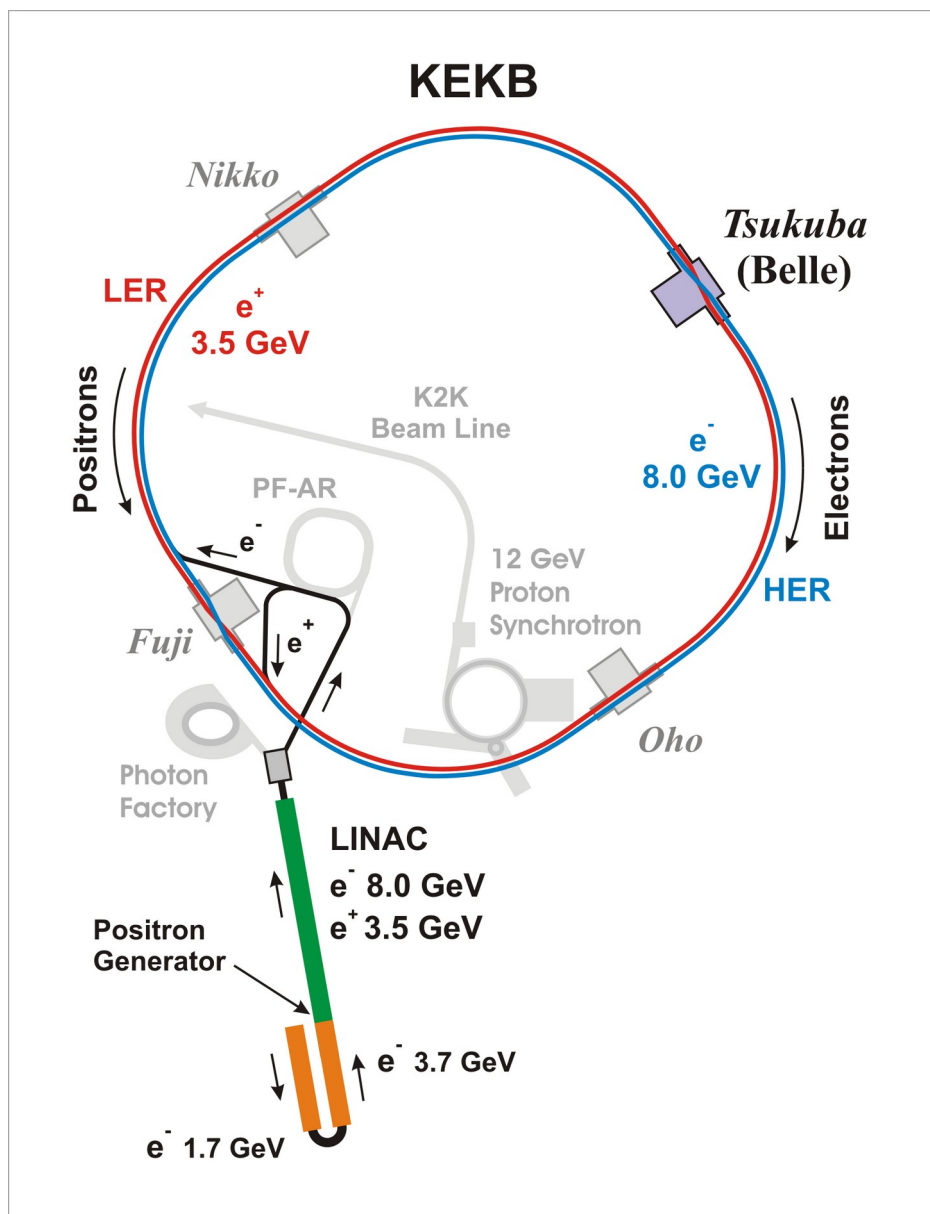
Moving very slowly, don't travel much before decay

# PEP-II Collider at SLAC (Stanford, CA)



PEP-II accelerator schematic and tunnel view

# KEKB collider at KEK (Tsukuba, Japan)



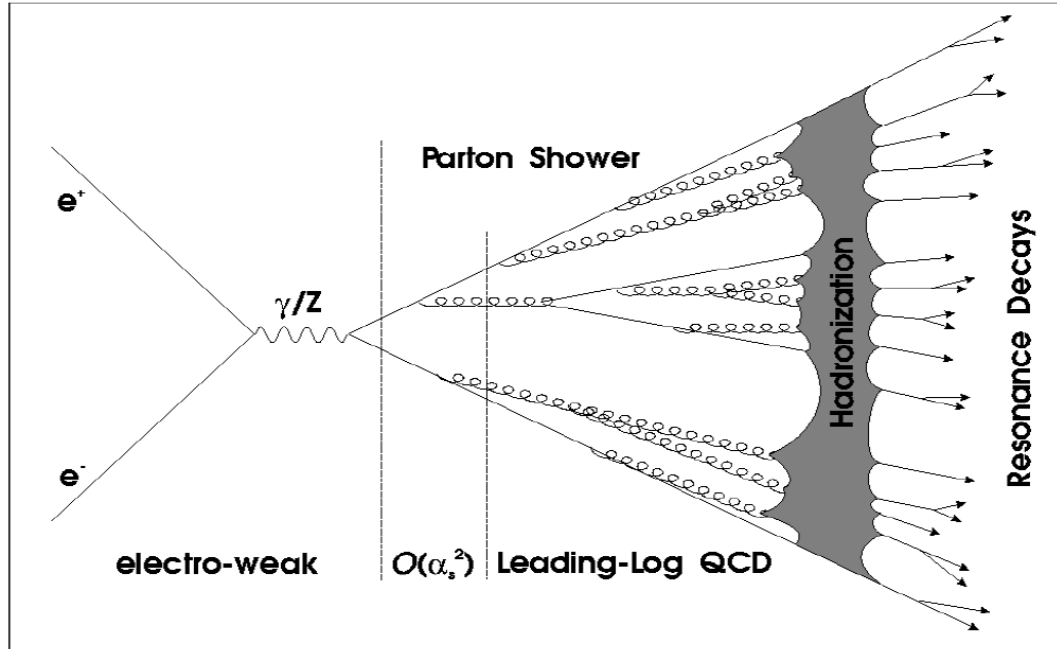
**KEKB: 1999-2010**

now upgraded to **SuperKEKB** (2019- ...)

**asymmetric B  
factory**

# B production at $Z^0$ Resonance

All types of B hadrons produced in  $Z \rightarrow b\bar{b}$  hadronization



$b$ hadron	Fraction [%]
$B^+, B^0$	$39.7 \pm 1.0$
$B_s^0$	$10.7 \pm 1.1$
$b$ baryons	$9.9 \pm 1.7$

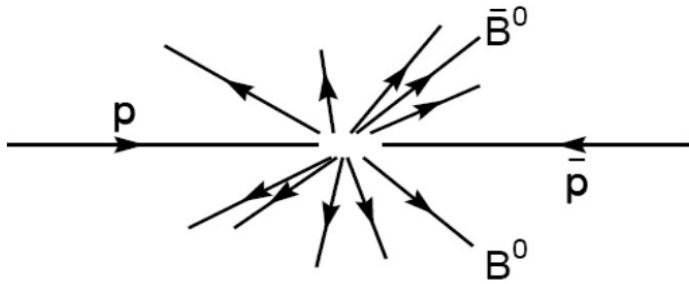
$$\frac{\Gamma(b\bar{b})}{\Gamma(TOT)} \sim 17\%$$

Average B momentum  $\sim 35$  GeV  
 $\Rightarrow (\beta\gamma)_B \approx 7$  (highly relativistic)

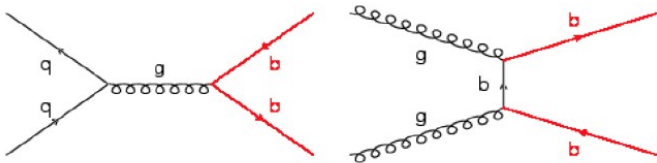
LEP/SLD Program ended in '95, made important contributions to  $b$  physics



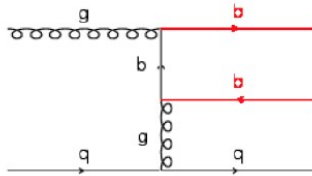
# B production at Hadron Colliders



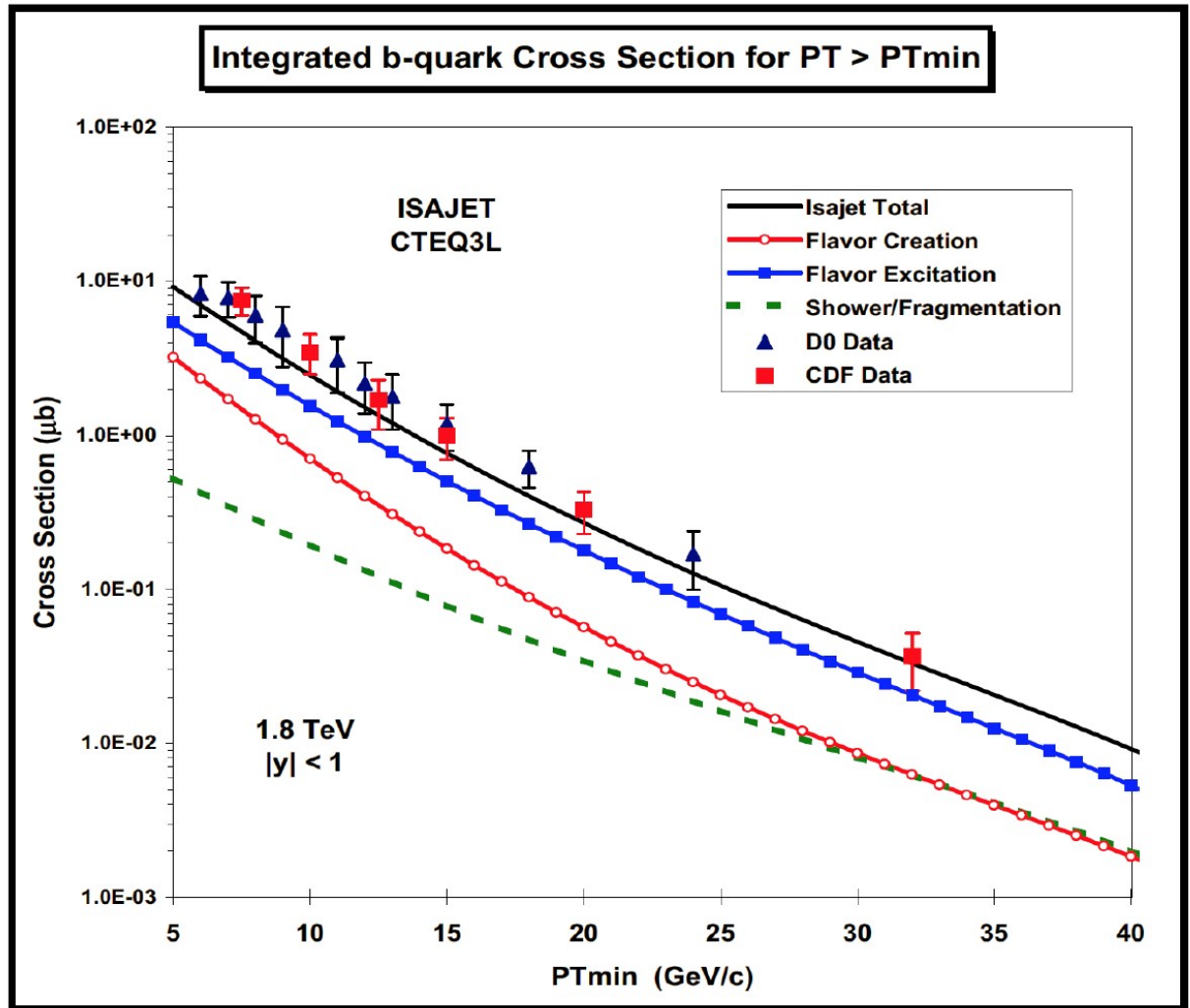
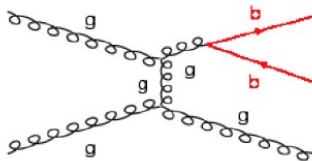
Lowest order



Flavor excitation



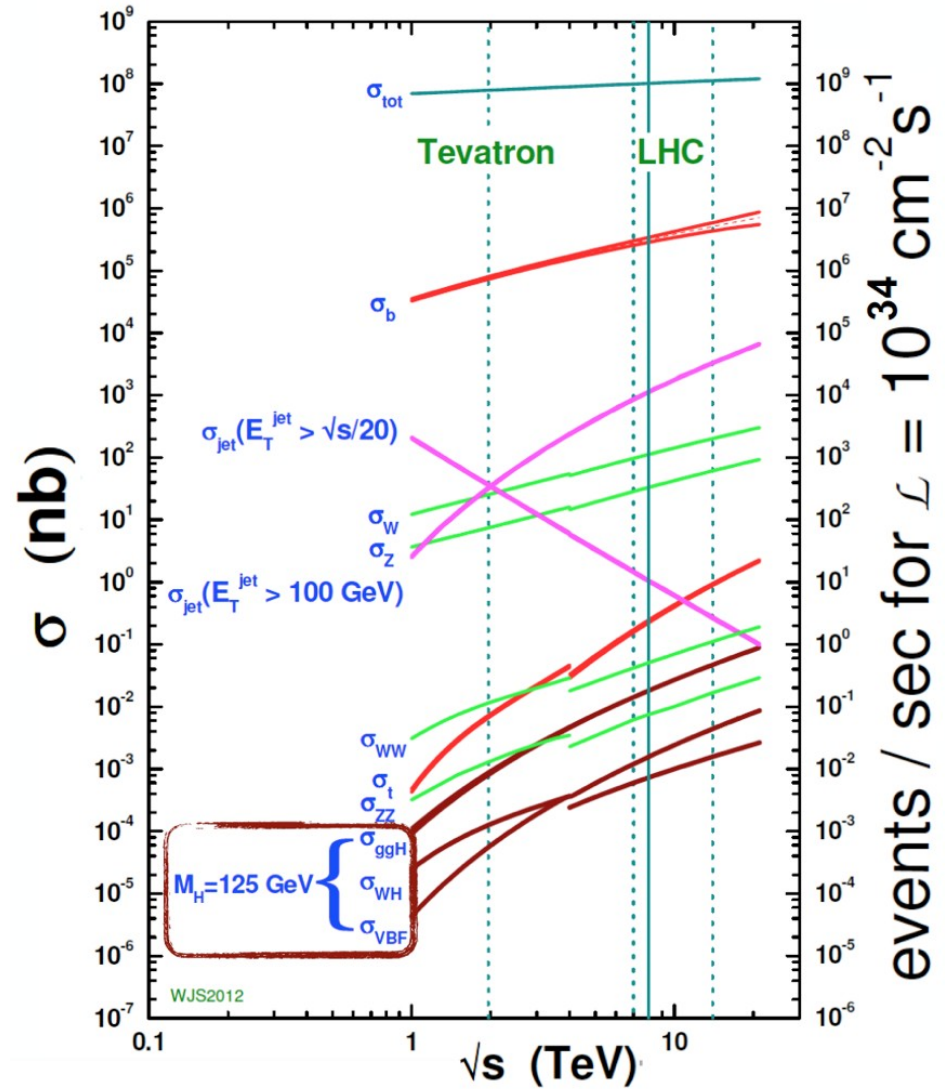
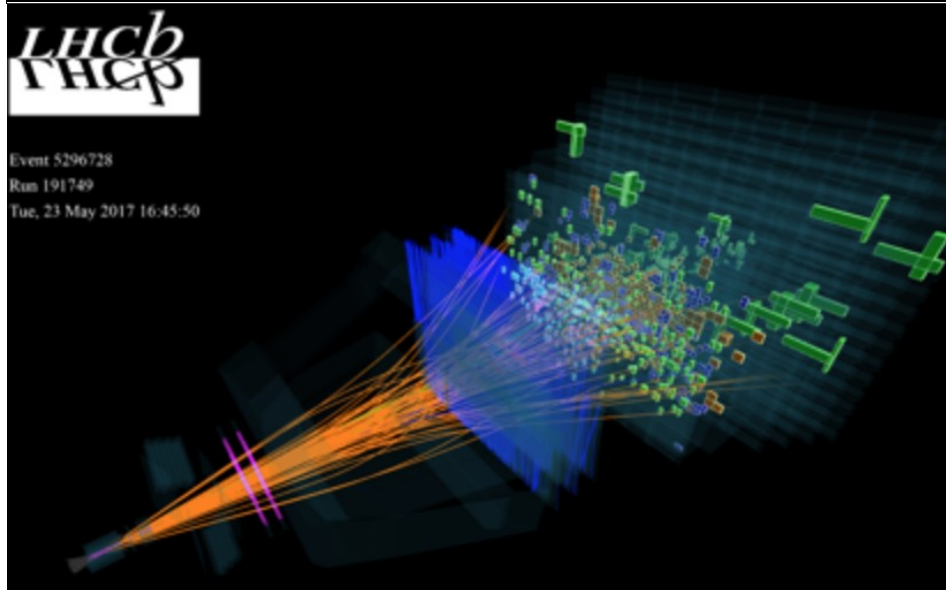
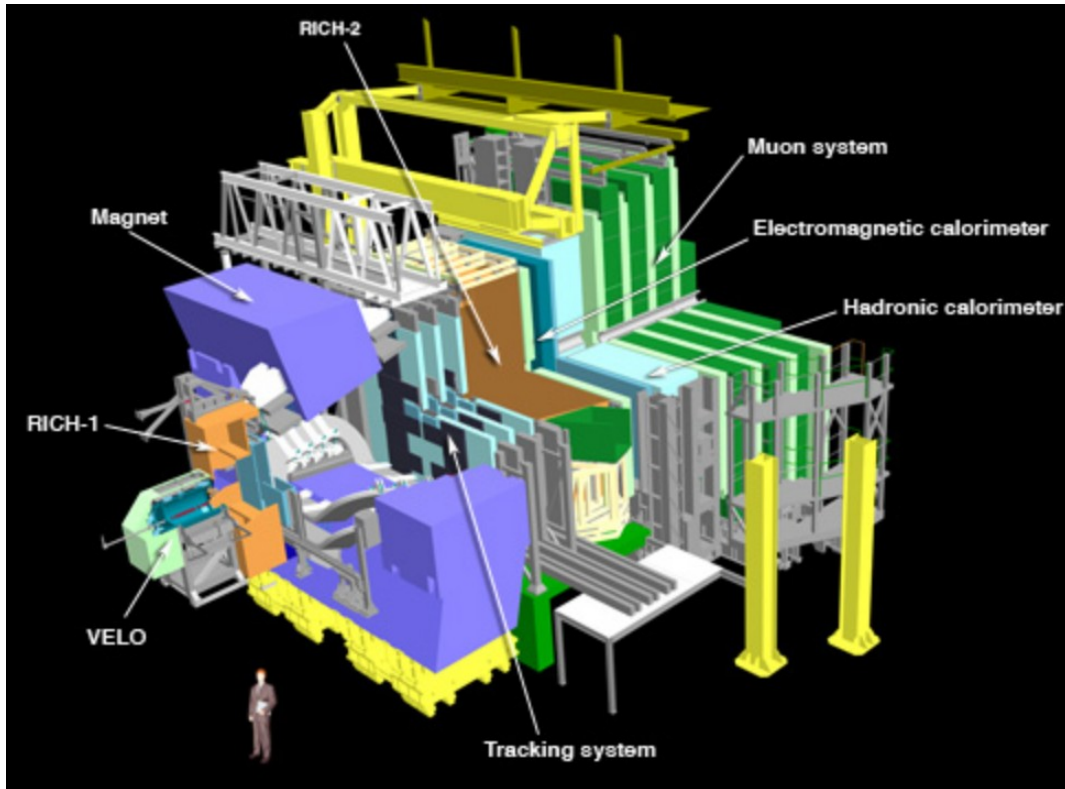
Gluon splitting



$$\sigma(b\bar{b}) \sim 10 \mu\text{b}$$

$$\frac{\sigma(b\bar{b})}{\sigma(TOT)} = \frac{1}{1000}$$

# B production at Hadron Colliders



# Summary of Past Experiments

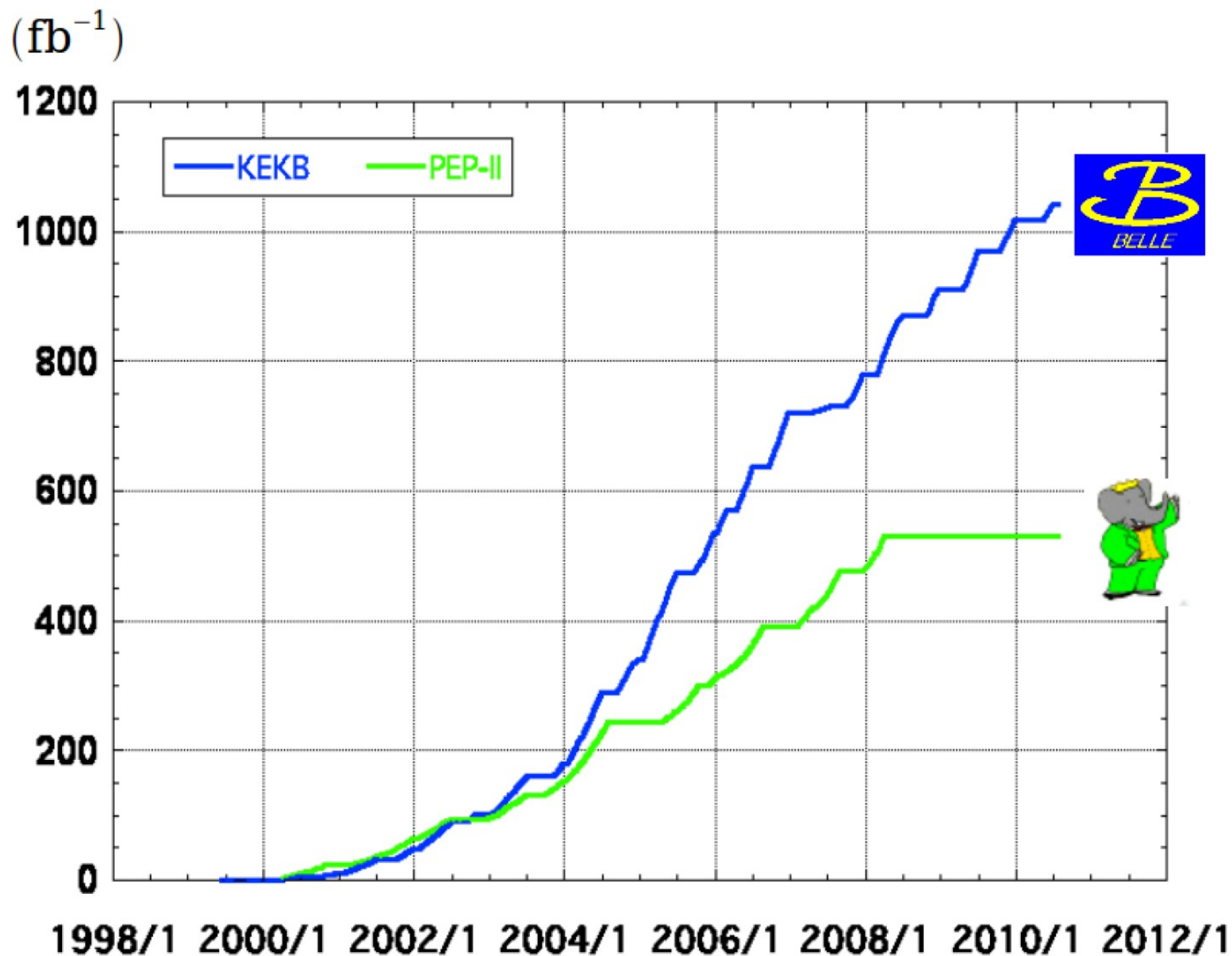
<u>Experiments</u>	<u># of b events</u>	<u>Environment</u>	<u>Characteristics</u>
LEP Coll. ALEPH/DELPHI/ L3/OPAL	~ 1M (each exp.)	Z <sup>0</sup> decays ( $\sigma \sim 6$ nb)	Back-to-back 45GeV b-jets All B hadrons produced <b>Stopped</b>
SLD	~0.1 M	Z <sup>0</sup> decays ( $\sigma \sim 6$ nb)	Back-to-back 45GeV b-jets All B hadrons produced <b>Stopped</b>
ARGUS	~0.2 M	Y(4s) decays symmetric ( $\sigma \sim 1.2$ nb)	B mesons produced at rest B <sup>0</sup> and B <sup>+</sup> produced <b>Stopped</b>
CLEO	~9 M	Y(4s) decays symmetric ( $\sigma \sim 1.2$ nb)	B mesons produced at rest B <sup>0</sup> and B <sup>+</sup> produced <b>Stopped</b>
Belle Babar	~130 M (each exp.)	Y(4s) decays asymmetric ( $\sigma \sim 1.2$ nb)	B mesons produced at rest B <sup>0</sup> and B <sup>+</sup> produced <b>Stopped</b>
Tevatron Coll. CDF/D0	~several	p $\bar{p}$ collider $\sqrt{s} = 1.8$ TeV	triggered events All B hadrons produced <b>Stopped</b>

# Summary of Present Experiments

<u>Experiments</u>	<u># of b events</u>	<u>Environment</u>	<u>Characteristics</u>
BelleII	goal: $50 \text{ ab}^{-1}$ $\sim 55 \cdot 10^9$ events	Y(4s) decays asymmetric ( $\sigma \sim 1.2 \text{ nb}$ )	B mesons produced at rest $B^0$ and $B^+$ produced <b>Running</b>
LHC Coll. LHCb	$\sim 5 \cdot 10^{10}$ events (*)	pp collider	triggered events All B hadrons produced <b>Running</b>
LHC Coll. CMS/ATLAS	$\sim 5 \cdot 10^{10}$ events (*)	pp collider $\sqrt{s} = 7, 8, 13 \text{ TeV}$	triggered events All B hadrons produced <b>Running</b>

(\*) very rough estimation

# Integrated luminosity of (past) B factories



**> 1  $\text{ab}^{-1}$**

**On resonance:**

$\Upsilon(5S)$ : 121  $\text{fb}^{-1}$

$\Upsilon(4S)$ : 711  $\text{fb}^{-1}$

$\Upsilon(3S)$ : 3  $\text{fb}^{-1}$

$\Upsilon(2S)$ : 25  $\text{fb}^{-1}$

$\Upsilon(1S)$ : 6  $\text{fb}^{-1}$

**Off reson./scan:**

~ 100  $\text{fb}^{-1}$



**~ 550  $\text{fb}^{-1}$**

**On resonance:**

$\Upsilon(4S)$ : 433  $\text{fb}^{-1}$

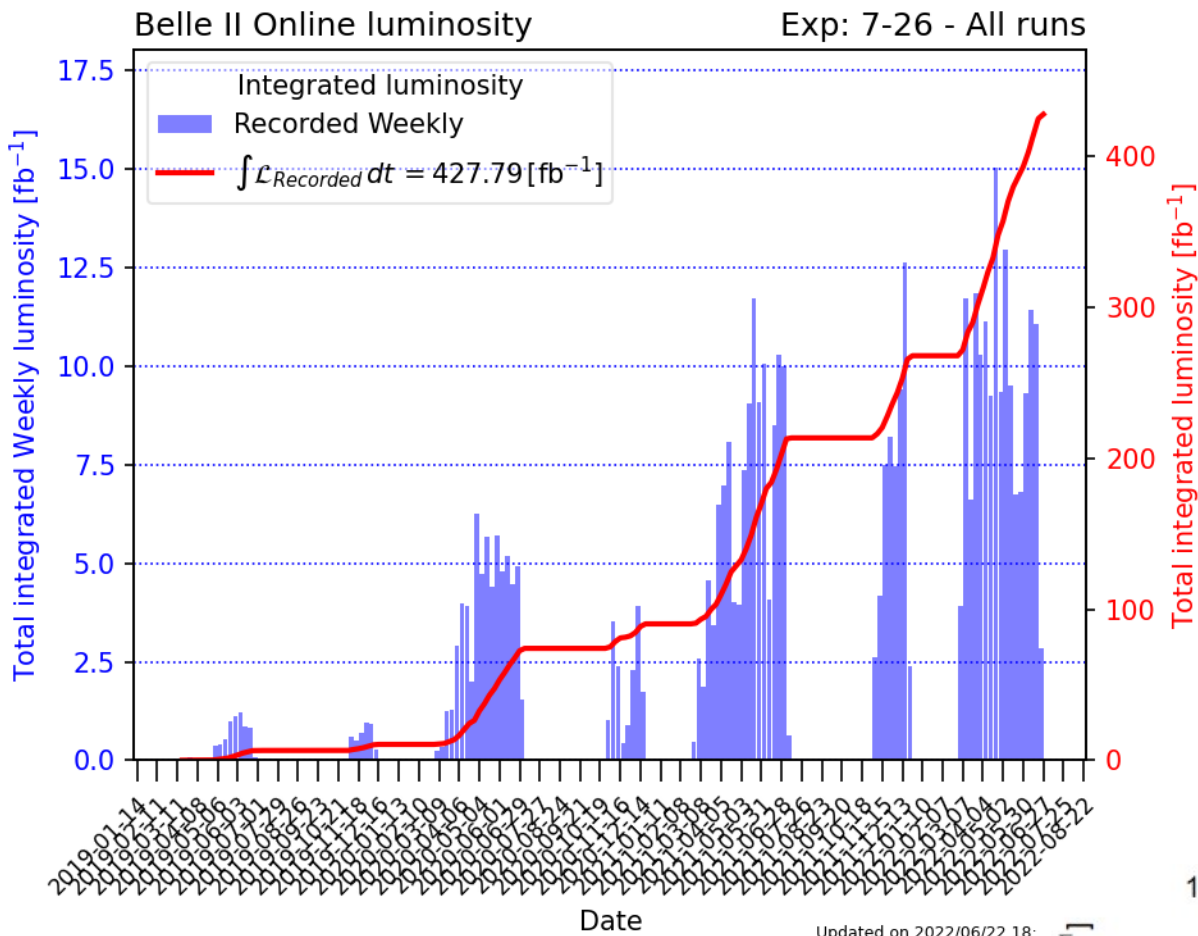
$\Upsilon(3S)$ : 30  $\text{fb}^{-1}$

$\Upsilon(2S)$ : 14  $\text{fb}^{-1}$

**Off resonance:**

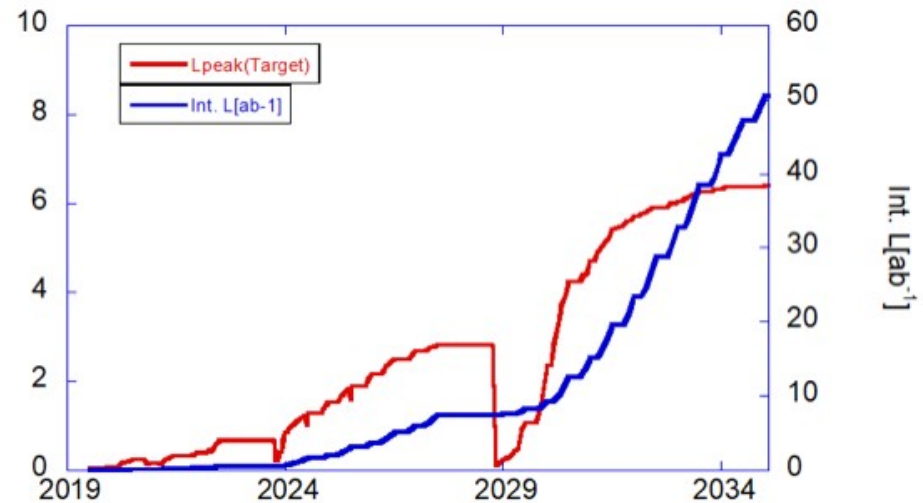
~ 54  $\text{fb}^{-1}$

# Integrated luminosity of Belle II B factory



*Experimental Su*

Peak Luminosity [ $\times 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$ ]



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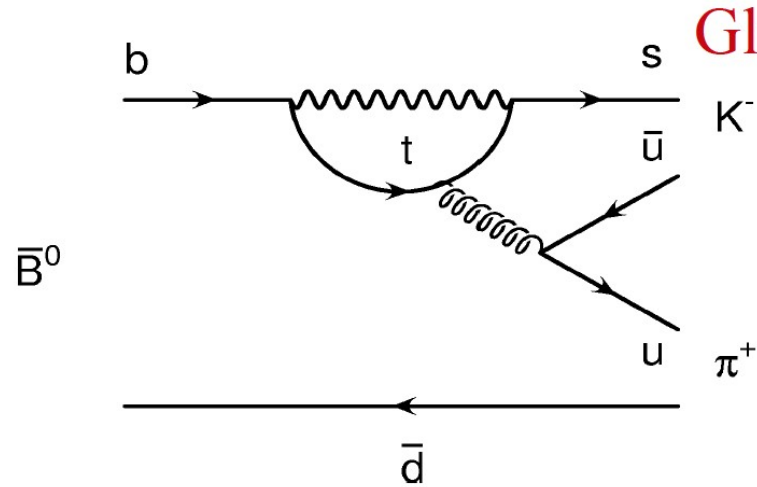
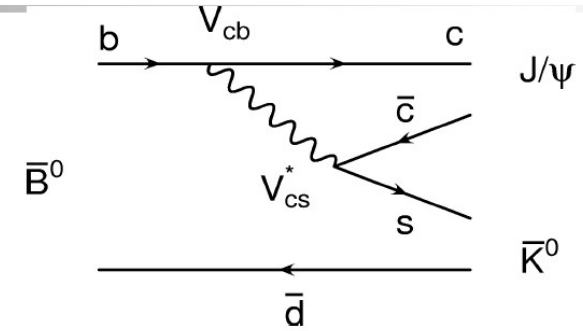
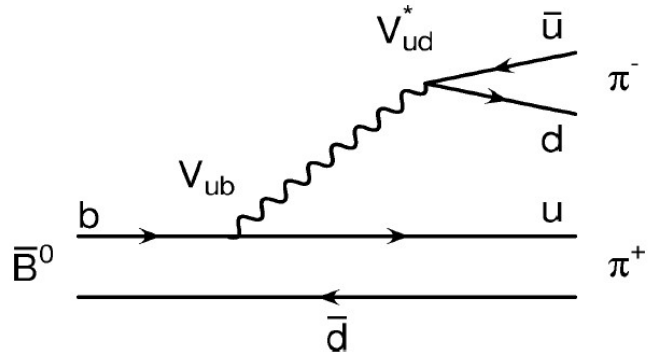
# Catalog of B decays

## Introduction to Diagram Jargon !

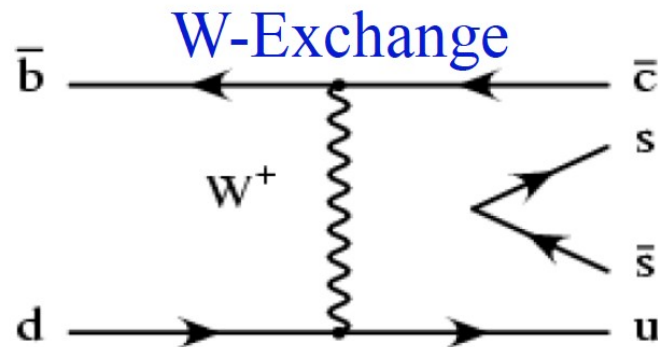
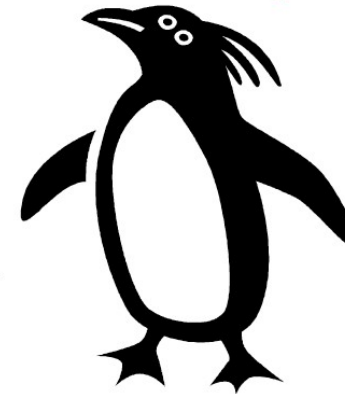
# Spectator

# Tree Diagrams

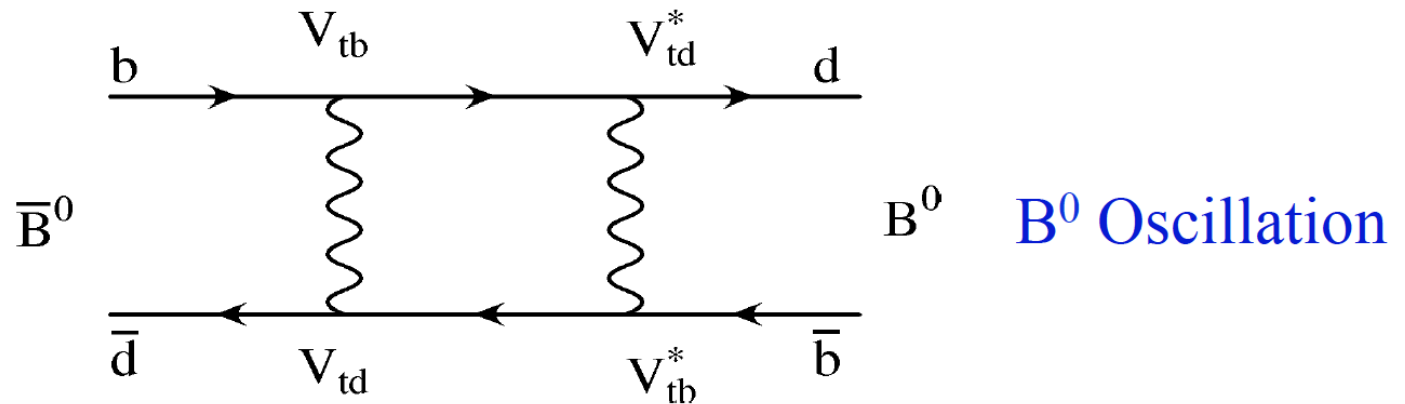
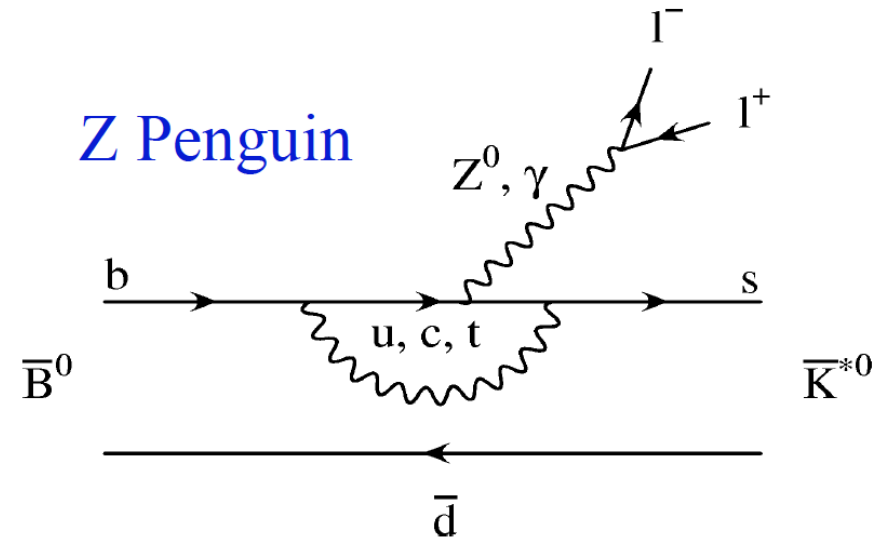
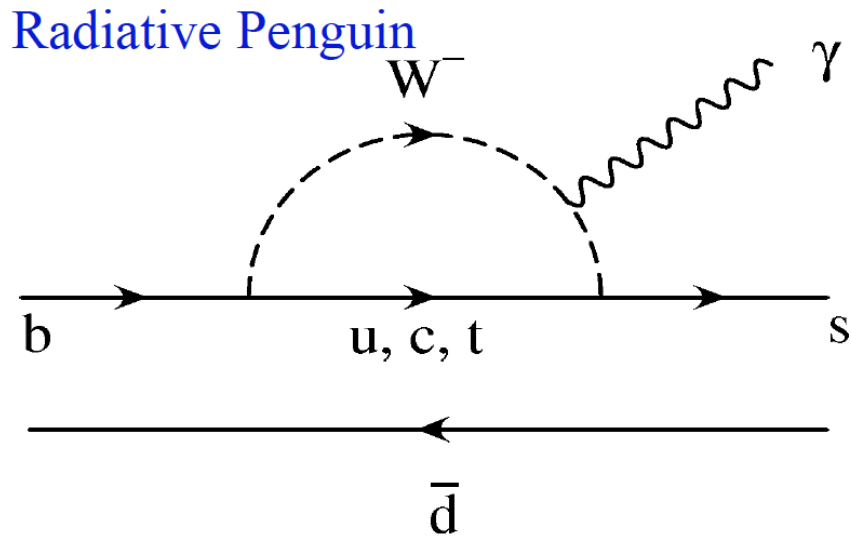
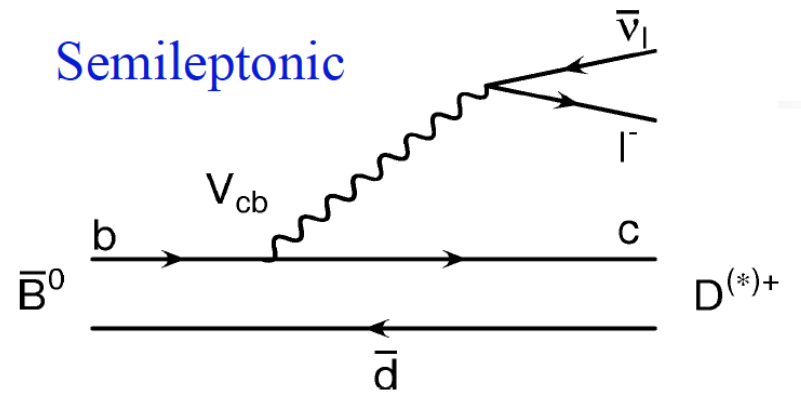
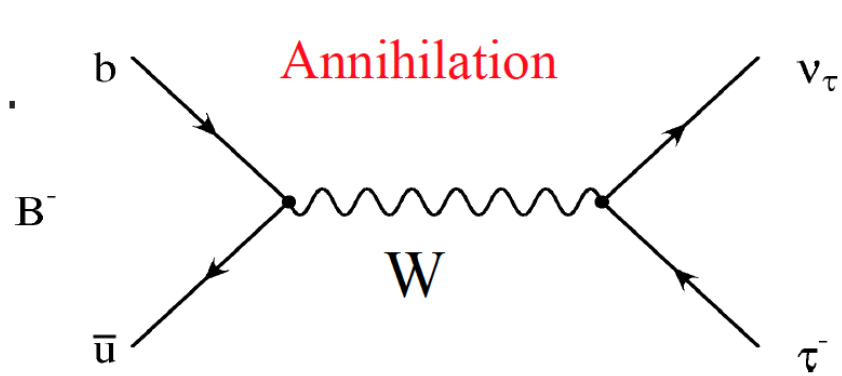
# Color Suppressed



# Gluonic Penguin







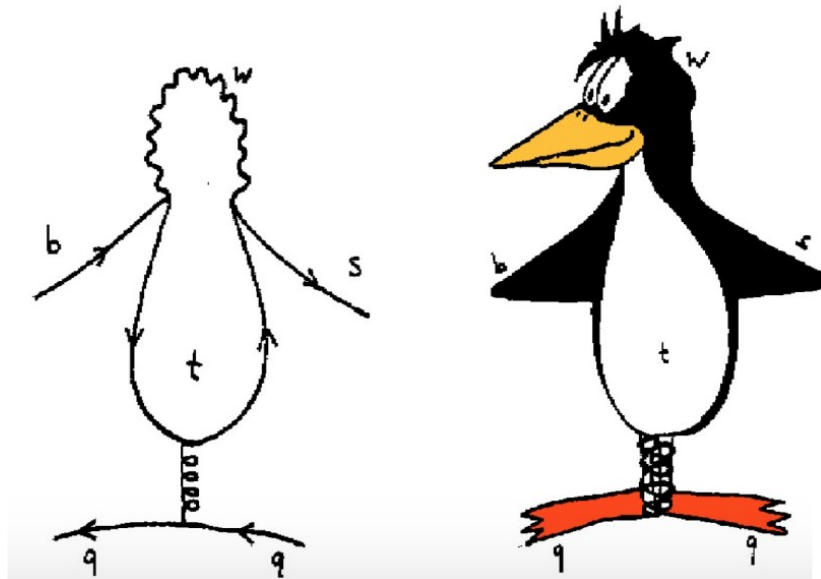
# Penguins in B Decays !?



Ref: Preface to Shifman's 1999 book, ITEP Lectures on Particle Physics and Field Theory, John Ellis recalls how the gluon interference diagram came to be called a penguin diagram.

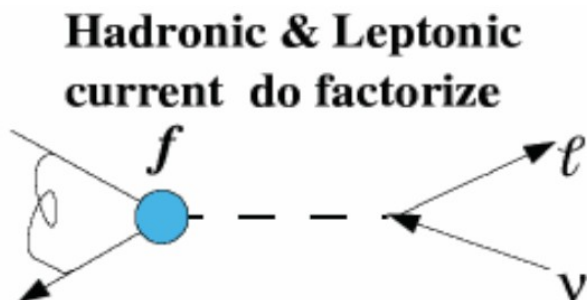
*One night in spring 1977, Ellis lost a bet during a game of darts. His penalty required that he use the word "penguin" in a journal article.* "For some time, it was not clear to me how to get the word into this b quark paper that we were writing at the time," Ellis wrote.

"Then, one evening I stopped on my way back to my apartment to visit some friends living in Meyrin, where I smoked some illegal substance. *Later, when I got back to my apartment and continued working on our paper, I had a sudden flash that the famous diagrams looked like penguins.* So we put the name into our paper, and the rest, as they say, is history."



# Typology of Tree Decay Amplitudes

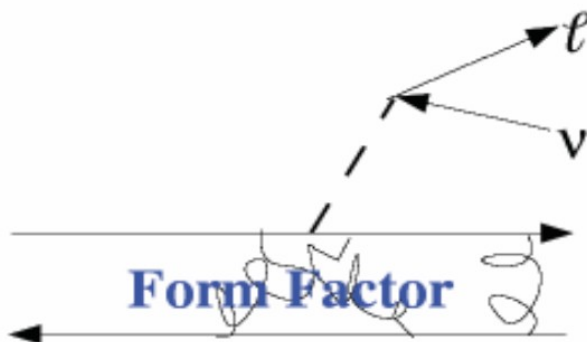
## Leptonic



- \* Low energy QCD: decay constant  $f$
- \* Lattice QCD starts to get precise

## Semileptonic

(In most cases best way to extract  $|V_{ij}|$ )



### Exclusive Decays:

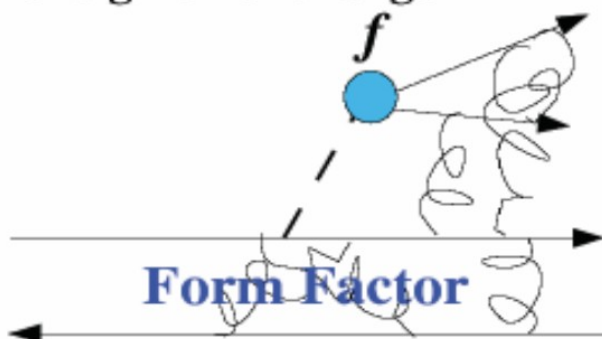
- \* FF: Symmetries ( $\chi$  & HQS)
- \* FF: Lattice QCD, Sum Rules; ...

### Inclusive Decays:

- \* Operator Product Expansion

## Hadronic

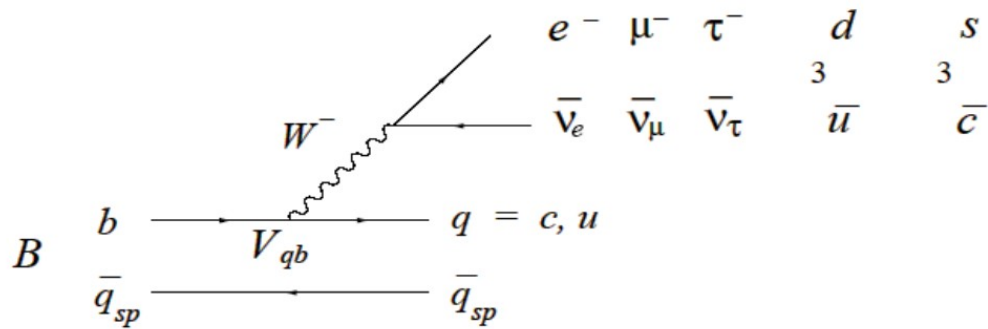
No factorization in naïve sense due to gluon exchange



Theoretical developments:

e.g. QCD Factorisation approach  
Not used for  $|V_{ij}|$  extraction (yet)

# Summary of $b$ -quark Decay

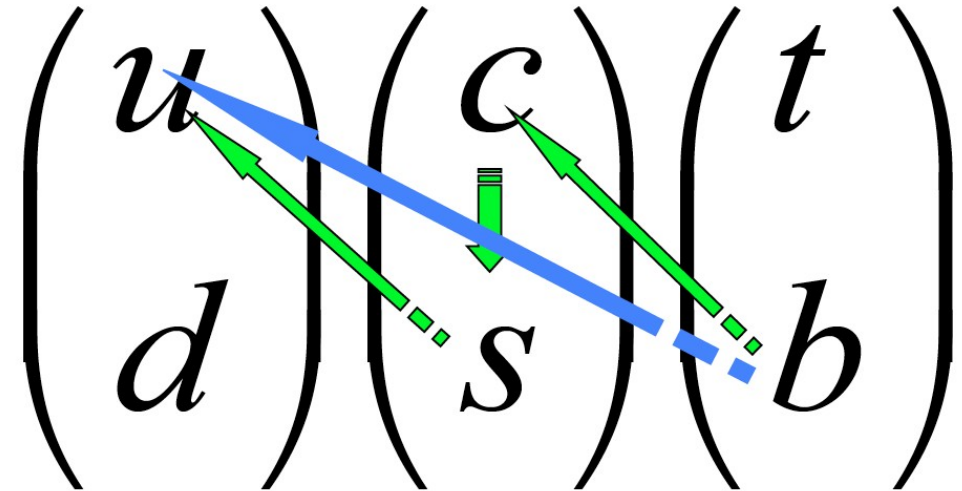


Mode	$N_c$	$f_{QCD}$	$f_{ps}$	$V_{xb}$	$\mathcal{B}$
$c\bar{u}d'$	3	1.3	0.52	0.038	48%
$c\bar{c}s'$	3	1.3	0.25	0.038	23%
$ce\bar{\nu}_e$	1	1.0	0.52	0.038	12%
$c\mu\bar{\nu}_\mu$	1	1.0	0.52	0.038	12%
$c\tau\bar{\nu}_\tau$	1	1.0	0.13	0.038	3%

$u\bar{u}d'$	3	1.3	1.00	0.003	0.6%
$u\bar{c}s'$	3	1.3	0.52	0.003	0.3%
$ue\bar{\nu}_e$	1	1.0	1.00	0.003	0.1%
$u\mu\bar{\nu}_\mu$	1	1.0	1.00	0.003	0.1%
$u\tau\bar{\nu}_\tau$	1	1.0	0.25	0.003	<0.1%

$s(d)g, s(d)\gamma, s(d)Z^0\dots$

$\mathcal{O}(10^{-3})$

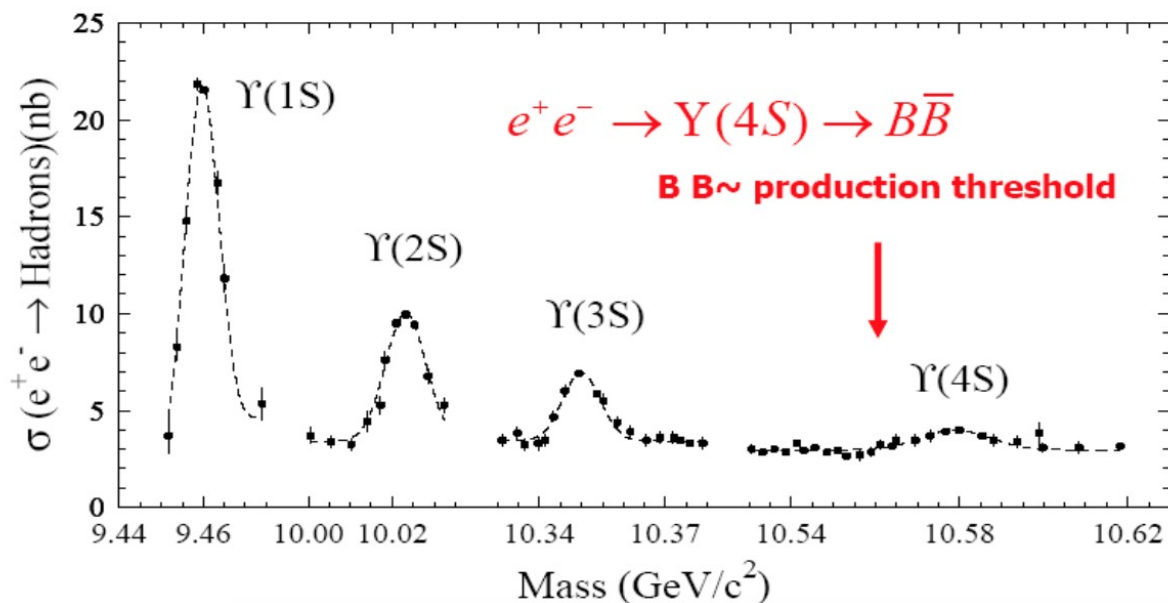
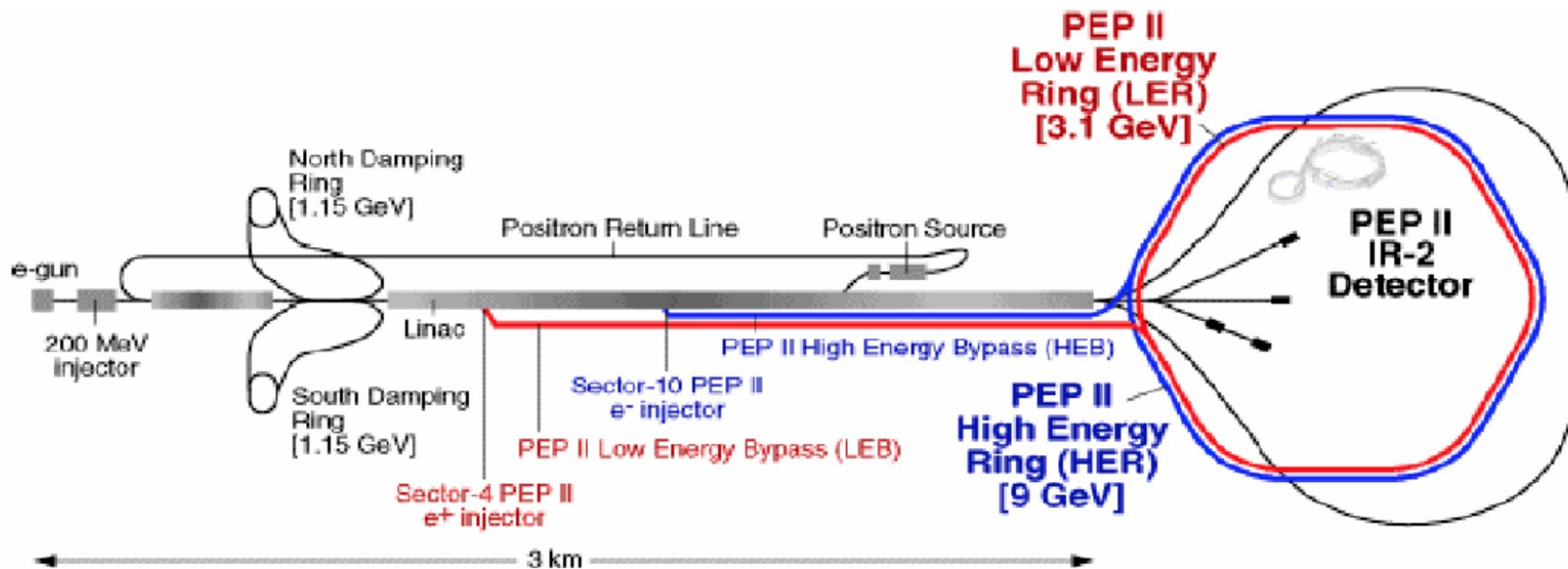


- 99% of B's  $\rightarrow$  D's
- 66(13)% of B's  $\rightarrow K^+(K^-)$ : flavor tagging
- 10% semi-leptonic BR: flavor tagging
- $7 \times 10^{-4}$  of B's  $\rightarrow J/\psi \rightarrow \mu^+\mu^-$
- mean track multiplicity for single B  $\sim 5.5$

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# **Brief Primer of B reconstruction at e<sup>+</sup>e<sup>-</sup> B factory**

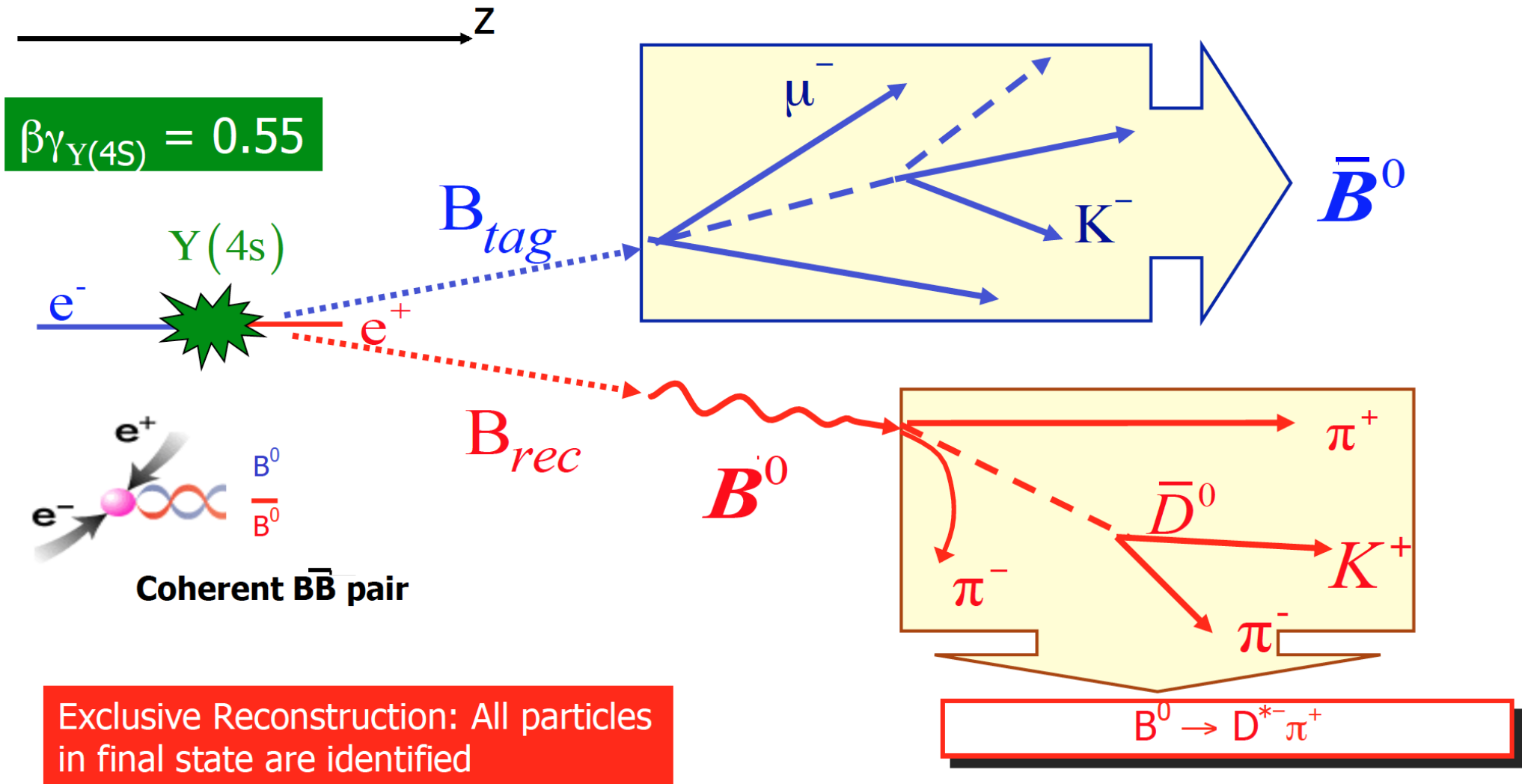
# PEP-II Asymmetric B-Factor at SLAC



- 9 GeV  $e^-$  on 3.1 GeV  $e^+$
- Y(4S) boost in lab frame
- $\beta\gamma = 0.55$

# Snapshot of $B\bar{B}$ Event at BaBar

Inclusive Reconstruction: Look at some of decay products carrying information about their mother



Exclusive Reconstruction: All particles in final state are identified

# Exclusive or Inclusive ?

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## ■ Exclusive Selection

- All products in selected final states are found in the detector
- Conservation laws connect measured quantities between initial and final states
- Advantages:
  - Typically better signal to noise ratio
    - Kinematic constraints remove most of combinatorial background
- Disadvantages:
  - Usually requires more reliance on theoretical models and theory for interpretation of results

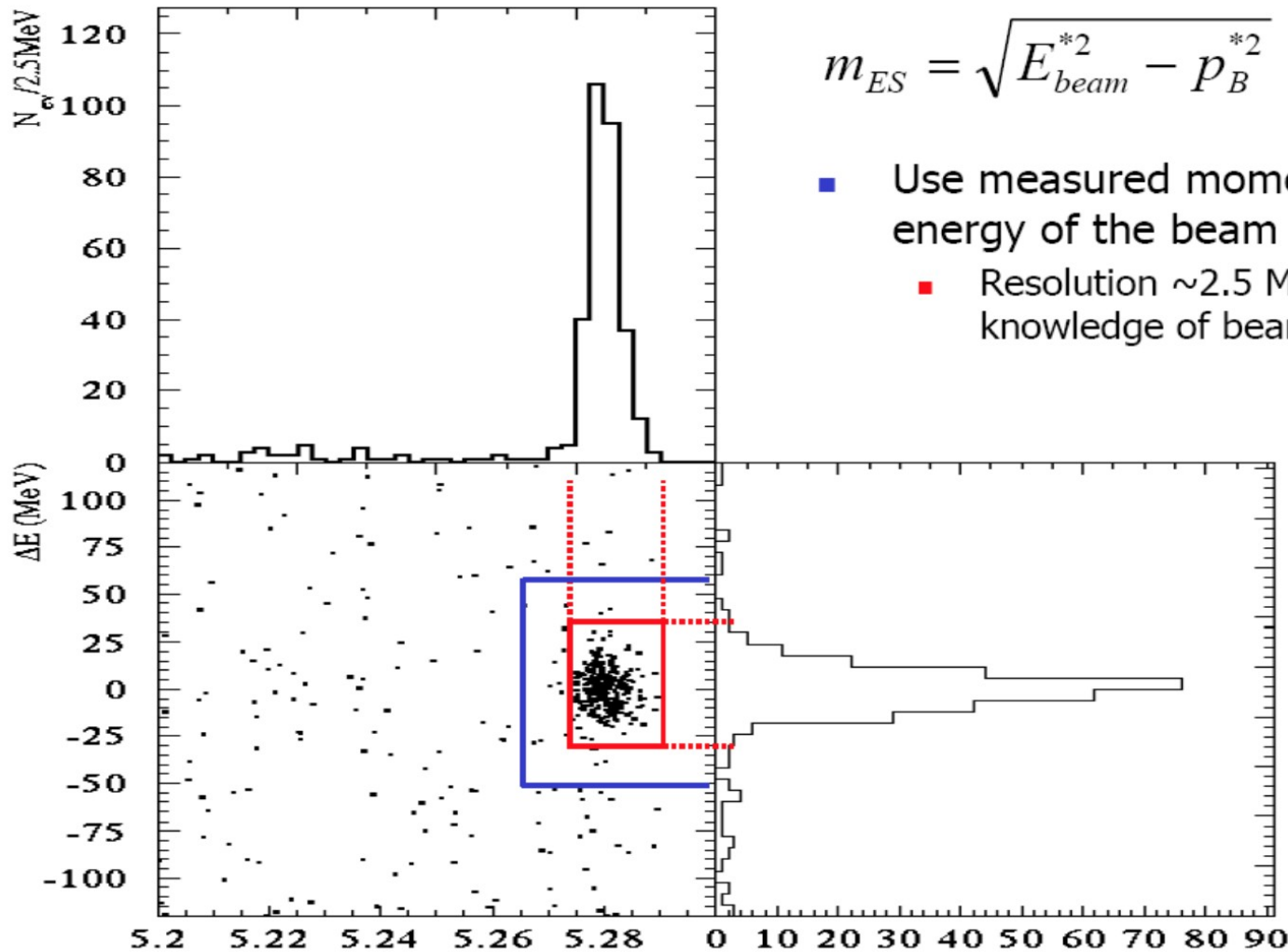
## ■ Inclusive Selection

- Not all particles in final state selected
- No kinematic relation between initial and final state
- Advantage:
  - Closer to transition diagram at quark level, hence typically less dependent on theory models
- Disadvantage:
  - More background because of reduced constraints



# Ingredients of B Reconstruction

- Take advantage of clean environment in  $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$ 
  - Energy of each B meson is known in the center of mass



$$m_{ES} = \sqrt{E_{beam}^{*2} - p_B^{*2}}$$

Energy-substituted mass

- Use measured momenta of B daughters and energy of the beam
  - Resolution  $\sim 2.5 \text{ MeV}/c^2$  dominated by knowledge of beam energy

Energy difference

$$\Delta E = E_B^* - E_{beam}^*$$

- Difference between total reconstructed and expected energy
  - Dominated by detector energy resolution
  - Resolution depends on particles in final states

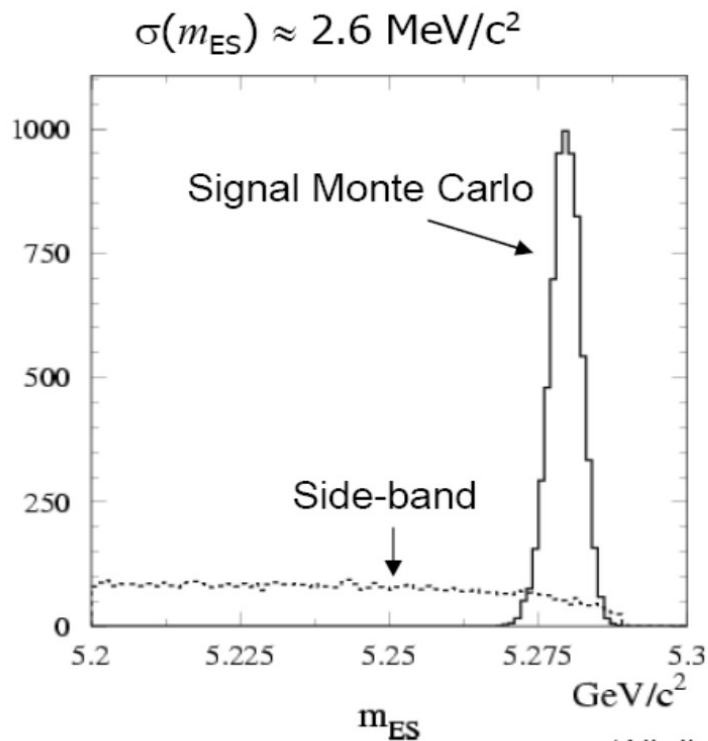
# Kinematic Variables

$$m_{ES} = \sqrt{E_{\text{beam}}^{*2} - p_B^{*2}}$$

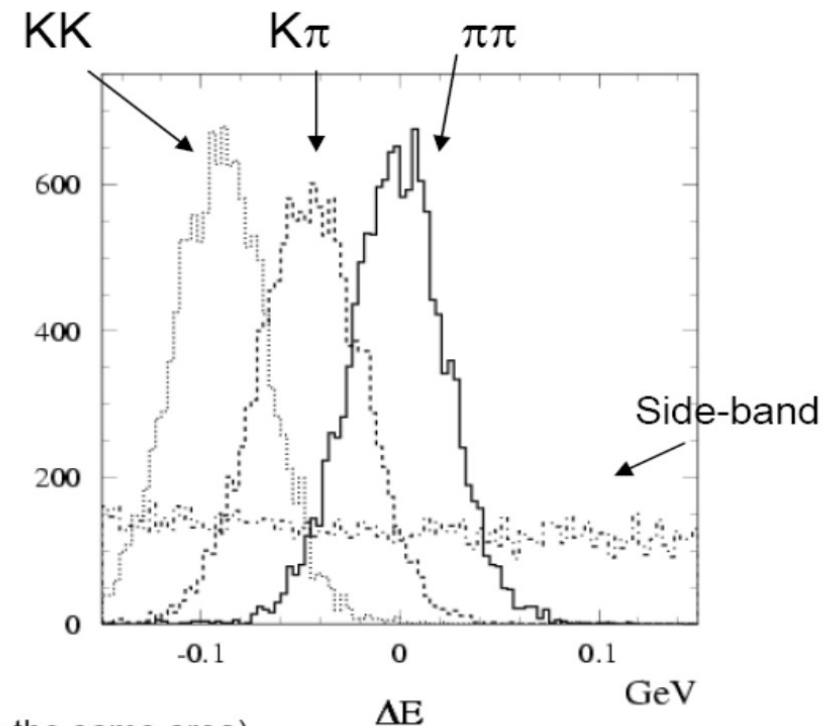
$$\Delta E = E_B^* - E_{\text{beam}}^*$$

- Dominated by tracking resolution
- Assume  $\pi$  mass for tracks
- Momentum dependent shift for  $K\pi$  and  $KK$

$$\sigma(\Delta E) \approx 26 \text{ MeV}$$



(All distributions are normalized to the same area)



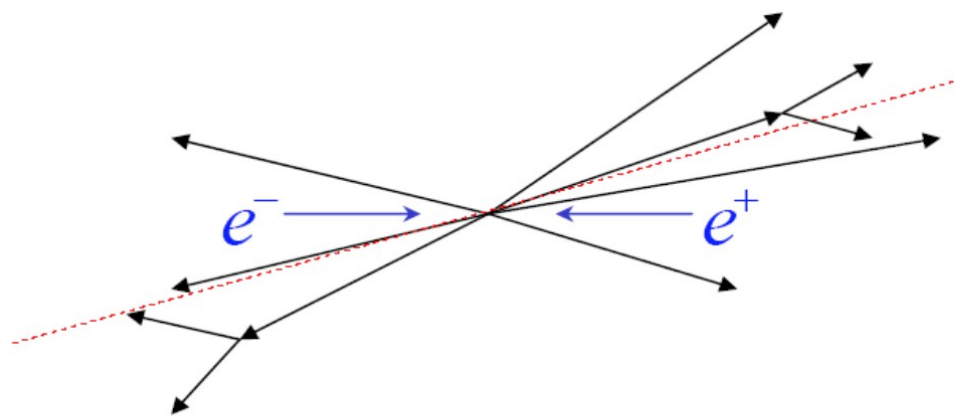
# Continuum Background Rejection

- Main source of background: continuum  $e^+e^- \rightarrow q\bar{q}$  ( $q = u, d, s, c$ )

- Branching fraction of interesting B decays  $\leq 10^{-4}$
  - Branching fraction of D decays:  $\cong 10^{-2}$
- } Overall branching fraction  $< 10^{-6}$

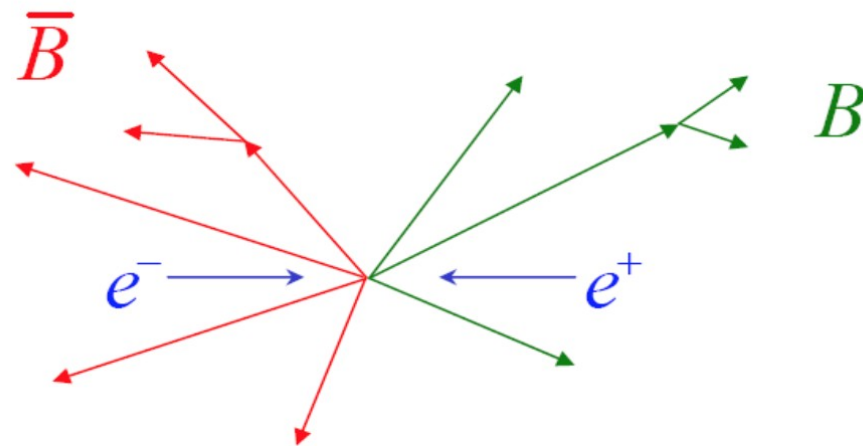
- Distinguish signal and background based on event topology

- Neural networks
- Fisher discriminant



Thrust Axis

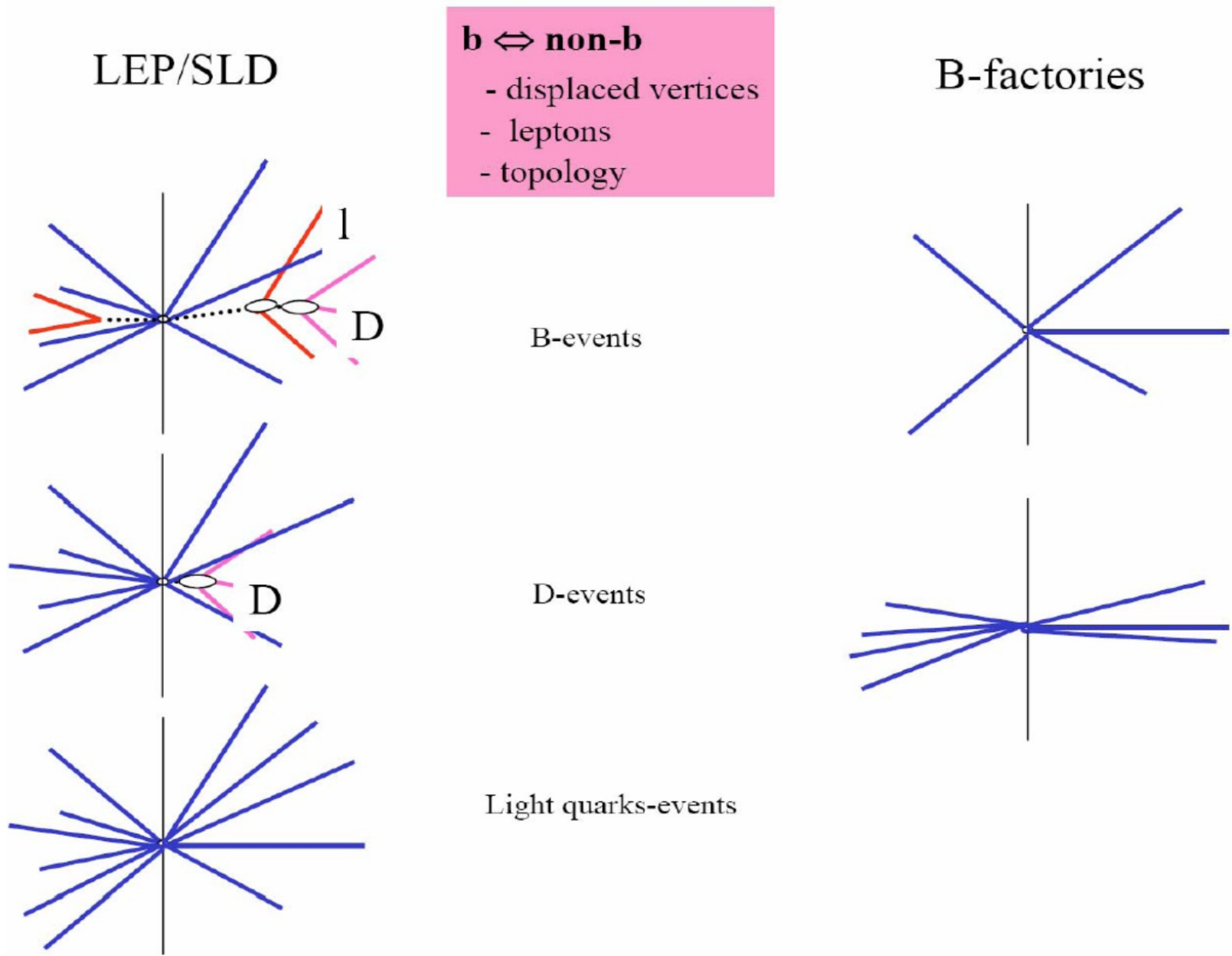
$$e^+e^- \rightarrow q\bar{q}$$



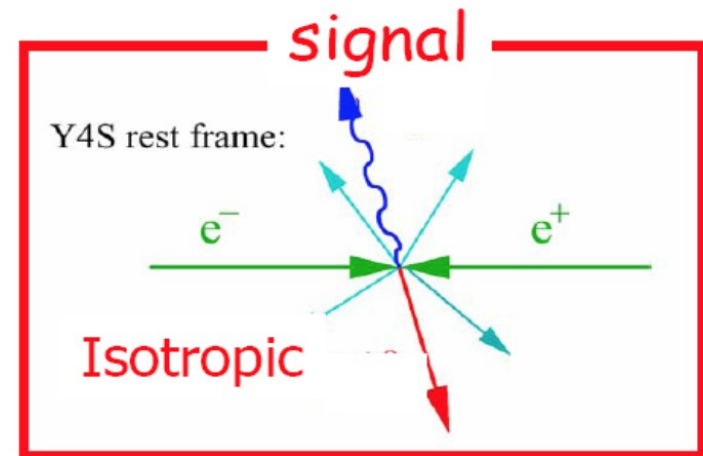
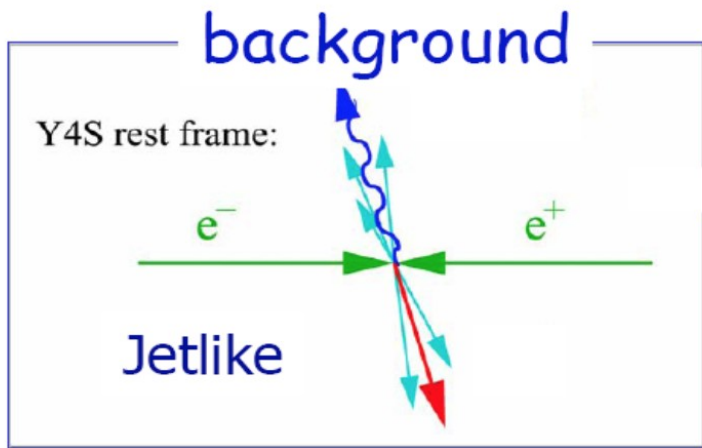
$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$$

$$T = \frac{\sum |\vec{T} \cdot \vec{p}_i|}{\sum |\vec{p}_i|} \text{ quantity to be maximized through } \vec{T}$$

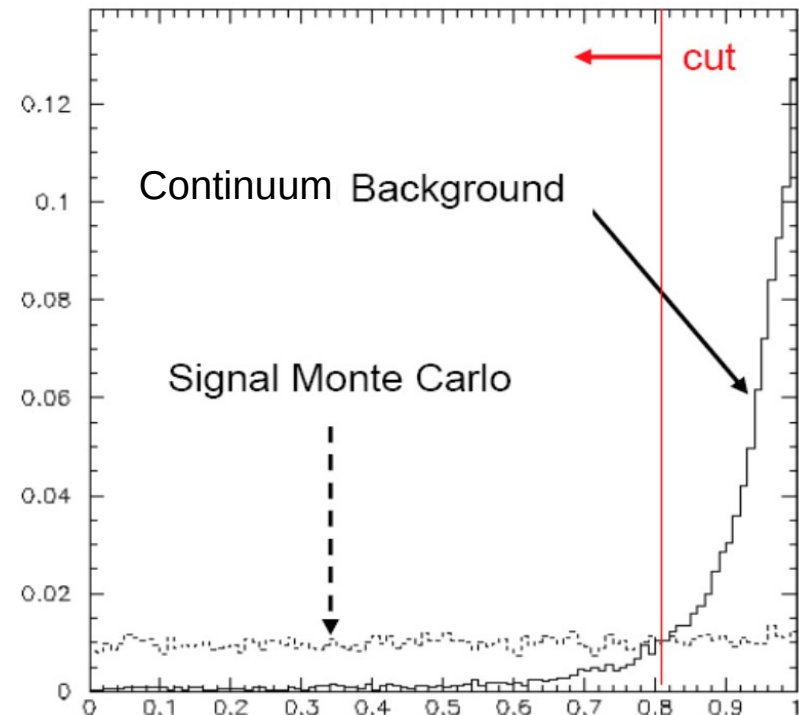
# Event Topology at LEP/SLD vs. B Factories



# Background Fighting: Sphericity Angle

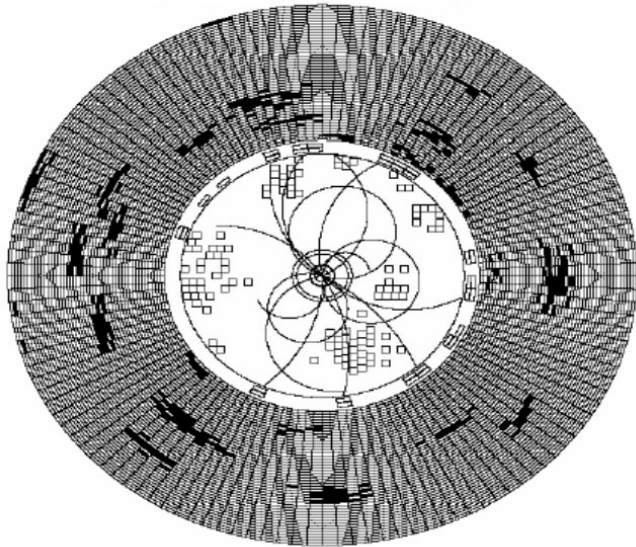


- $\cos\theta_s$ : Angle between the B candidate and the rest of event

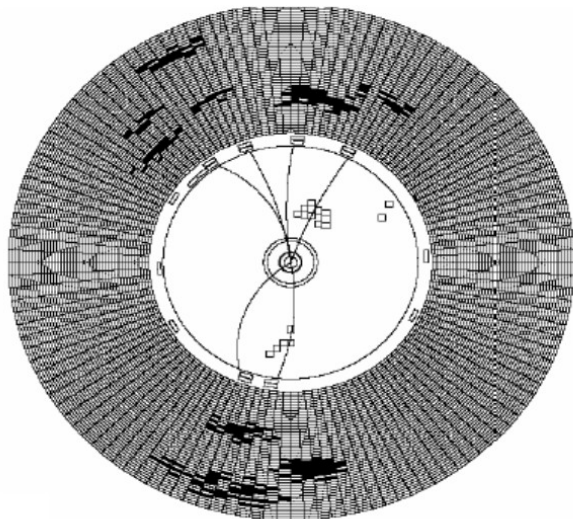


# 2<sup>nd</sup> Fox-Wolfram Moment

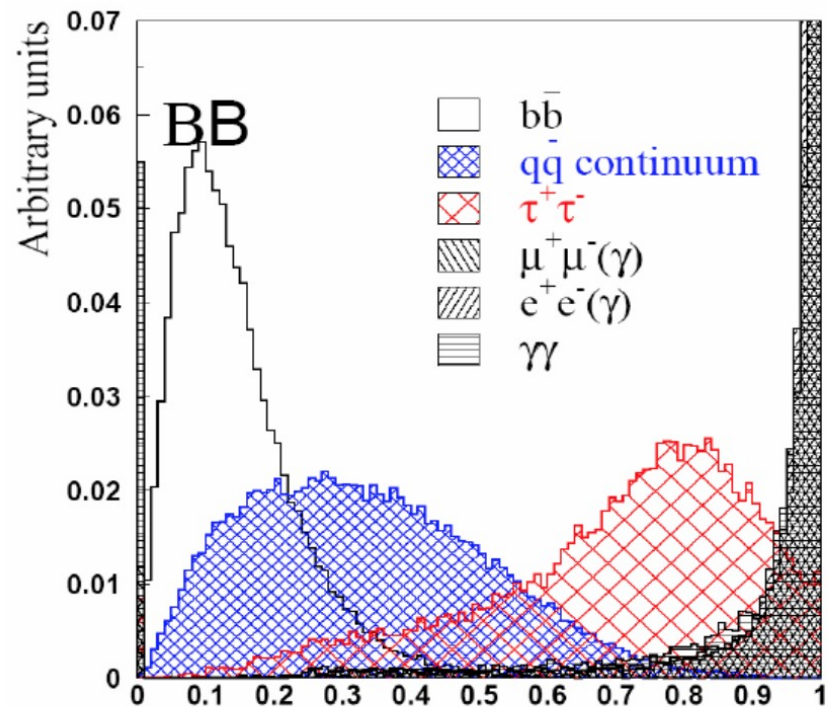
$\Upsilon(4S) \rightarrow B\bar{B}$  Decay



$e^+e^- \rightarrow u\bar{u}, d\bar{d}, s\bar{s}, c\bar{c}$  decays



Differences in the event topology (Isotropic B Vs jet-like Continuum) and Energy flow structure in these events used to construct continuum background suppression tools.



*Experimental Subnuclear Physics*

$$H_k = \sum_{i,j}^N |\vec{p}_i| |\vec{p}_j| P_k(\cos \theta_{i,j})$$

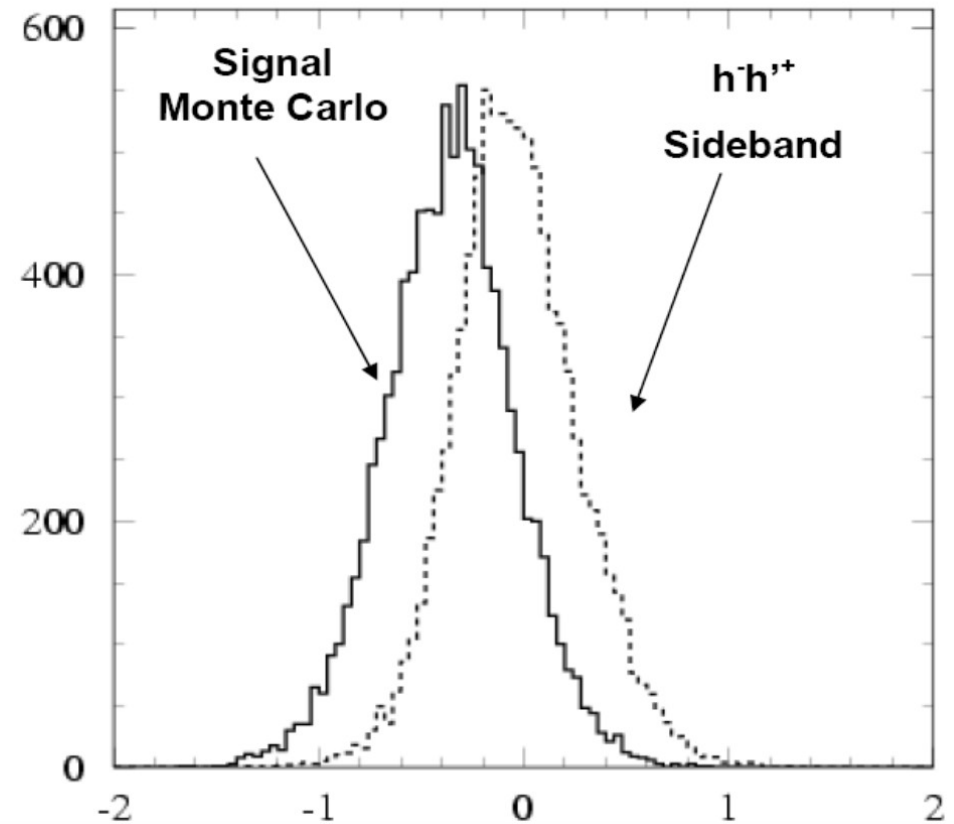
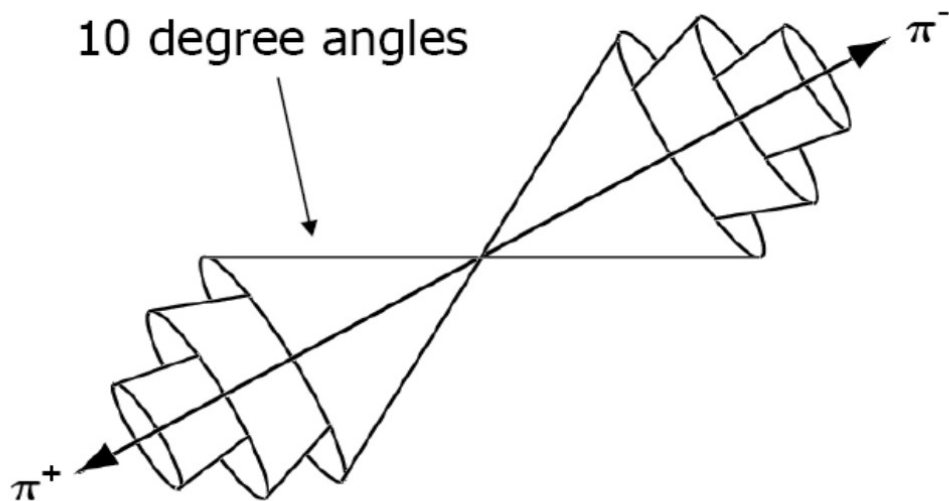
k-th order Fox-Wolfram moment

$$R^2 = H_2 / |H_2|$$

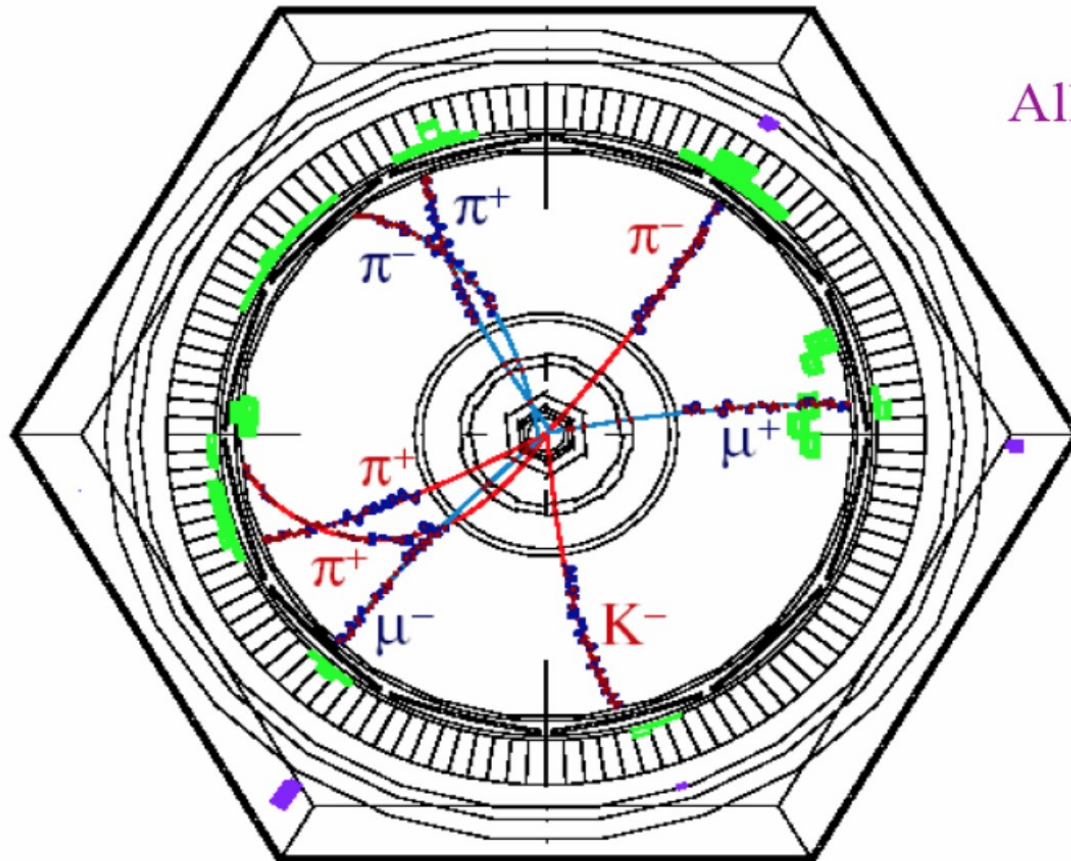
30

# Background Fighting: Fisher Discriminant

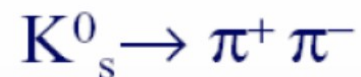
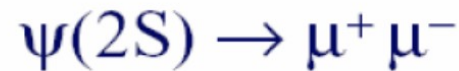
- Optimized linear combination of energy flow into cones about candidates
- Sensitive only to the rest of event
- Studied and calibrated on data:  $B \rightarrow D^0 \pi^-$ ,  $h^- h'^+$  sideband
- Validated with Monte Carlo



# A completely reconstructed $Y(4s)$ event at BaBar



All particles accounted for  
Nothing Missing !





# Measurement of $|V_{cb}|$

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$$\mathbf{V}_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & \boxed{V_{cb}} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \quad \mathbf{V}_{CKM} = \begin{pmatrix} 1-\lambda^2/2 & \lambda & A\lambda^3(\rho-i\eta) \\ -\lambda & 1-\lambda^2/2 & \boxed{A\lambda^2} \\ A\lambda^3(1-\rho-i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

$|V_{cb}|$  exclusive  $\longrightarrow$

# $|V_{cb}|$ from $B^0 \rightarrow D^{(*)}l\nu$ decays

Differential measurement of  $B(B^0 \rightarrow D^{(*)}l\nu)$  allows for the extraction of  $|V_{cb}|$  through the expression:

$w$  = product of the B and D 4-velocities  
 $q^2 = (p_B - p_D)^2$

$$\frac{d\Gamma}{dw} \propto |V_{cb}|^2 F^2(w) G(w)$$

Form factor of  $B \rightarrow D^*$  transition

Known kinematic factor

$$w = v_B \cdot v_D = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$

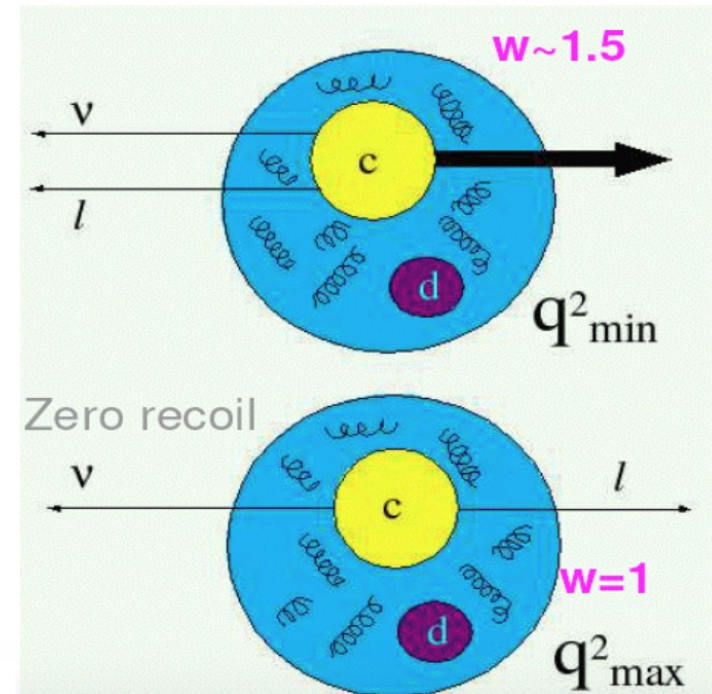
HQET and LQCD provide calculation at zero recoil

In reality the formula is slightly more complicated:

$$F^2(w)G(w) = h_{A_1}^2(w) \sqrt{w-1} (w+1)^2 \left\{ 2 \left[ \frac{1-2wr+r^2}{(1-r)^2} \right] \times \left( 1 + R_1(w)^2 \frac{w-1}{w+1} \right) + \left[ 1 + (1-R_2(w)) \frac{w-1}{1-r} \right]^2 \right\}$$

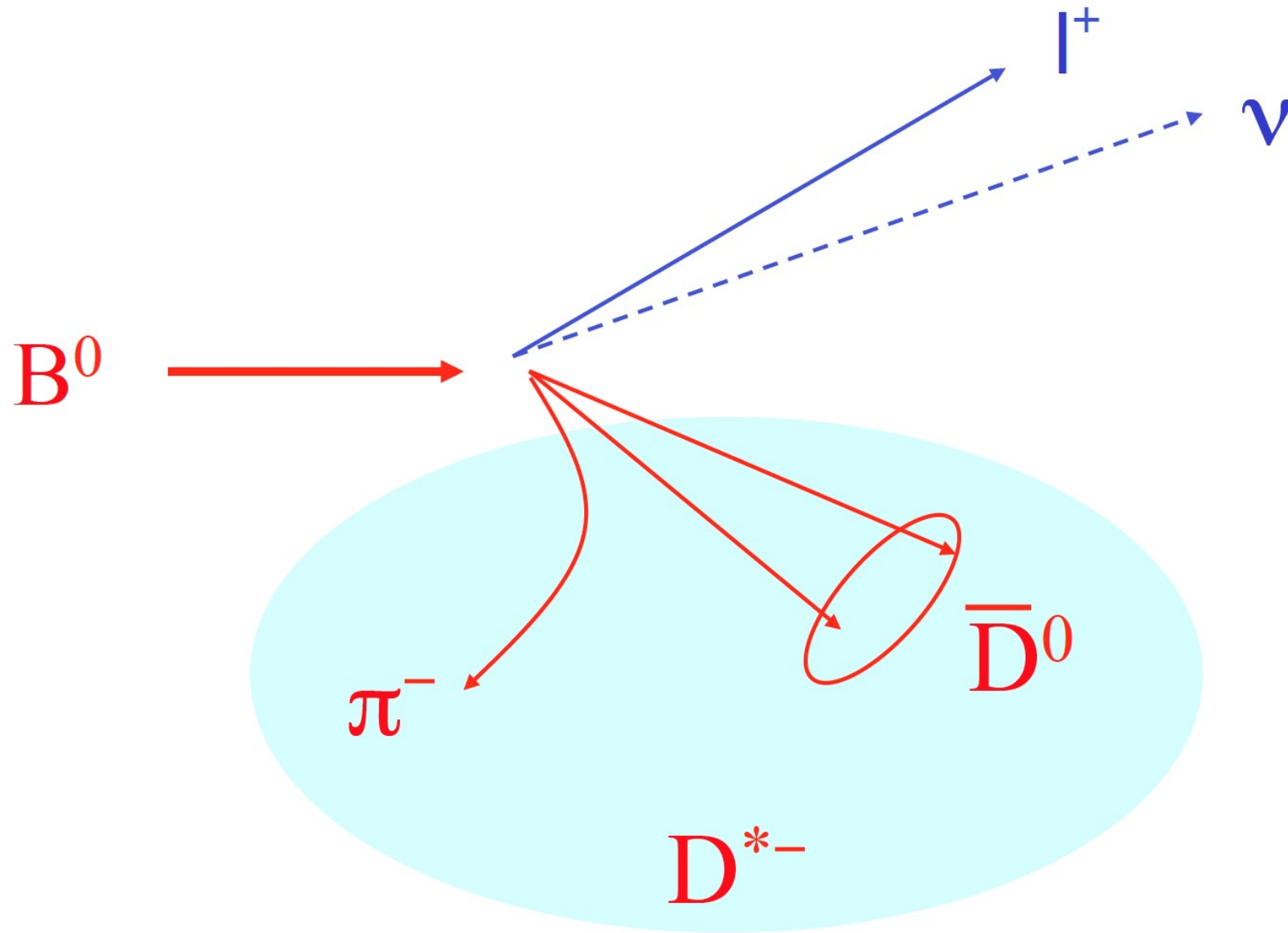
where  $r = \frac{M_{D^*}}{M_{B^0}}$

$F \rightarrow 1$  for  $w \rightarrow 1$



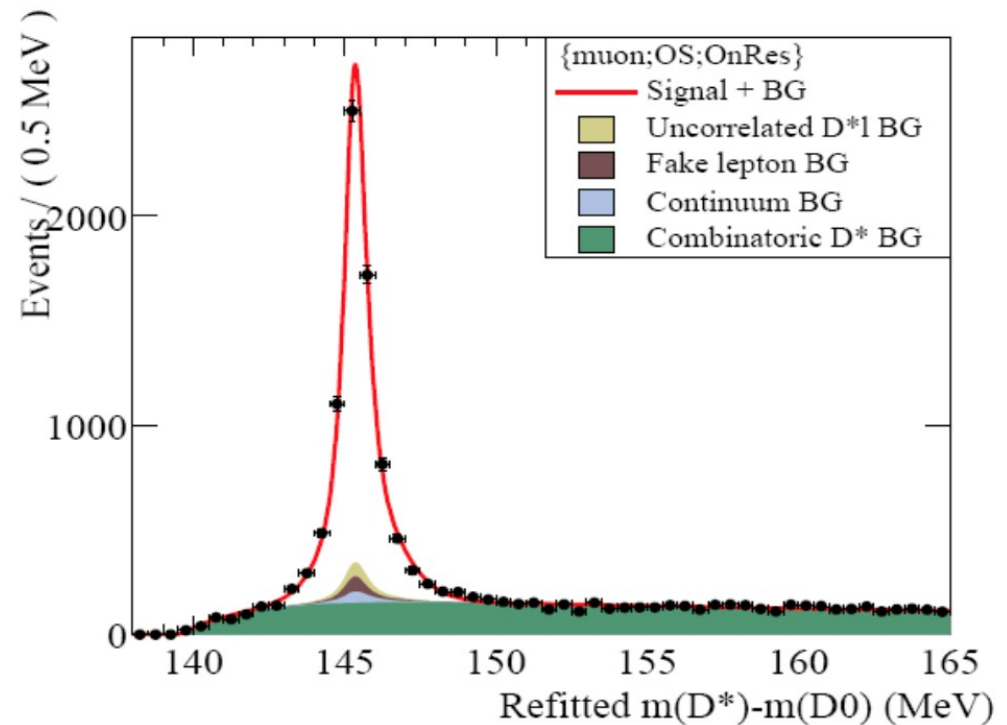
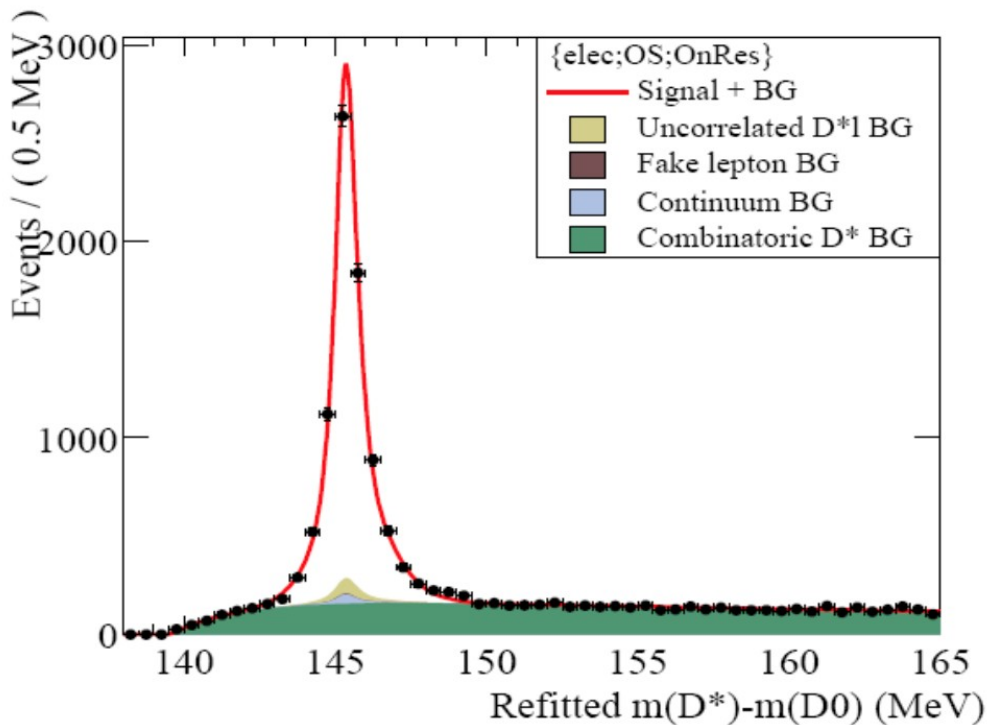
# $B^0 \rightarrow D^{(*)}l\nu$ decays

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# $D^{(*+ -)}D^0$ mass difference

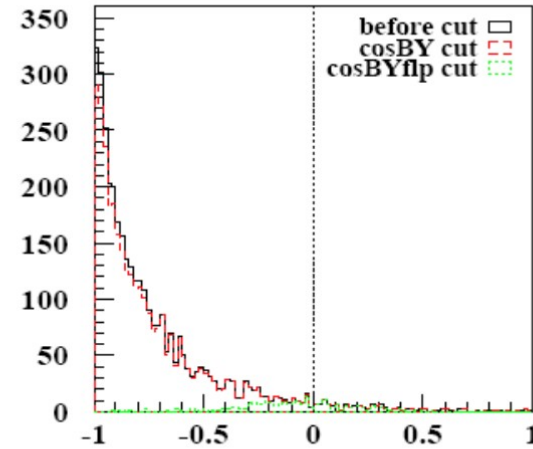
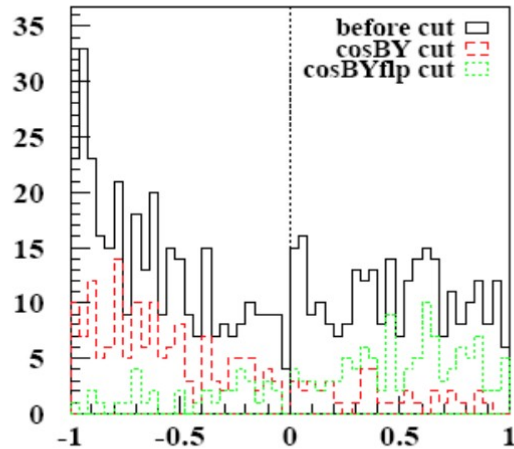
- $D^0$  mass: 1864 MeV
- $D^*$  mass: 2010 MeV
- Fixed momentum for soft pion
  - Only experimental resolution



# Angular Variables for $B^0 \rightarrow D^{(*)}l\nu$ selection

- Angle between  $D^*$  and lepton

Background

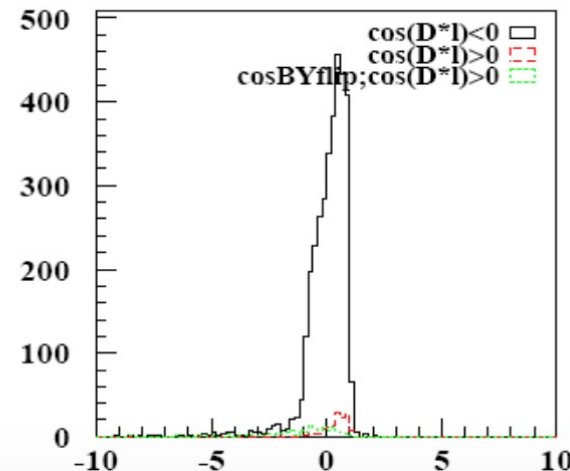
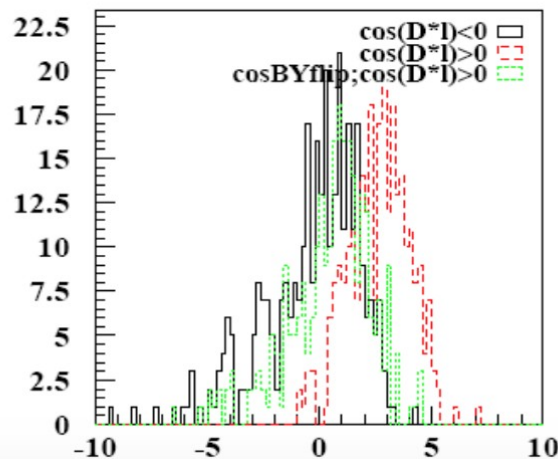


Signal

- Angle between  $B^0$  and the  $D^*l$  system
  - From kinematic quantities since B direction not measured

$$\cos\theta_{B^0,D^*l} = \frac{-(m_{B^0}^2 + m_{D^*l}^2 - 2E_{B^0}E_{D^*l})}{2|\vec{p}_{B^0}||\vec{p}_{D^*l}|}$$

Background



Signal

# Extraction of $|V_{cb}|$

## Measurement:

- Determine number of  $B^0 \rightarrow D^{*-} l^+ \nu$  candidates as function of  $w$
- Obtain  $h_{A1}(w)|V_{cb}|$  distribution
- Fit differential spectrum and extrapolate to  $w=1$

In BaBar:

$$h_{A1}(1)|V_{cb}| = (35.5 \pm 0.3_{stat} \pm 1.6_{syst})$$

and using

$$h_{A1}(w=1) = 0.919^{+0.030}_{-0.035}$$

Hashimoto et al.  
PRD 66, 014503  
(LQCD)

$$|V_{cb}| = (38.7 \pm 0.3_{stat} \pm 1.7_{syst} \pm 1.5_{1.3A1}) \times 10^{-3}$$

