

LCD (24/02)

Calculus of Communicating Systems (Milner, '80)

CCS

pb: Which kind of communication?



\* ether

- ① send is always possible <sup>unless full</sup> (~~unbounded~~)
- ② receive is possible (if there are messages)
- ③ no order guarantee

\* buffer (bounded)

- ①, ②
- ③ order of messages is maintained

\* shared memory

- ① sending → writing to memory
- ② receiving → reading from memory
- ③ no order guarantee

⋮

Idea: no distinction between

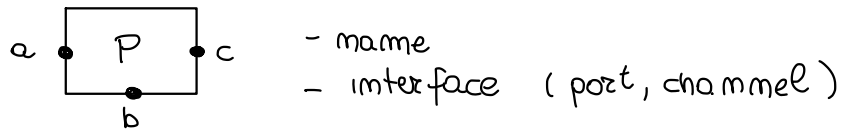
- active entities (agents)
- passive " (medium)

EVERYTHING IS A PROCESS



PROCESS : interacting through synchronous message passing

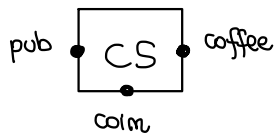
STRUCTURE :



BEHAVIOUR : CCS program

- structure
- interactions

Example : Computer scientist



Syntax of CCS

\* Inaction (nil)

$0$                       dead lock

\* Action prefixing

given a channel coin, coffee

$\overline{\text{coin}} . 0$

$\text{coffee} . 0$

$\overline{\text{coin}} . \text{coffee} . 0$

$\overline{\text{pub}} . \overline{\text{coin}} . \text{coffee} . 0$

in general, given a channel  $c$  and process  $P$

$c . P$                        $\overline{c} . P$

\* Process Constants

$$\text{Break} \stackrel{\text{def}}{=} \overline{\text{coin}}. \text{coffee}. 0$$

$$\text{Clock} \stackrel{\text{def}}{=} \overline{\text{tick}}. \text{Clock}$$

$$\text{CM} \stackrel{\text{def}}{=} \text{coin}. \overline{\text{coffee}}. \text{CM}$$

$$\text{CS} \stackrel{\text{def}}{=} \overline{\text{pub}}. \overline{\text{coin}}. \text{coffee}. \text{CS}$$

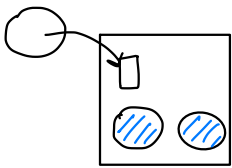
\* Non deterministic Choice

given processes P, Q one construct  $P + Q$

$$\text{CTM} \stackrel{\text{def}}{=} \text{coin}. ( \overline{\text{coffee}}. \text{CTM} + \overline{\text{tea}}. \text{CTM} )$$

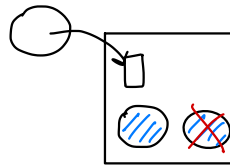
?  $\left[ \text{CTM}'_1 \stackrel{\text{def}}{=} \text{coin}. ( \overline{\text{coffee}} + \overline{\text{tea}} ). \text{CTM} \right]$  NOT IN THE SYNTAX  
 • is not sequential composition

$$\text{CTM}' \stackrel{\text{def}}{=} \text{coin}. \overline{\text{coffee}}. \text{CTM}' + \text{coin}. \overline{\text{tea}}. \text{CTM}'$$



CTM

$\neq$



CTM'

same sequences of interactions (same traces)

EXERCISE : Broken Clock

it emits a tick and then it can stop after any number of ticks

$$\text{Clock} \stackrel{\text{def}}{=} \overline{\text{tick}}. \text{Clock}$$

$$\text{BC} \stackrel{\text{def}}{=} \text{tick}. (\text{BC} + 0)$$

$$\text{BC} + 0 \sim \text{BC}$$

$$\text{BC} \stackrel{\text{def}}{=} \text{tick}. \text{BC} + \text{tick}. 0$$

EXERCISE : Failing coffee machine

$$CM \stackrel{\text{def}}{=} \text{coin} . \overline{\text{coffee}} . CM$$

→ can get a coin and provide nothing

→ at any moment, can fail emitting a  $\overline{\text{fail}}$  message

$$BCM \stackrel{\text{def}}{=} \text{coin} . (\overline{\text{coffee}} . BCM + \overline{\text{fail}} . 0 + BCM) + \overline{\text{fail}} . 0$$

$$BCM \stackrel{\text{def}}{=} \text{coin} . \overline{\text{coffee}} . BCM + \text{coin} . BCM + \overline{\text{fail}} . 0$$

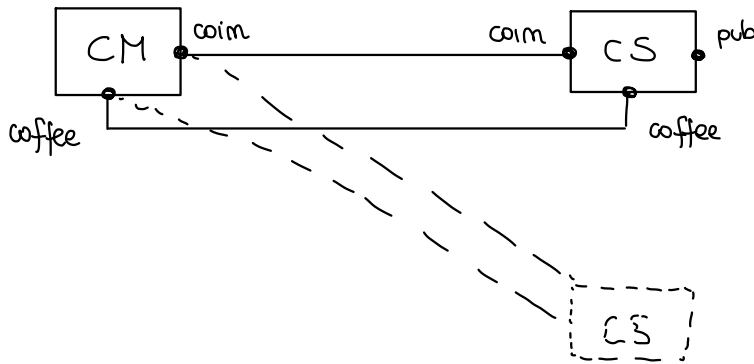
??

\* Parallel Composition

given two processes P, Q you can consider  $P | Q$

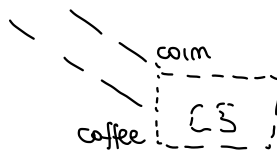
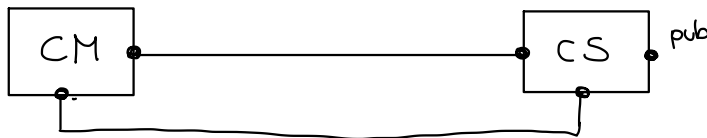
$$CM \stackrel{\text{def}}{=} \underline{\text{coin}} . \overline{\text{coffee}} . CM$$

$$CS = \overline{\text{pub}} . \underline{\text{coin}} . \overline{\text{coffee}} . CS$$



\* RESTRICTION

$$(CM | CS) \setminus \{ \text{coin}, \text{coffee} \}$$



\* Rebellioning

$$\text{CHOC} \stackrel{\text{def}}{=} \text{coim. } \overline{\text{choc}} . \text{CHOC}$$

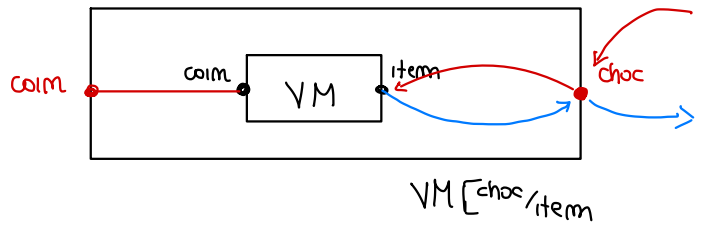
$$\text{CHIPS} \stackrel{\text{def}}{=} \text{coim. chips. CHIPS}$$

⋮

$$\text{VM} \stackrel{\text{def}}{=} \text{coim. } \overline{\text{item}} . \text{VM}$$

$$\text{CHOC} = \text{VM} \left[ \begin{array}{l} \text{choc} \\ \text{item} \end{array} \right]$$

$$\text{CHIPS} = \text{VM} \left[ \begin{array}{l} \text{chips} \\ \text{item} \end{array} \right]$$



\* BEHAVIOUR

focus on interactions

→ state transitions

→ triggered by communications (send / receive)

$$P \xrightarrow{\text{com}} P'$$

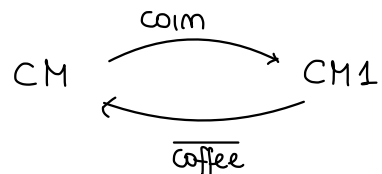
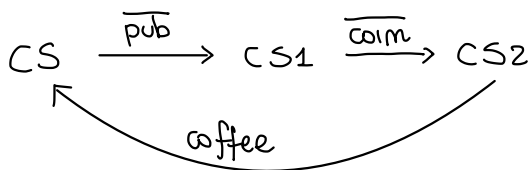
$$\text{CS} = \overline{\text{pub}} . \text{CS1}$$

$$\text{CS1} = \overline{\text{coim}} . \text{CS2}$$

$$\text{CS2} = \text{coffee} . \text{CS}$$

$$\text{CM} = \text{coim} . \text{CM1}$$

$$\text{CM1} = \overline{\text{coffee}} . \text{CM}$$



$$\text{CS} \mid \text{CM}$$

$$\downarrow \overline{\text{pub}}$$

$$\text{CS1} \mid \text{CM}$$

$$\xrightarrow{\tau} \text{CS2} \mid \text{CM1}$$

~~coim/coim~~

↑

invisible action / silent action

# System "Office"

$$CS = \overline{pub}. CS1$$

$$CS1 = \overline{coim}. CS2$$

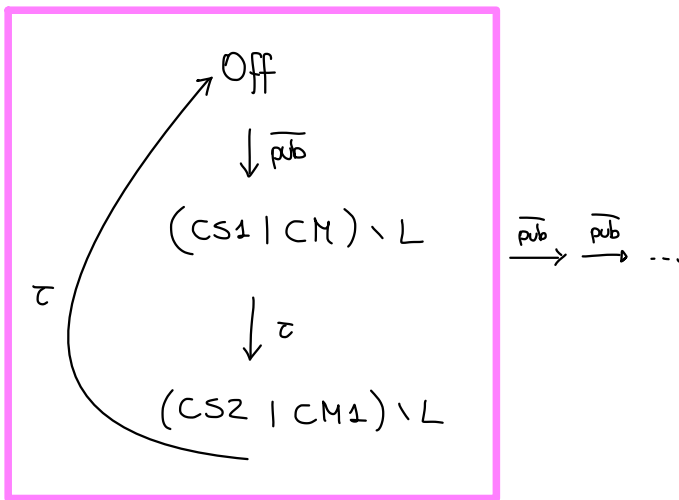
$$CS2 = \overline{coffee}. CS$$

$$CM = \overline{coim}. CM1$$

$$CM1 = \overline{coffee}. CM$$

$$Off = (CS \mid CM) \setminus L$$

$$L = \{coim, coffee\}$$



$$Spec = \overline{pub}. Spec$$

$$\downarrow \overline{pub}$$

$$\downarrow \overline{pub}$$

Spec

~

Off

↑  
implementation

We need

- syntax
- operational behaviour
- program equivalence
- verification algorithms and tools