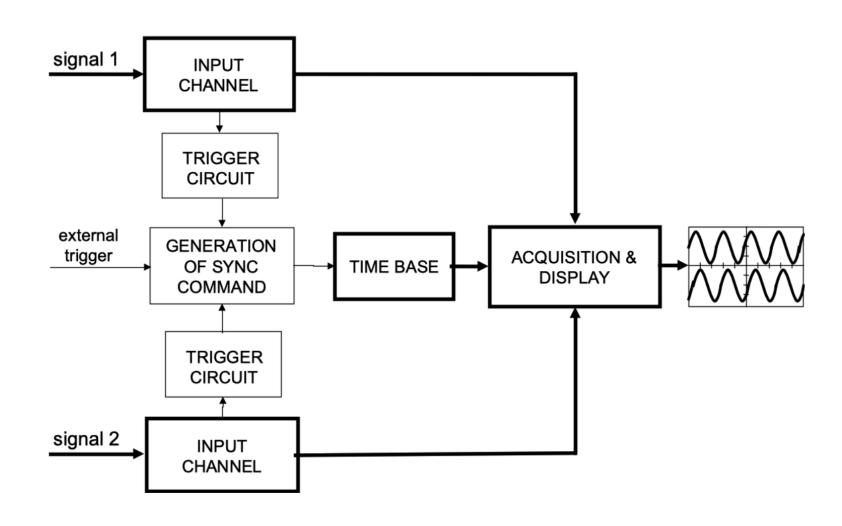


Oscilloscope analog front end

Lecture #3
Electronic measurements
Claudio Narduzzi, Alessandro Pozzebon

The oscilloscope





Input channel functions

- Amplify or attenuate the signal
- Realize a stable **input impedance**
- Provide a choice of coupling modes

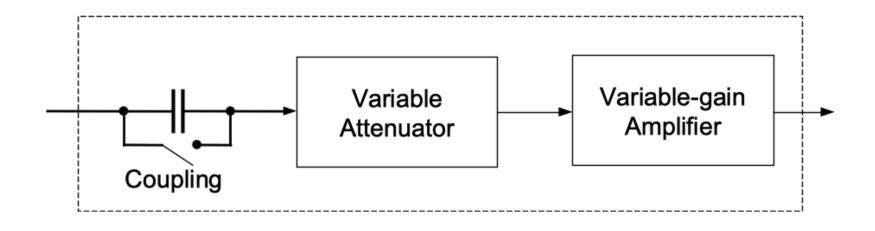


- Variable-gain amplifiers
- Attenuators
- Filters
- Coupling circuits

Configured through the processors



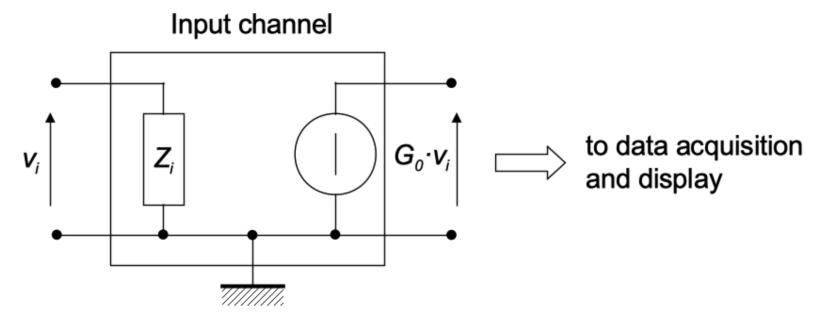
Input channel functions



- 2-4 channels
- Simultaneous acquisition of different signals
- Common time reference
- Separate vertical scale settings

Input channel model

Voltage controlled generator



- Input impedance Z_i
- Frequency response G(f)
- Static gain $G_0 = G(0)$
- Calibrated vertical scale factor $1/G_0$



Calibration through comparison with **known DC voltage levels**

Input impedance

- Input impedance Z_i as large as possible
- Parallel of a large resistance R_i and a small capacitance C_i
- $R_i = 10 \text{ M}\Omega$, $C_i = 10 20 \text{ pF}$
- Low frequencies $\Rightarrow |Z_i| \cong R_i \Rightarrow \text{Negligible loading effect}$
- **High frequencies** ⇒ Capacitive reactance ⇒ impedance drop

$$Z_i = R_i \frac{1}{1 + j\omega R_i C_i}$$



Input impedance

 $R_i = 1 M\Omega$ and $C_i = 15 pF$

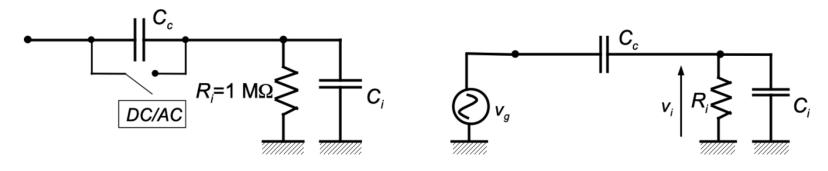
f	R_i	$ X_i $	$ Z_i $
0	$1~\mathrm{M}\Omega$	∞	$1~\mathrm{M}\Omega$
1 kHz	$1~\mathrm{M}\Omega$	$10~\mathrm{M}\Omega$	$900 \text{ k}\Omega$
1 MHz	$1~\mathrm{M}\Omega$	$10~\mathrm{k}\Omega$	$10~\mathrm{k}\Omega$
10 MHz	$1~\mathrm{M}\Omega$	$1~\mathrm{k}\Omega$	$1~\mathrm{k}\Omega$
100 MHz	$1~\mathrm{M}\Omega$	100 Ω	$100~\Omega$

- **Lower input impedance** ⇒ larger current absorption at higher frequencies
- High input impedance: limited loading effect
- 50 Ω input impedance: matched impedance \Rightarrow wavelength comparable to the physical size of circuits

 $\downarrow \downarrow$

avoid reflections

- Direct-current (DC) coupling: the whole signal, including its DC component, is acquired
- Alternating-current (AC) coupling: only the alternating is acquired

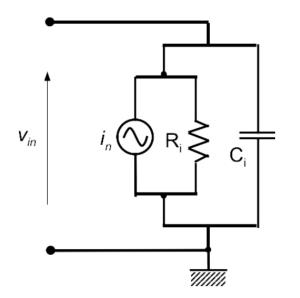


$$V_i(s) = V_g(s) \cdot \frac{j\omega R_i C_c}{1 + j\omega R_i (C_c + C_i)}$$

- High pass filter
- -3 dB cut-off frequency ~ 10 Hz
- C_c in the order of some tens of nF $\Rightarrow C_c \gg C_i$

Sensitivity and noise

- Thermal noise: random motion of electrons
- Power spectral density kT [W/Hz] (k Boltzmann constant = $1.38 \times 10^{-23} \text{ J/K}$)
- Noise power is generated by an equivalent current source i_n in parallel to the "noiseless" input resistance R_{in}

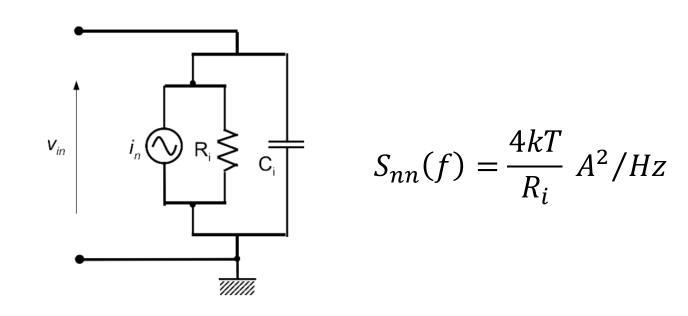


$$S_{nn}(f) = \frac{4kT}{R_i} A^2/Hz$$

• Noise voltage v_{in} is produced by the noise current i_n flowing through the input impedance Z_i and is displayed as additive noise superposed on the measured signal

Sensitivity and noise

- Thermal noise: random motion of electrons
- Power spectral density kT [W/Hz] (k Boltzmann constant = $1.38 \times 10^{-23} \text{ J/K}$)



Input noise variance

$$E[v_{in}^{2}] = \frac{4kT}{R_{i}} \cdot \frac{1}{2\pi} \int_{0}^{+\infty} \frac{R_{i}^{2}}{1 + \omega^{2}(R_{i}C_{i})^{2}} d\omega = 4kT \cdot \frac{1}{2\pi} \frac{\pi}{2R_{i}C_{i}}$$

Sensitivity and noise

•
$$v_{in(RMS)} = \sigma_n = \sqrt{\frac{kT}{c_i}}$$

- Determined by the the equivalent noise of the input RC circuit
- Smaller levels of C_i lead to higher levels of noise
- $C_i = 10 \text{ pF} \text{ and } T = 300 \text{ K} \Rightarrow v_{in(RMS)} \cong 20 \,\mu\text{V}$
- Signal-to-Noise Ratio (SNR)
 - Uniform probability density function for signals within the input voltage range $\pm V_{FS} \Rightarrow Variance \sigma_S^2 = V_{FS}^2/3$
 - $SNR_{thermal} = \frac{V_{FS}^2}{3} \frac{C_i}{kT}$

Dynamic characteristics

• Flatness: maximum deviation of |G(f)| from the DC value

flatness =
$$\frac{max_j|G(f)-G(0)|}{G(0)}$$

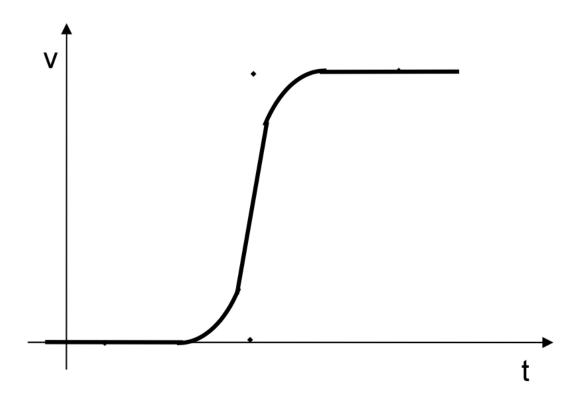
- Non distortion conditions
- Linear frequency response with:
 - Constant magnitude
 - Linear phase (constant group delay)

Dynamic characteristics: Step response

- Faithful waveform reproduction in the time domain
- Step response:
 - Shortest possible rise time
 - No overshoot

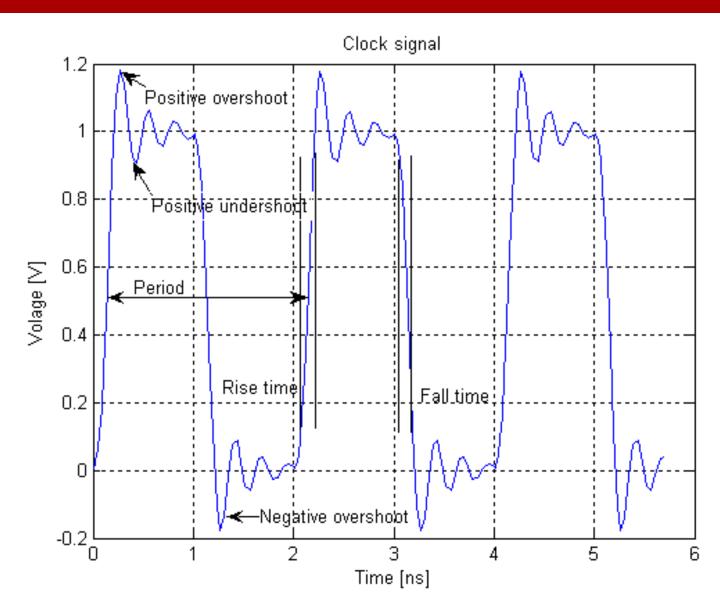
- Follow any voltage variation avoiding the creation of artifacts
- Linear system with Gaussian impulse response

$$g(t) = A \cdot e^{-(t-\tau_0)^2}$$





Dynamic characteristics: Step response



Dynamic characteristics: Rise time

- Signals with sharp edges (digital signals or clock signals)
- Edge not distorted
 - Significant high-frequency contributions
 - Instrument bandwidth limitations
- Rise time: time required for the transition between two levels

Dynamic characteristics: Rise time

- T_r: oscilloscope rise time
- T_v: visualized rise time
- T_s: signal rise time
- Relative deviation from T_s :

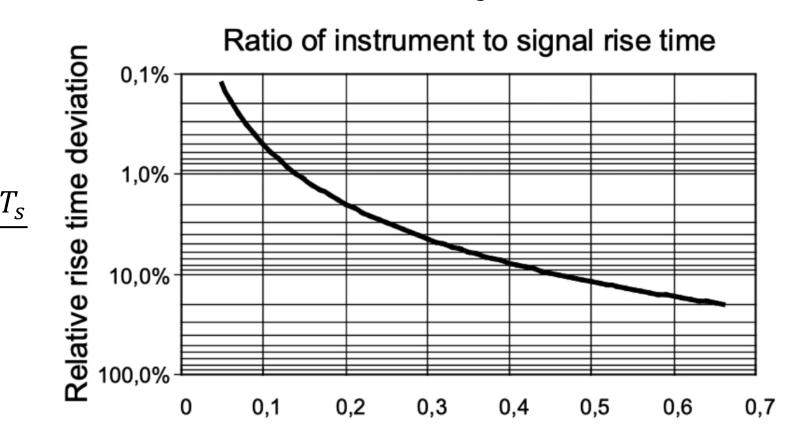
$$\frac{T_v - T_s}{T_s}$$

$$T_v \cong \sqrt{T_s^2 + T_r^2}$$

• To make the difference from T_v negligible, $T_r \ll T_s$

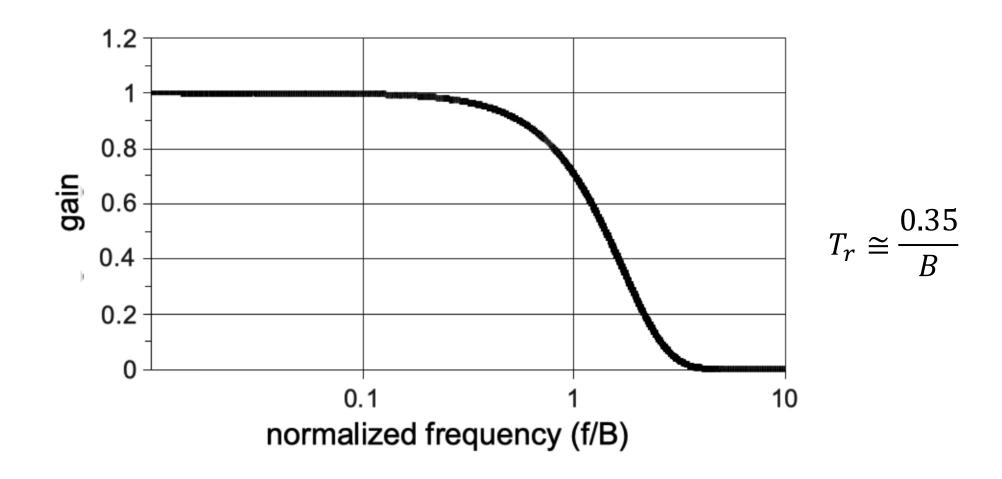
Dynamic characteristics: Rise time

 $\frac{T_r}{T_s}$



Frequency response

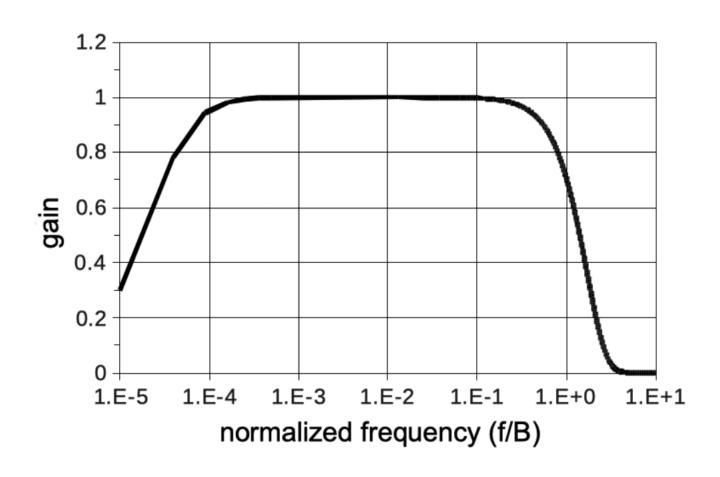
• B \Rightarrow -3 dB bandwidth \Rightarrow attenuation about 30%



Frequency response

- The frequency response may present some ripple ⇒ flatness
- Two parallel paths for broad band amplification
 - DC-coupled low-frequency
 - AC-coupled high-frequency (cross-over frequency around 1 kHz)
- Output noise higher for higher-gain circuits → Different vertical scale factor,
 different noise level

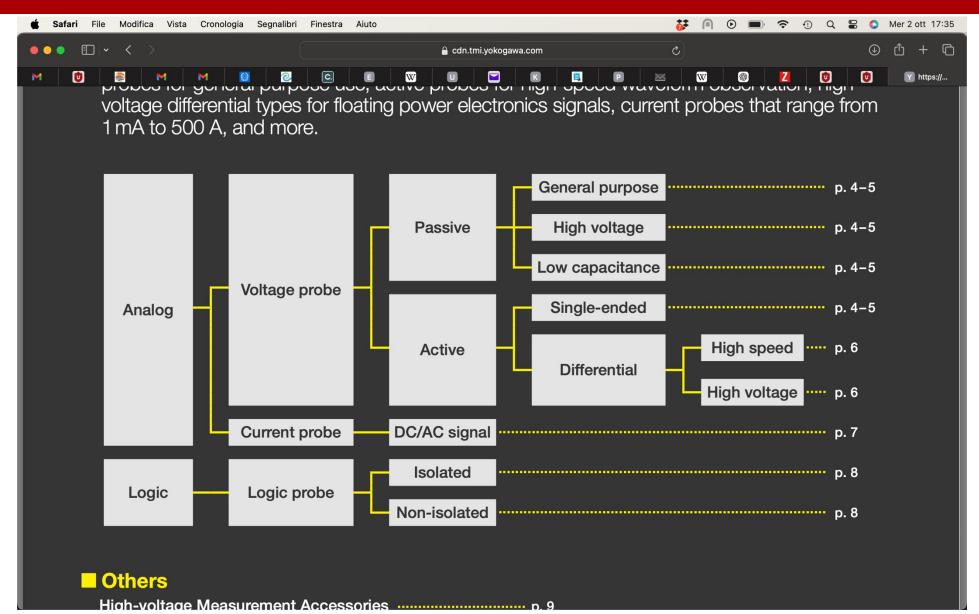
Frequency response with AC coupling











- Connections are circuits with their own parameters
- Connections may alter the circuit behaviour (Loading effect)
- Length is comparable to the wavelength ⇒ **Transmission lines**

- Probe: device enabling to pick up the signal of interest and take it to the input connectors of the measuring instrument
- A pair of conductors, a coaxial cable and a BNC connector
 - Reduce the loading effect
 - Avoid signal distortion
 - Enable contact with test points

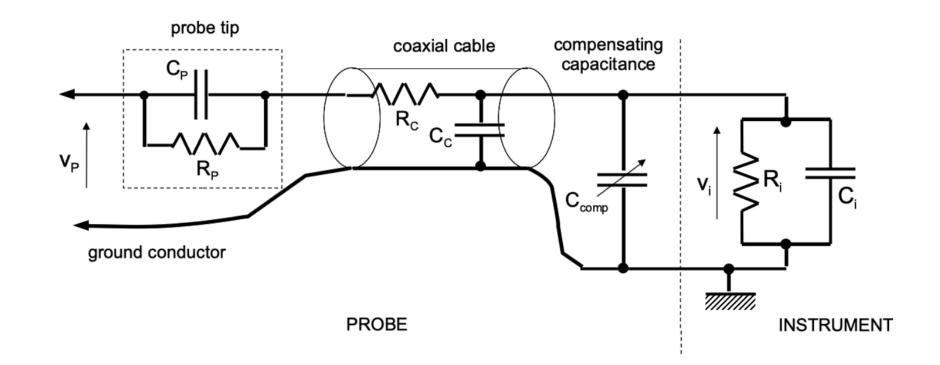
- Cable length ⇒ **Propagation effects**
- Propagation speed $v = 1/\sqrt{\epsilon \mu} = \frac{c}{\sqrt{\epsilon_r}}$
- Polyethylene $\Rightarrow \epsilon_r = 2.3 \Rightarrow v \cong 2 \times 10^8 \text{ m/s}$
- 1 m cable \Rightarrow 200 MHz sinewave
- Up to few MHz the cable can be described by a lumped-parameter electrical network

- Coaxial cables capacitance C_c : 0.5-2 pF/cm
- In parallel with the instrument input impedance

- A tip containing a parallel RC network
- A connector body, that contains a variable capacitor, placed in parallel to the BNC connector linking the probe to the oscilloscope
- A coaxial cable from the tip to the connector body

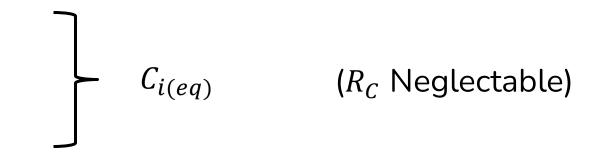
- Attenuation factor: ratio between the voltage v_x at the signal source and the voltage v_i at the oscilloscope input
- Typical factor 10

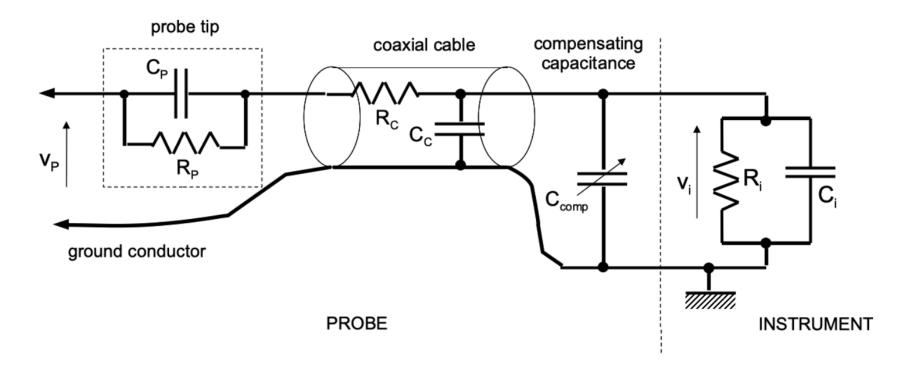
- Probe tip: C_p and R_p in parallel
- Coaxial cable: small R_c and C_c in series
- Compensation capacitance C_{comp}



Parallel:

- Oscilloscope input capacitance C_i
- Cable capacitance C_c
- Compensation capacitance C_{comp}

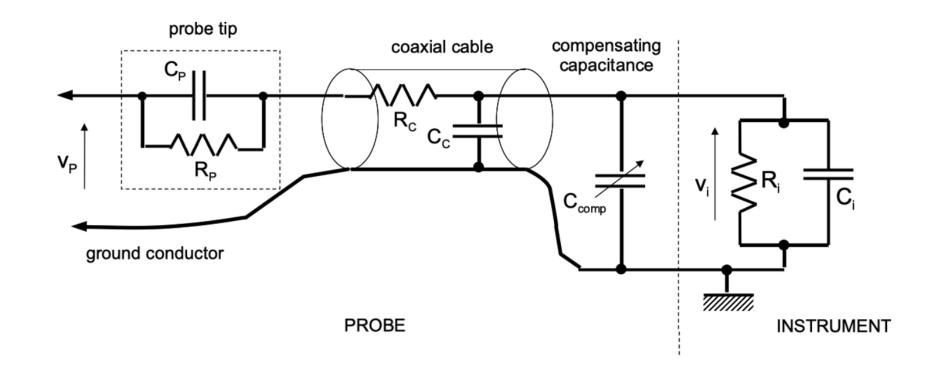




Series:

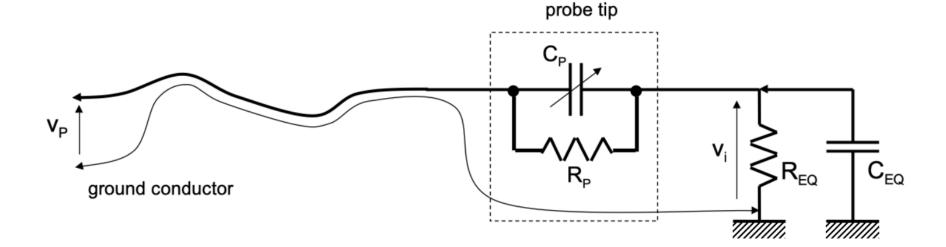
- Parallel in the probe tip
- $Z_{i(eq)}$ (parallel of $C_{i(eq)}$ and R_i)

- Constant input $\Rightarrow v_i = v_p \frac{R_i}{R_i + R_p}$
- $R_p = 9R_i$



- Probe impedance $Z_p(s) = R_p \frac{1}{1 + sR_pC_p}$
- Input impedance $Z_{i(eq)}(s) = R_i \frac{1}{1 + sR_iC_{i(eq)}}$

$$\frac{1}{\alpha_{probe}} = \frac{R_i \frac{1}{1 + sR_i C_{i(eq)}}}{R_p \frac{1}{1 + sR_p C_p} + R_i \frac{1}{1 + sR_i C_{i(eq)}}}$$



- Probe impedance $Z_p(s) = R_p \frac{1}{1 + sR_pC_p}$
- Input impedance $Z_{i(eq)}(s) = R_i \frac{1}{1 + sR_iC_{i(eq)}}$

$$\frac{1}{\alpha_{probe}} = \frac{R_i \frac{1}{1 + sR_i C_{i(eq)}}}{R_p \frac{1}{1 + sR_p C_p} + R_i \frac{1}{1 + sR_i C_{i(eq)}}}$$

$$R_P C_P = R_i C_{i(eq)}$$

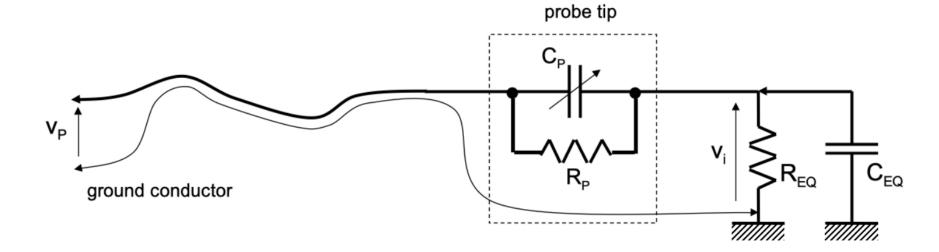
$$\alpha_{probe} = \frac{R_P + R_i}{R_i}$$
 Independent of frequency

Equivalent impedance:

$$Z_{EQ}(s) = R_p \frac{1}{1 + sR_p C_p} + R_i \frac{1}{1 + sR_i C_{i(eq)}}$$

Compensation condition satisfied:

$$Z_{EQ}(s) = (R_p + R_i) \frac{1}{1 + s(R_p + R_i) \frac{C_{i(eq)}}{\alpha_{probe}}}$$



• Equivalent impedance:

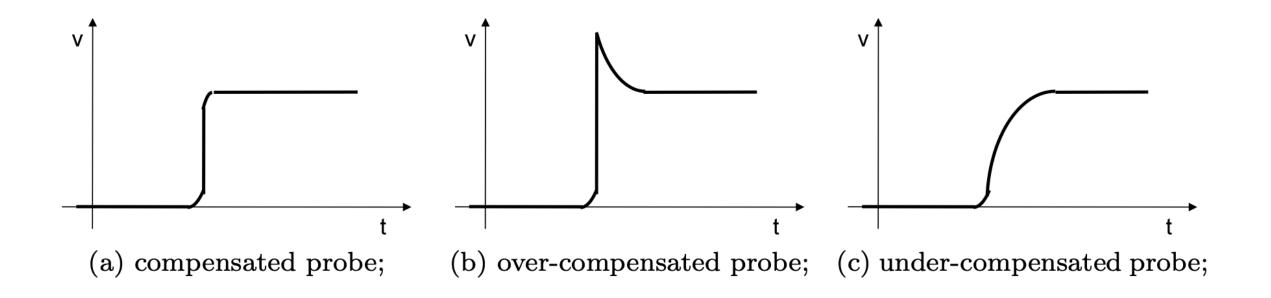
$$Z_{EQ}(s) = R_p \frac{1}{1 + sR_p C_p} + R_i \frac{1}{1 + sR_i C_{i(eq)}}$$

Compensation condition satisfied:

$$Z_{EQ}(s) = (R_p + R_i) \frac{1}{1 + s(R_p + R_i) \frac{C_{i(eq)}}{\alpha_{probe}}}$$

•
$$R_{EQ} = R_p + R_i = R_i \cdot \alpha_{probe}$$

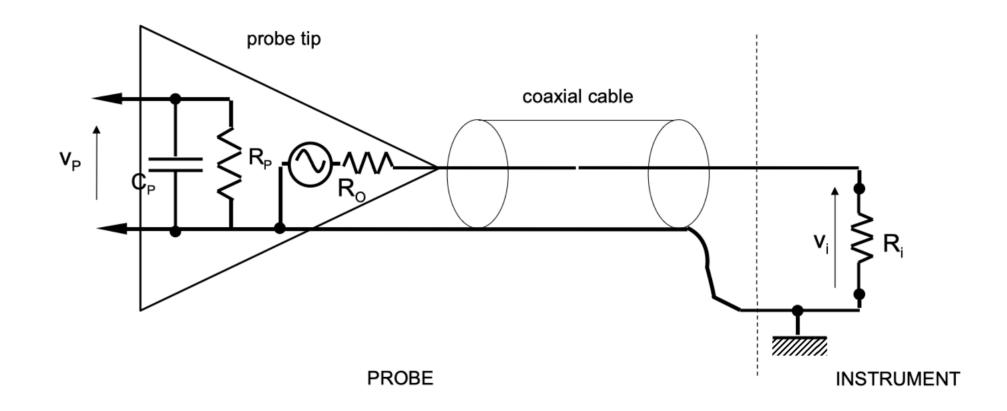
•
$$C_{EQ} = \frac{C_{i(eq)}}{\alpha_{probe}}$$



- Over-compensated: C too high \rightarrow Limited attenuation of the high order harmonics
- Under-compensated: C too small \rightarrow Larger attenuation of the high order harmonics

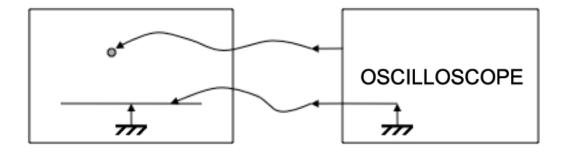


Active probes

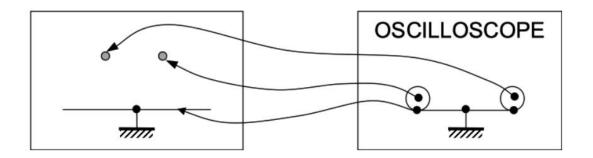


Pseudo-differential measurement

 Oscilloscopes feature a single-ended input with the ground reference connected to earth

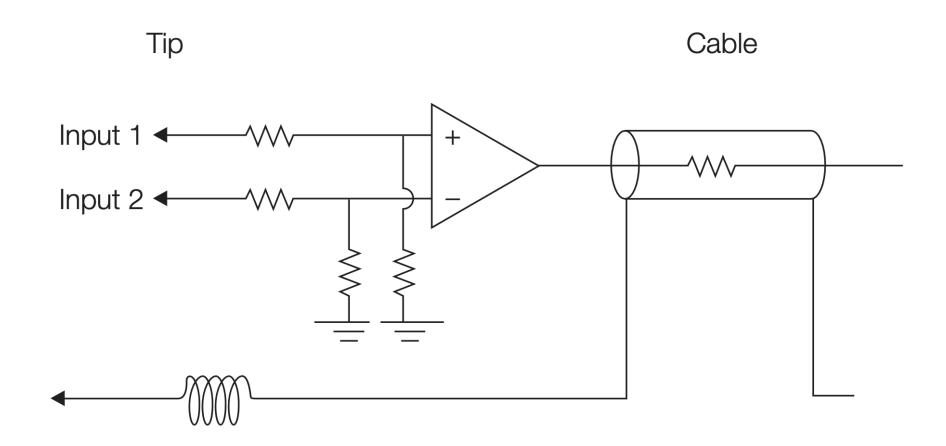


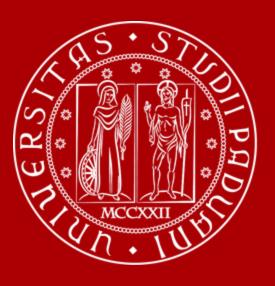
• Pseudo-differential measurement: measure the "voltage to ground" of the two points independently, then determine their difference





Differential probes





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