



If we consider the same min square error loss function since we have

$$\left. \begin{aligned} z &= \sigma^*(W^3 \sigma^2) \\ \sigma^2 &= \sigma^*(W^2 \sigma^1) \\ \sigma^1 &= \sigma^*(W^1 X) \end{aligned} \right\} \Rightarrow z = \sigma^*(W^3 \sigma^*(W^2 \sigma^*(W^1 X)))$$

we considered min square error as loss function so:

$$J(w) = \frac{1}{2m} \sum_{\text{seq}^{(s)}} \sum_k t_k^{(s)} - z_k^{(s)}$$

$$\frac{\partial J}{\partial w_3} = \frac{\partial J}{\partial z} \times \frac{\partial z}{\partial w_3}$$

$$\frac{\partial J}{\partial w_2} = \frac{\partial J}{\partial z} \times \frac{\partial z}{\partial w_3} \times \frac{\partial w_3}{\partial \sigma^2} \times \frac{\partial \sigma^2}{\partial w^2}$$

$$\frac{\partial J}{\partial w_1} = \frac{\partial J}{\partial z} \times \frac{\partial z}{\partial w_3} \times \frac{\partial w^3}{\partial \sigma^2} \times \frac{\partial \sigma^2}{\partial w^2} \times \frac{\partial w^2}{\partial \sigma^1} \times \frac{\partial \sigma^1}{\partial w_1}$$

* σ is element wise sigmoid of corresponding entry