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Basic Laboratory Instrumentation

Lecture #2

Electronic measurements

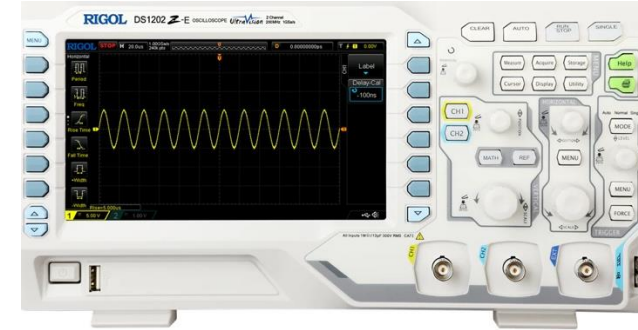
Alessandro Pozzebon



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Basic instrumentation

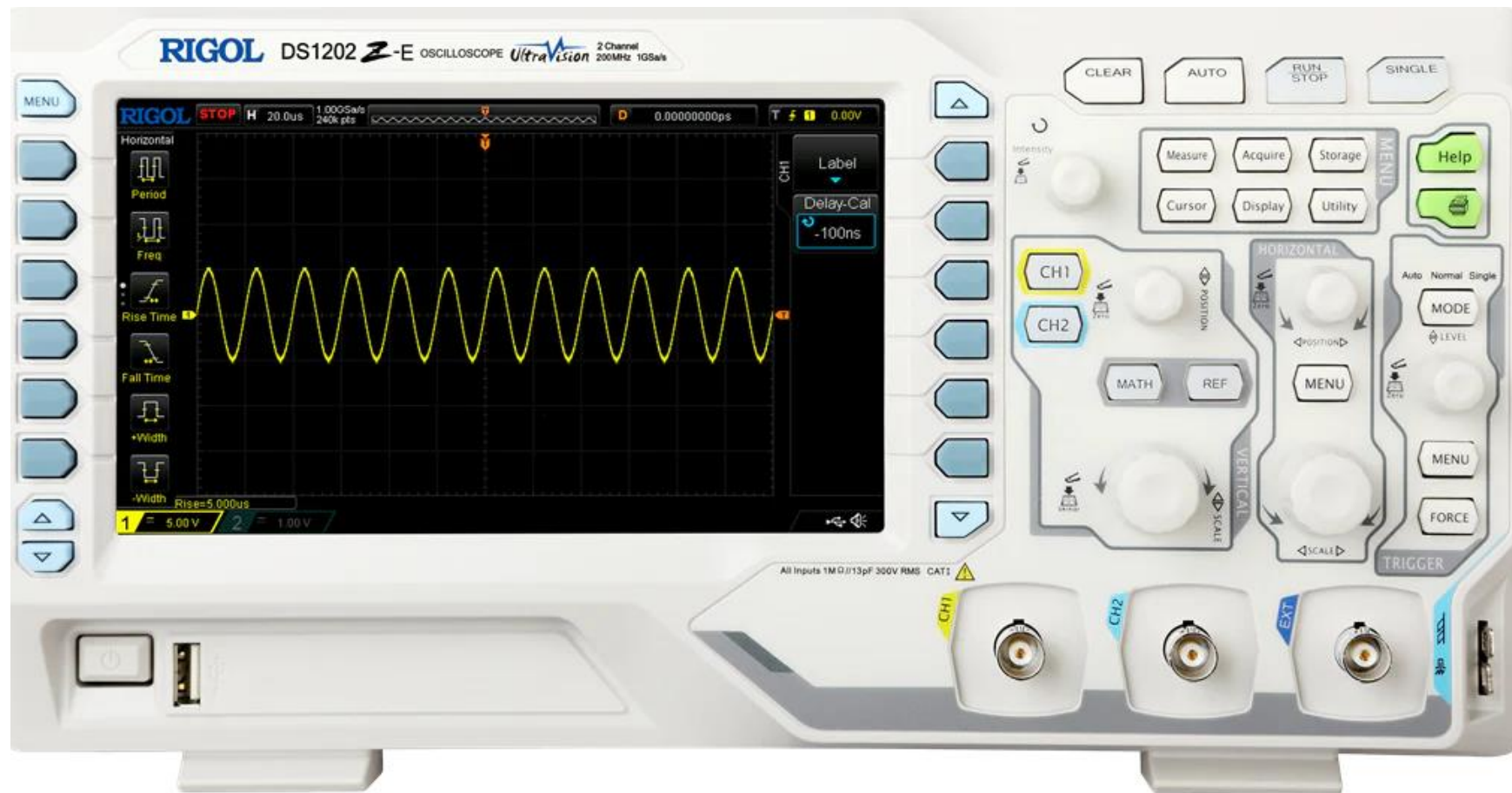
- Oscilloscope
- Signal Generator
- Digital multimeter





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Oscilloscope





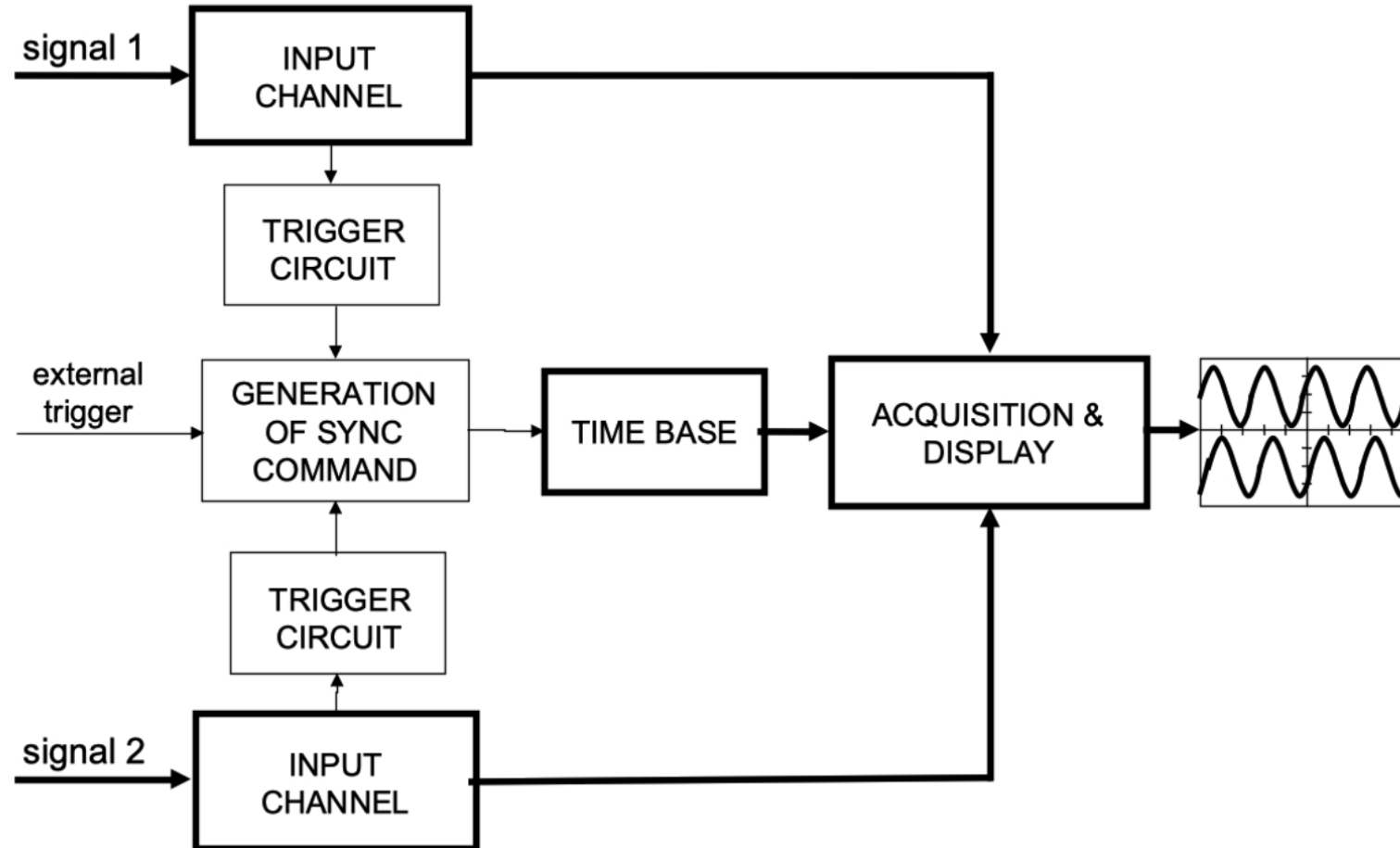
- **Waveform analysis:** the accurate measurement of signal behaviour
 - Observe
 - Measure
 - Compare
- **Diagnostics:** checking a system operation to detect possible anomalies and signal variations
- Finite **observation interval**
 - Synchronization
- Simultaneous acquisition of **2-4 signals**



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Oscilloscope

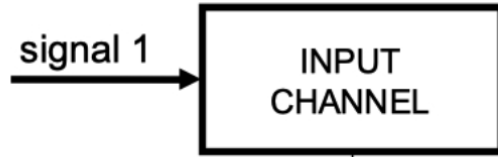
Functional scheme





Oscilloscope

Functional scheme

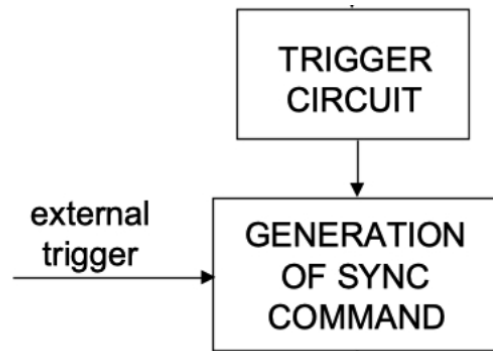


- Amplification and attenuation
- Bandwidth
 - From less than 100 MHz to several GHz
- **Input impedance** → as high as possible
 - Parallel of a resistance $R = 1 \text{ M}\Omega$ and a capacitance in the order of ten pF



Oscilloscope

Functional scheme



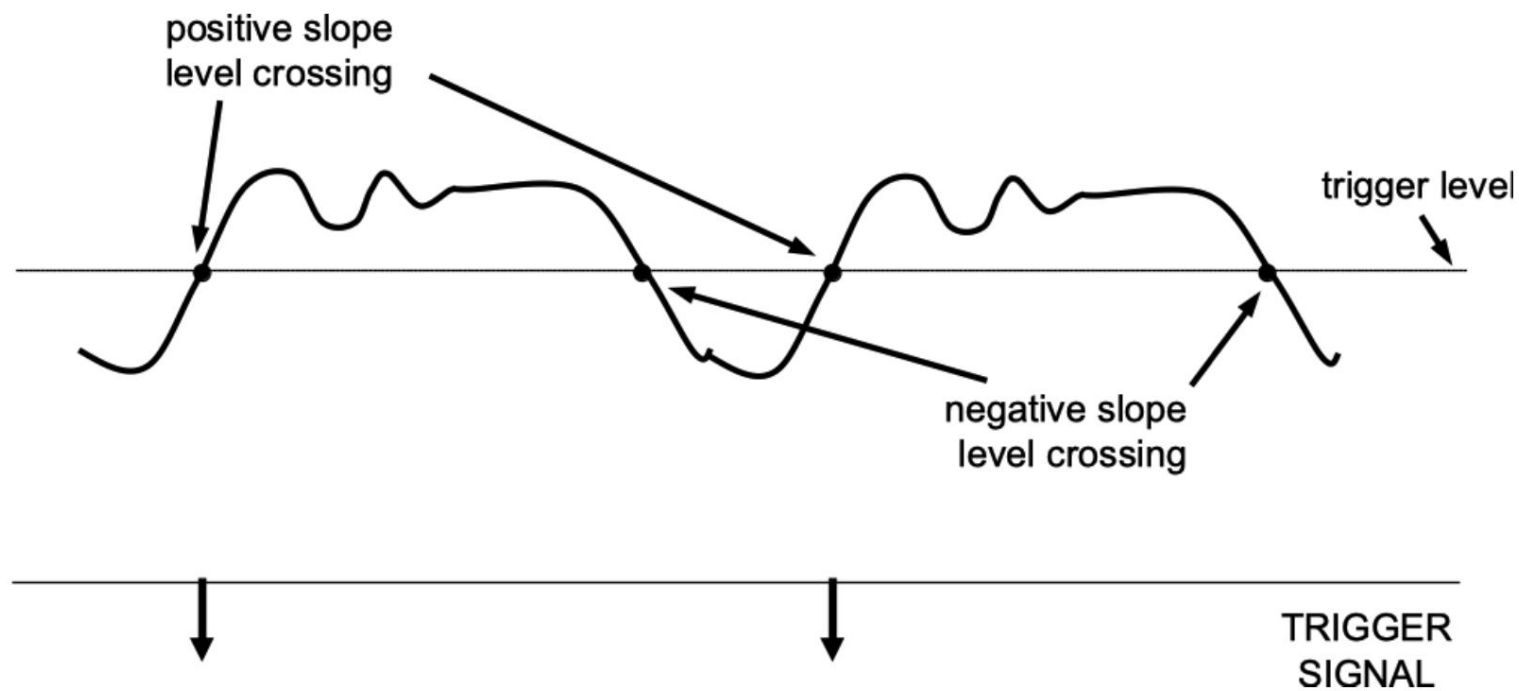
- Determine **reference points** to synchronize the instrument
- **Trigger event**: crossing of a preset voltage level
- **Synchronization command**: can combine multiple conditions and inputs
- **External trigger**



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Oscilloscope

Functional scheme





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Oscilloscope

Functional scheme

- **Internal time reference**
- Measurement of time intervals
- Observation interval length from **few ns to several s**
- **Calibrated** reference
- **Internal instrument clock**
- Crystal oscillator with relative uncertainty in the order of 10^{-4} to 10^{-6}





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Oscilloscope

Functional scheme

- **Digital Sampling Oscilloscope (DSO)**
- High speed data and acquisition system
- **Analog-to-Digital Converter (ADC)**
- Computing capabilities for **digital signal processing**
- Direct **measurements and signal analysis**



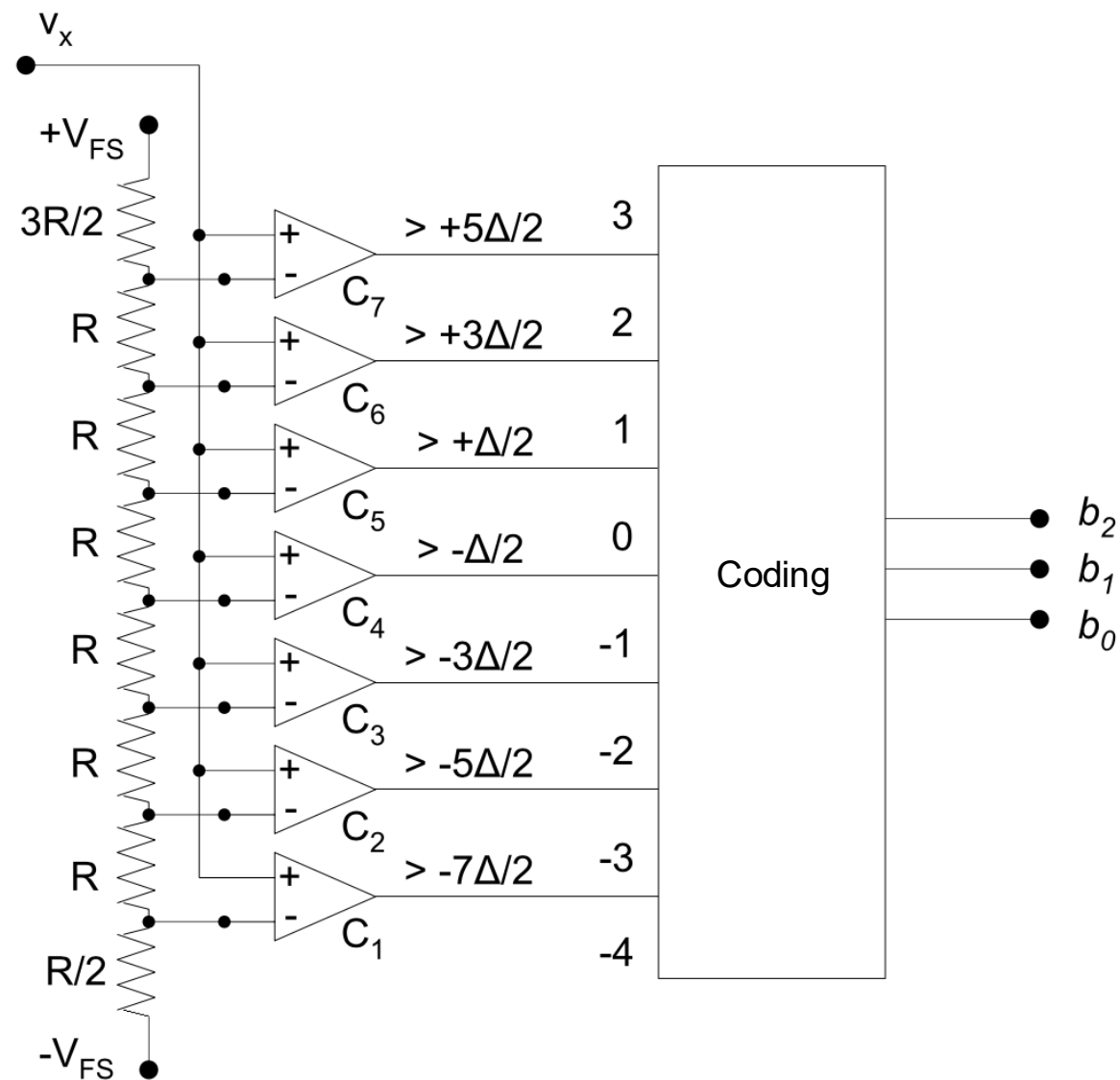


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Oscilloscope

Analogue to Digital conversion

Flash ADC

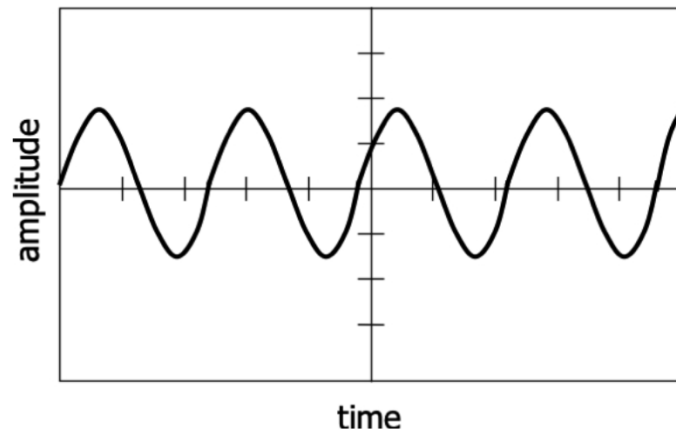




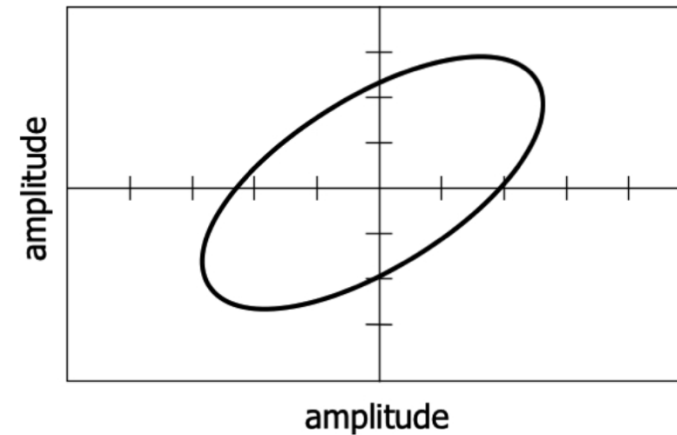
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Oscilloscope: visualization

- **x-t display** (voltage per division vs time per division)
 - Time base
- **x-y display** (voltage per division vs voltage per division)
 - Implicit time variable



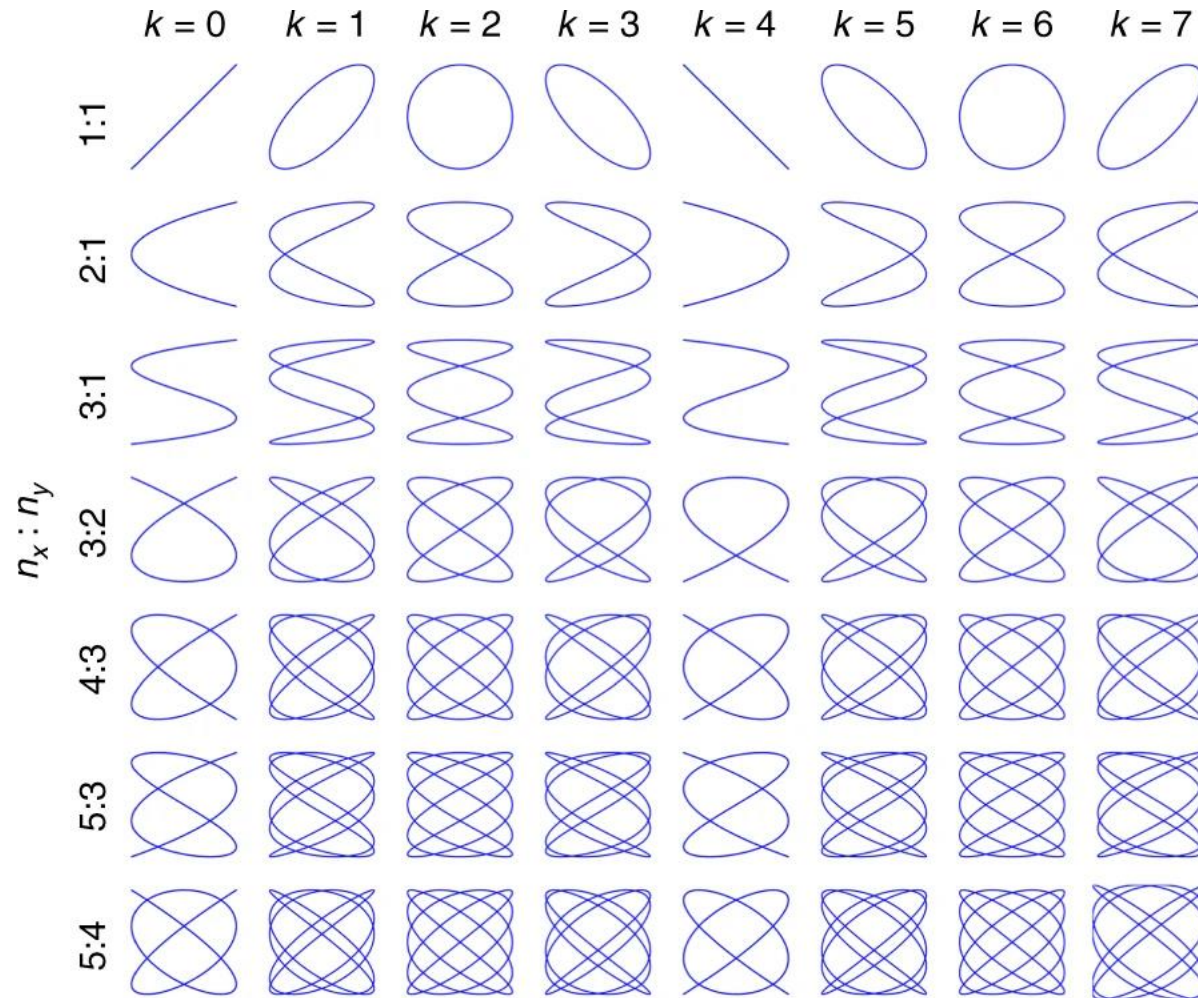
(a) amplitude versus time display



(b) XY display



Lissajous curves

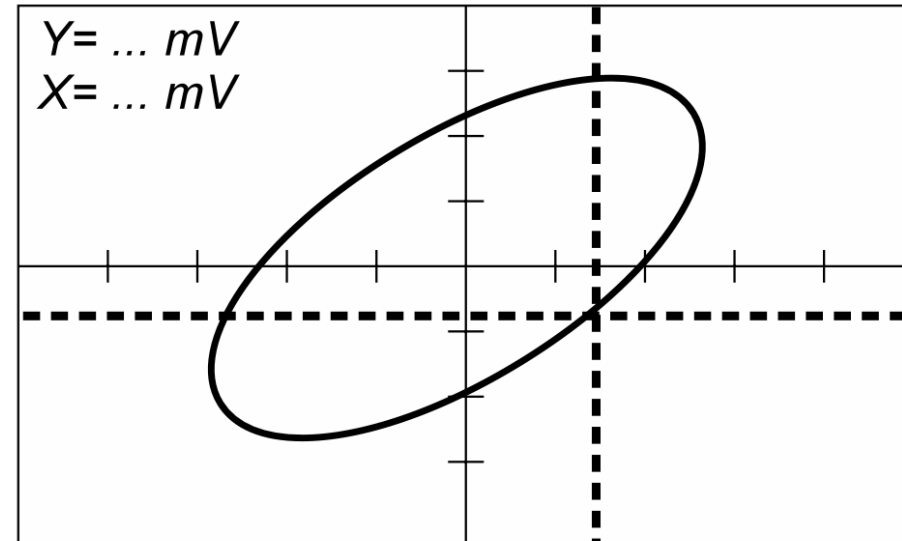
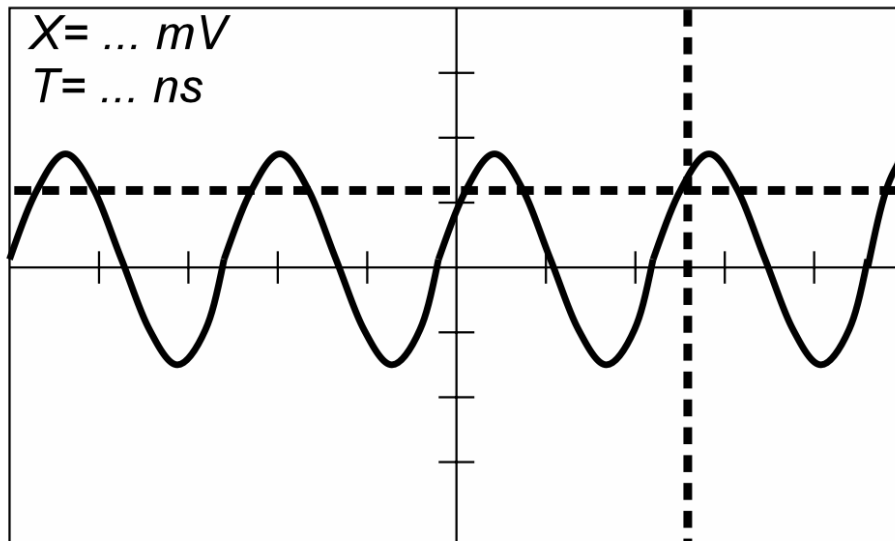




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Oscilloscope: visualization

- **Grid** (divisions)
- **Cursors**
- **Scale factors** (voltage per division, time per division)





Oscilloscope: Measurement accuracy

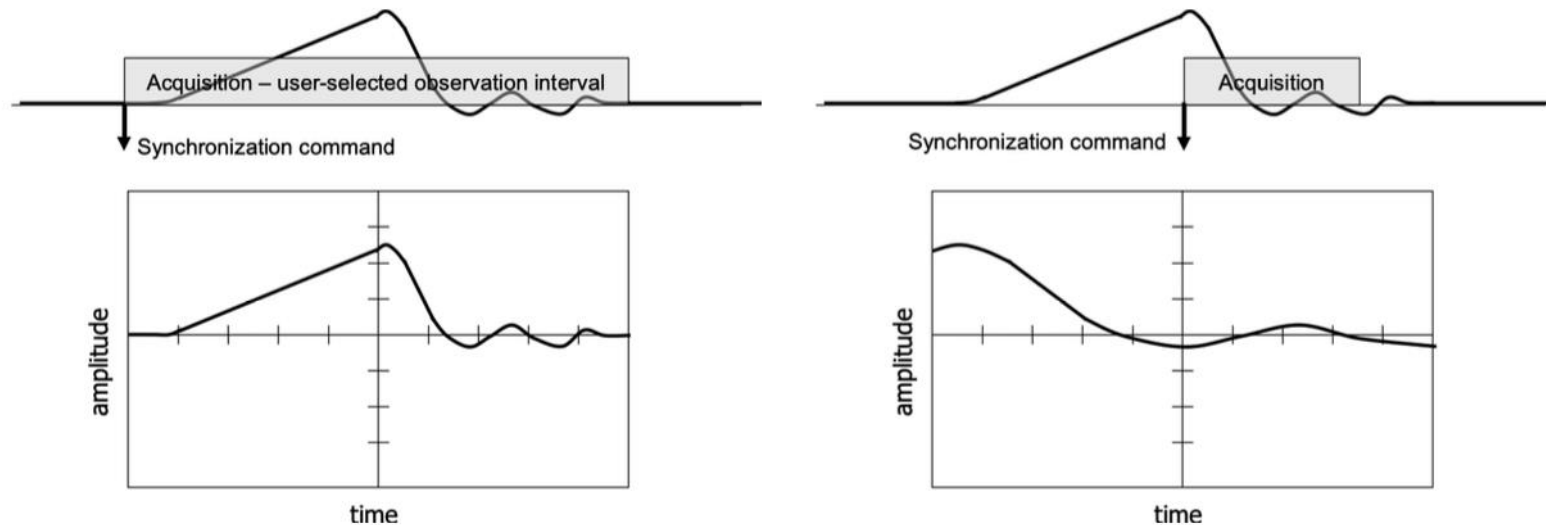
- **Amplitude uncertainty:**
 - **Lower bound** → **ADC resolution**
 - 2^b quantization levels for a b bit ADC
 - **Input range** → height of the oscilloscope grid
 - **Uncertainty: $1/2^b$ of the full scale value** → lower than 1%
 - **Noise and calibration uncertainty** → around 1%
- **Time base uncertainty:**
 - Reciprocal of the **instrument memory depth**: N samples → $1/N$ uncertainty
 - Further limited by graphical resolution → 600×1000 pixels, $1/1000$ resolution
 - **Clock uncertainty**



Oscilloscope: Operating cycle

- **Horizontal scale factor** → set observation interval length
- **Vertical scale factor** → set the amplitude scale
- **Trigger** → Synchronize signal acquisition

Non repetitive signal → acquisition is triggered by a synchronization command

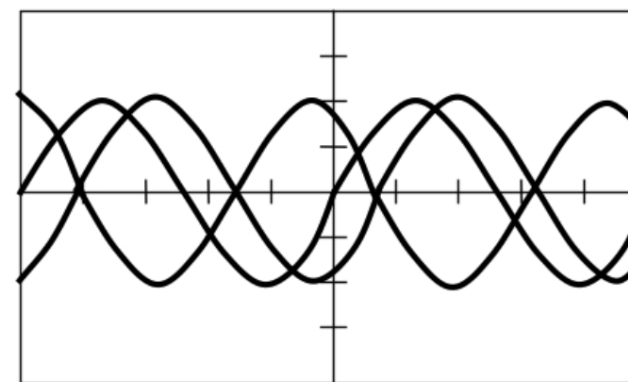
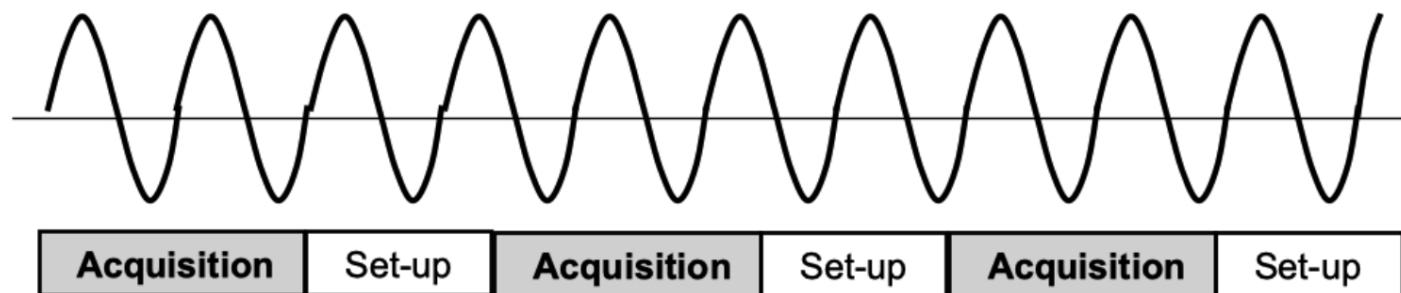




Oscilloscope: Operating cycle

Periodic signal \rightarrow trace constantly updated

- Acquisition phase t_A
- Setup-up phase t_B
 - Minimum interval = $t_A + t_B$

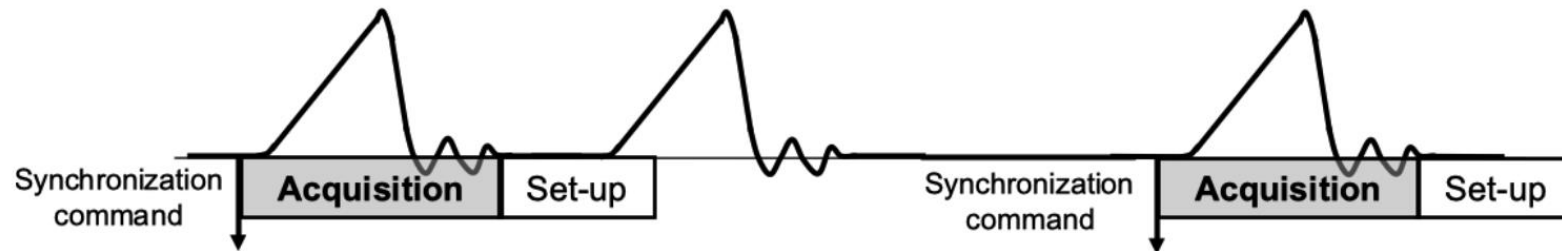




Oscilloscope: Operating cycle

Periodic signal → trace constantly updated

- Acquisition phase t_A
- Setup-up phase t_B
 - Minimum interval = $t_A + t_B$
- Wait phase t_c

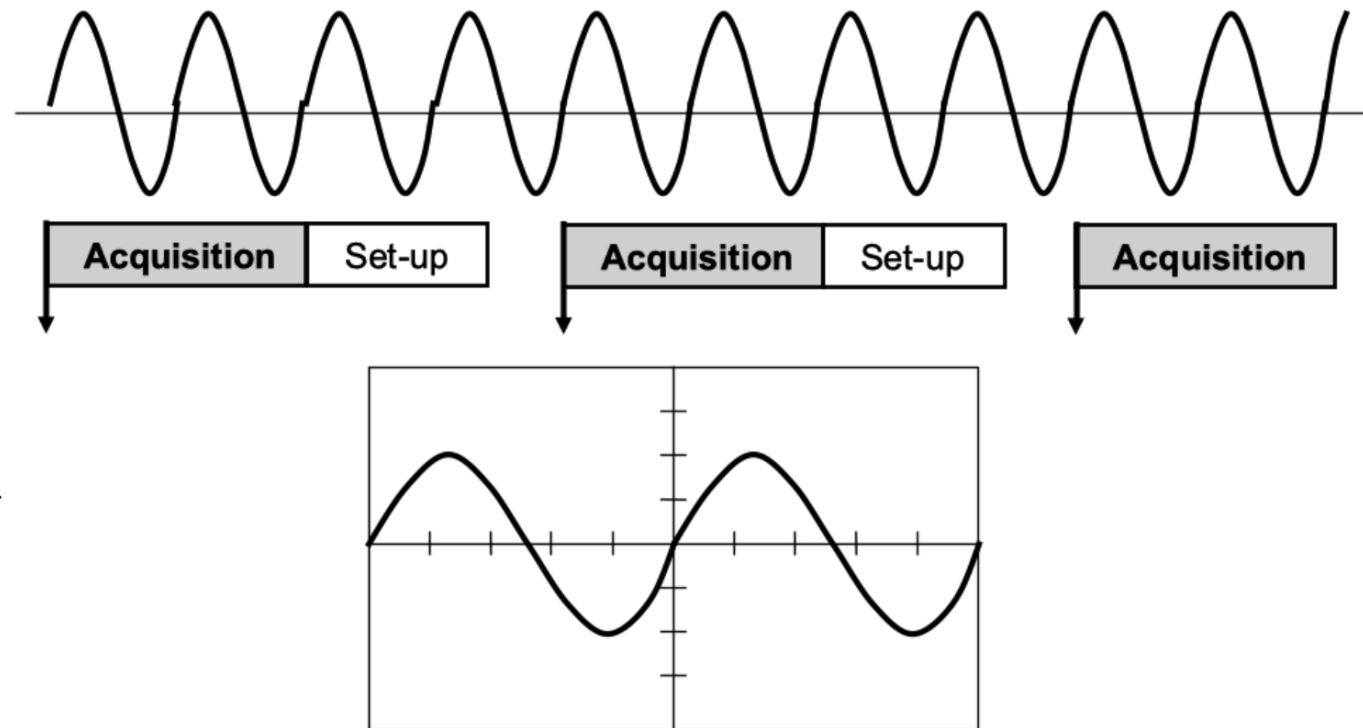




Oscilloscope: Operating cycle

Periodic signal \rightarrow trace constantly updated

- Acquisition phase t_A
- Setup-up phase t_B
 - Minimum cycle length = $t_A + t_B$
- Wait phase t_c
 - Total cycle length = $t_A + t_B + t_c$
- Signal period T
 - $t_A + t_B + t_c = MT$ with $M \in \mathbb{Z}$

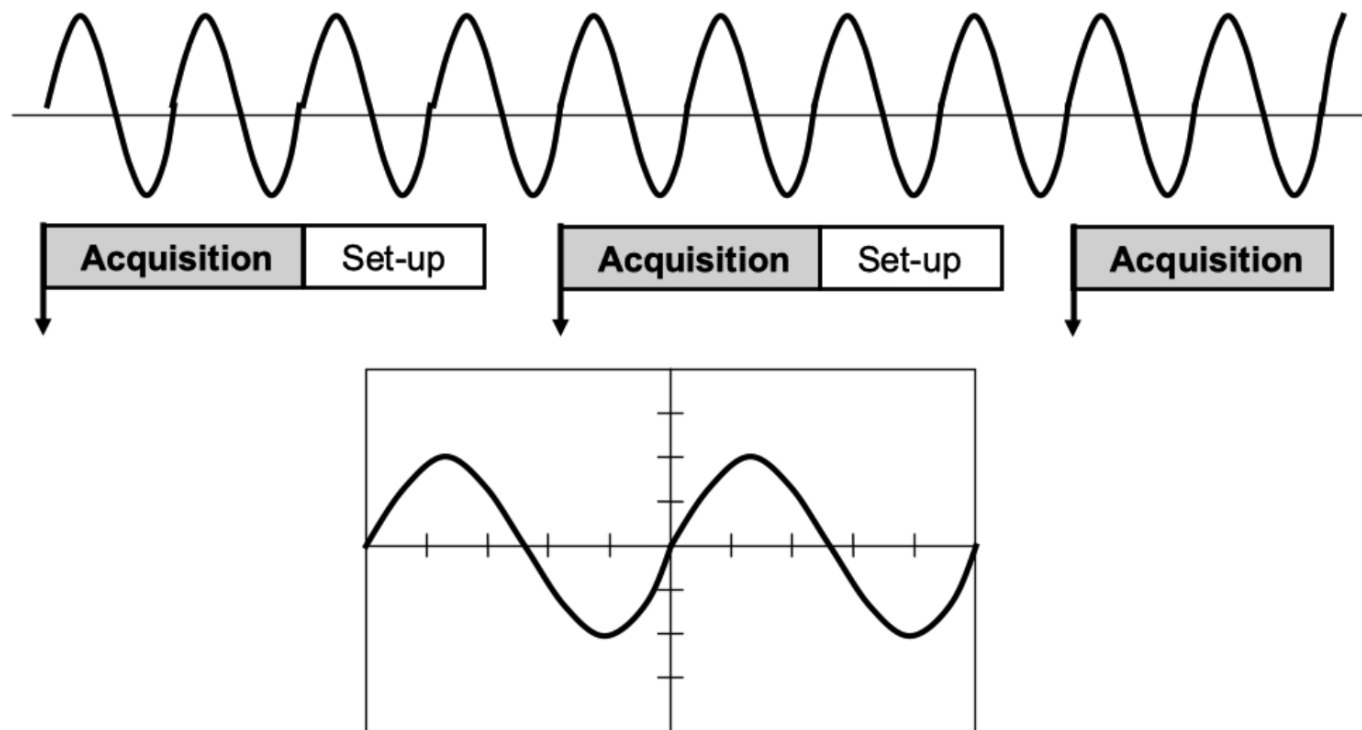




Oscilloscope: Operating cycle

Periodic signal → trace constantly updated

- **Signal period T**
 - $t_A + t_B + t_C = MT$ with $M \in \mathbb{Z}$
- **Trace update rate**
 - $1 / t_A + t_B + t_C$
- **Acquisition efficiency**
 - $0 < t_A / t_A + t_B + t_C < 1$





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Signal generator





Signal generator

- **Test inputs for measurements**
- **Different waveforms** according to the specific test
- **Analog signals** → different waveforms (multi-sine combinations)
- **Digital signals** → transitions between two levels
- **Linear systems** → **Sinewaves**
 - Same frequency as the input
 - Different amplitude and phase



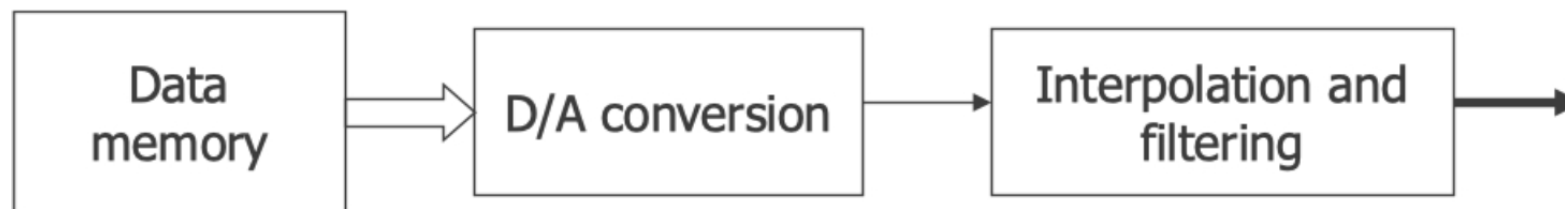
Signal generator

- **Sinewave generator**
 - Adjustable amplitude and frequency
 - Low harmonic content
 - Stable output frequency
 - Stable output amplitude
 - Limited number of low level spurious components
- **Specialized laboratory equipment**



Signal generator

- **Waveform generator**
 - **Different generable signals:** sinusoidal, triangular, square and ramp waveforms
- More flexibility, less accuracy...
- **Sampling Shannon theorem** → continuous-time reconstruction (band limited signal)
- **Digital Samples** → **Analog samples** → **Interpolation - Low-pass filtering**





Signal generator

- **Arbitrary Waveform Generator (AWG)**
 - Signal stability
 - Good frequency and amplitude resolution
 - Low harmonic distortion
 - Easy generation of complex waveforms
- **Digital memory** for the writing of samples related to arbitrary waveforms
- **Common waveforms stored permanently** → faster standard operations (changing amplitude and frequency)





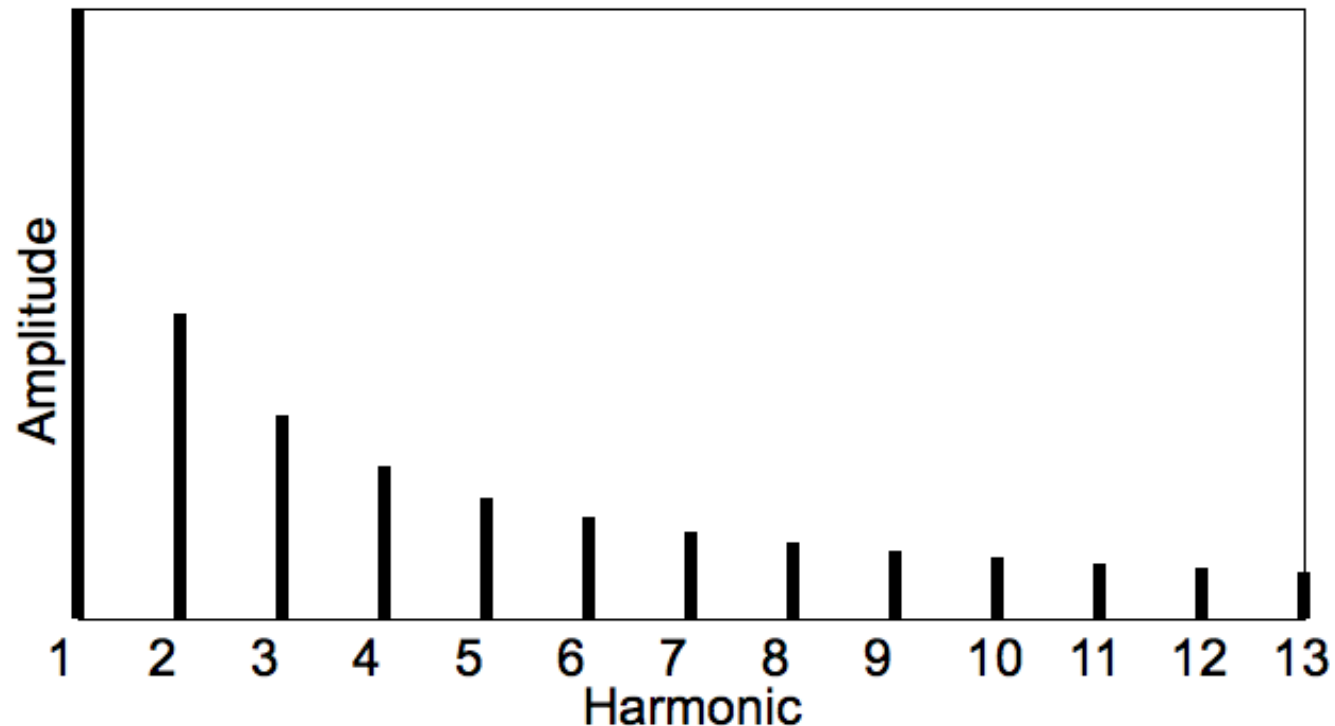
- **Arbitrary Waveform Generator (AWG)**
 - Voltage source
 - 50 Ω output impedance \rightarrow adaptation to the characteristic impedance of coaxial cables
 - Actual voltage indication only in case of maximum power transfer ($R_G = R_L$)
- Connection of an AWG to the oscilloscope \rightarrow **High impedance load**



Test waveforms

Sinewave

- Spectrum composed of a single spectral line (with its frequency image)
- Possible harmonic components





Test waveforms

Sinewave

- **Spectrum composed of a single spectral line** (with its frequency image)
- Possible harmonic components
- **Total Harmonic Distortion (THD)**: typical values < -70 dB

$$\frac{\sqrt{V_{RMS_2}^2 + V_{RMS_3}^2 + \dots}}{V_{RMS_1}}$$

- **Signal to Noise and Distortion (SINAD)**: typical values > 70 dB

$$\frac{V_{RMS_1}}{\sqrt{V_{RMS_2}^2 + V_{RMS_3}^2 + \dots + N}}$$

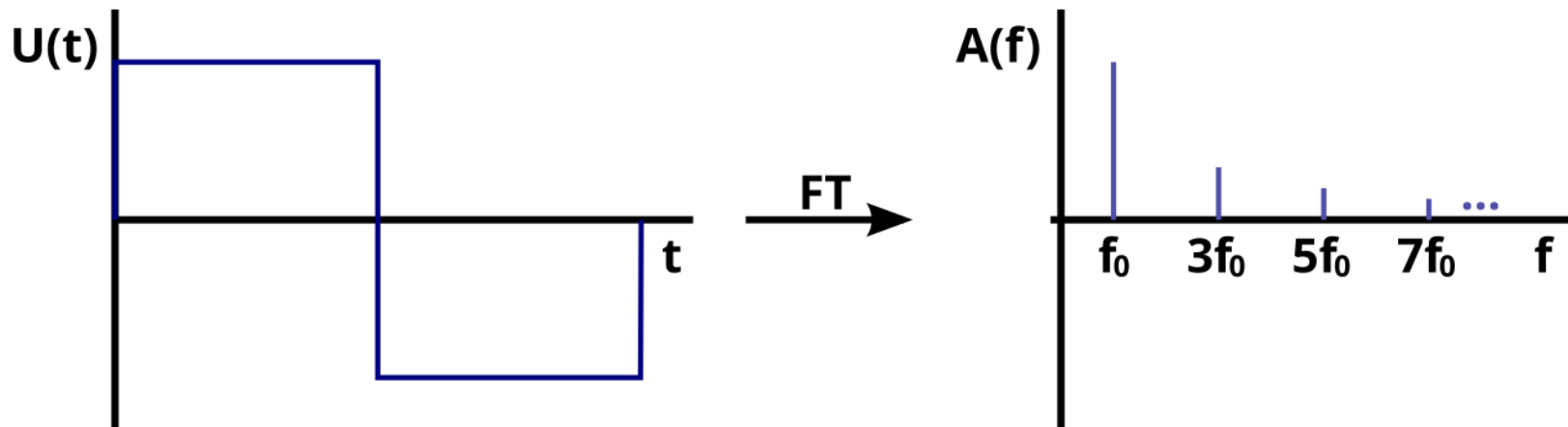


Test waveforms

Square Wave

- Spectral lines at the **fundamental frequency and its integer multiples** (harmonics)
- Fundamental frequency and harmonic components at **odd multiples**

$$\left| \frac{A_k}{A_1} \right| = \begin{cases} \frac{1}{k} & \text{for } k \text{ odd} \\ 0 & \text{for } k \text{ even} \end{cases}$$





Test waveforms

Square Wave

- Spectral lines at the **fundamental frequency and its integer multiples** (harmonics)
- Fundamental frequency and harmonic components at **odd multiples**

$$\left| \frac{A_k}{A_1} \right| = \begin{cases} \frac{1}{k} & \text{for } k \text{ odd} \\ 0 & \text{for } k \text{ even} \end{cases}$$

- Asymmetries in the lengths of level \rightarrow duty cycle D not 50%

$$\left| \frac{A_k}{A_1} \right| = \frac{1}{k} \frac{\sin \pi k D}{\sin \pi D}$$

- In general $D \cong 0.5 \rightarrow D = \frac{1}{2} (1 + 2\delta)$

$$\left| \frac{A_k}{A_1} \right| = \begin{cases} \frac{1}{k} & \text{for } k \text{ odd} \\ \pi \delta & \text{for } k \text{ even} \end{cases}$$



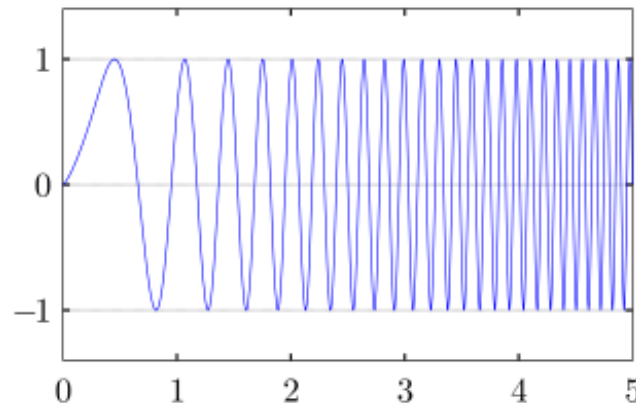
Test waveforms

Frequency sweep or chirp

- Sinewave whose frequency varies linearly with time in a certain interval

$$f(t) = f_1 + \frac{f_2 - f_1}{T_{\text{sweep}}} t \quad \text{with } 0 \leq t \leq T_{\text{sweep}}$$

- Spectrum with constant amplitude for $f_1 \leq f \leq f_2$
- Measuring the **system response** $\mathbf{G(f)}$ for a certain frequency interval. $|Y(f)|$ proportional to $|G(f)|$





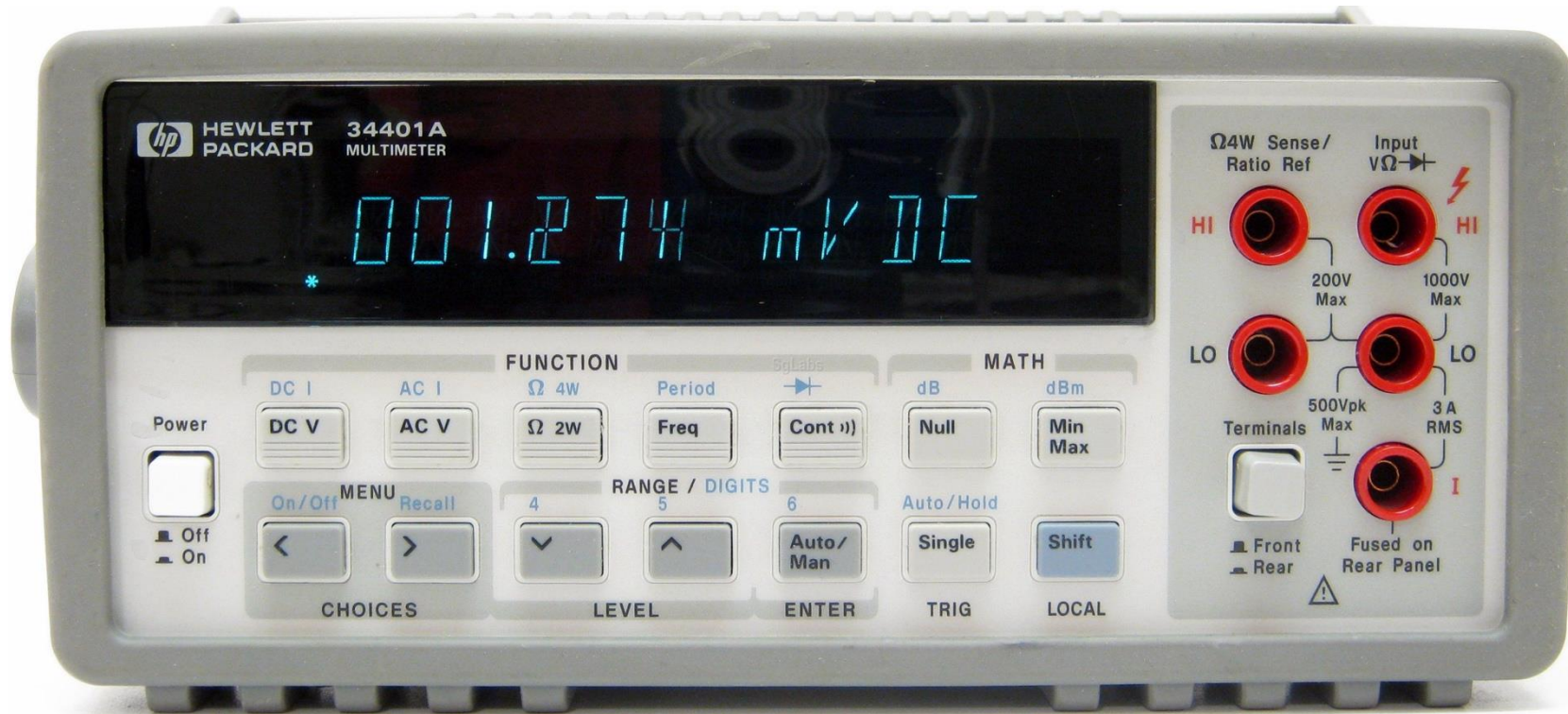
Synchronization output

- **Two levels signal:** the rising edge of a steep transition coincides with the start of a signal period
- Zero mean sinewave → Zero crossing
- Maximum possible slope
- **‘Sync’ output → Oscilloscope ‘external trigger’**



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Digital multimeter (DMM)





- **Measurements of:**
 - DC and AC voltage
 - DC and AC current
 - Resistance
- High resolution ADC (up to 24 bits or higher)
- **3 or 5 inputs**
 - Positive voltage
 - Negative voltage
 - Current
 - Ω -sense terminal
- Different measurement ranges



DMM resolution

- **Resolution:** *smallest change in a quantity being measured that causes a perceptible change in the corresponding indication*
- ± 1 variation in the least significant digit
- Same quantity of the measured quantity \rightarrow same measurement unit
- **Relative resolution**

$$\frac{\Delta_X}{X_M}$$
$$\frac{\Delta_X}{X_{FS}}$$



DMM number of digits

- **Resolution \rightarrow Number of digits \rightarrow Uncertainty**
- D decimal digits $\rightarrow 10^D - 1$ maximum displayed value $\rightarrow \frac{1}{10^D}$ resolution relative to full scale
- 4-digit DMM $\rightarrow 10^{-4}$ resolution relative to full scale value
- Typical full scale values: (0.3, 3, 30, 300), (0.2, 2, 20, 200)
- Still D digits, but the the most significant is not employed to display the maximum value
- $(D - 1) + \frac{1}{2}$ DMMs (e.g., $3^{1/2}$, $5^{1/2}$, $6^{1/2}$, $8^{1/2}$)



DC voltage measurements

- **Wide range of values** → attenuators/amplifiers
- **Autorange**
- **Input resistance** $R_{in} = 10\text{ M}\Omega$
- **Differential** input configuration with floating ground
- **Offset errors** → offset compensation
- **Autozero** (Active by default)

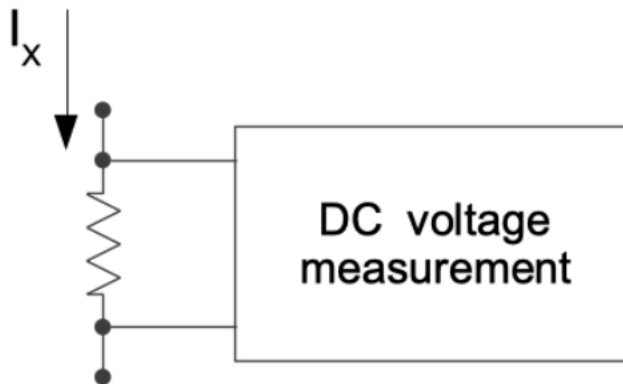


DC current measurements

- Current shunt

$$I_M = \frac{V_M}{R_{shunt}}$$

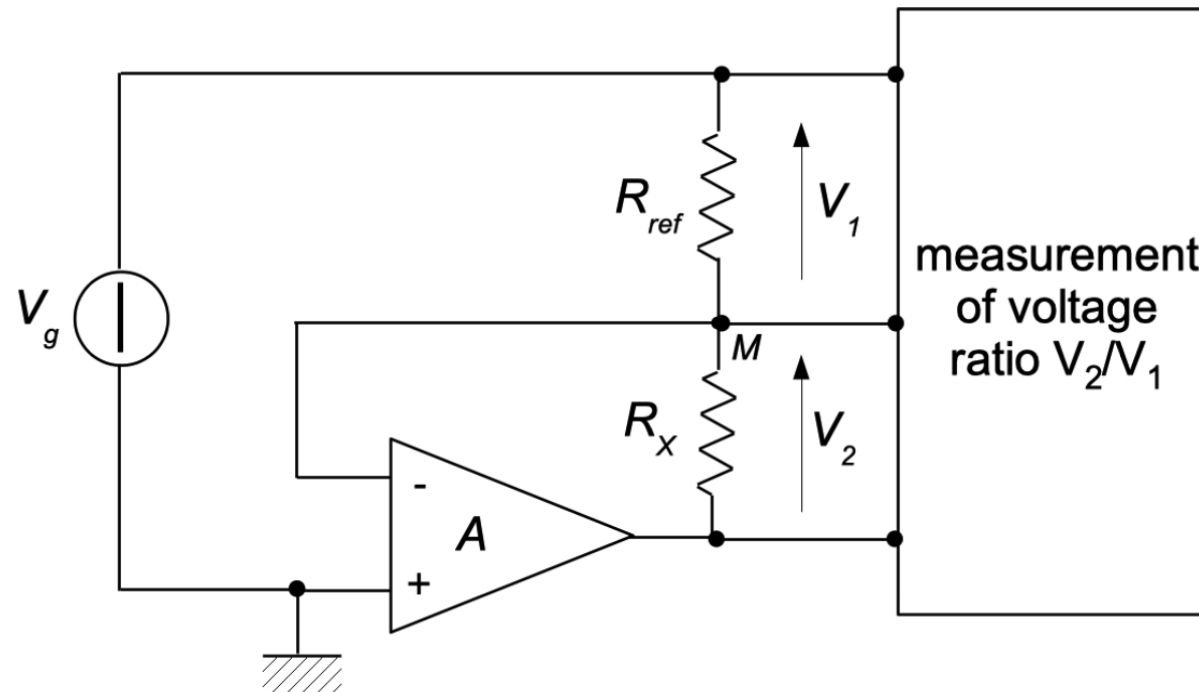
- Interruption of a circuit line
- Shunt resistance **as low and as constant as possible**





Resistance measurements

- Test current injection

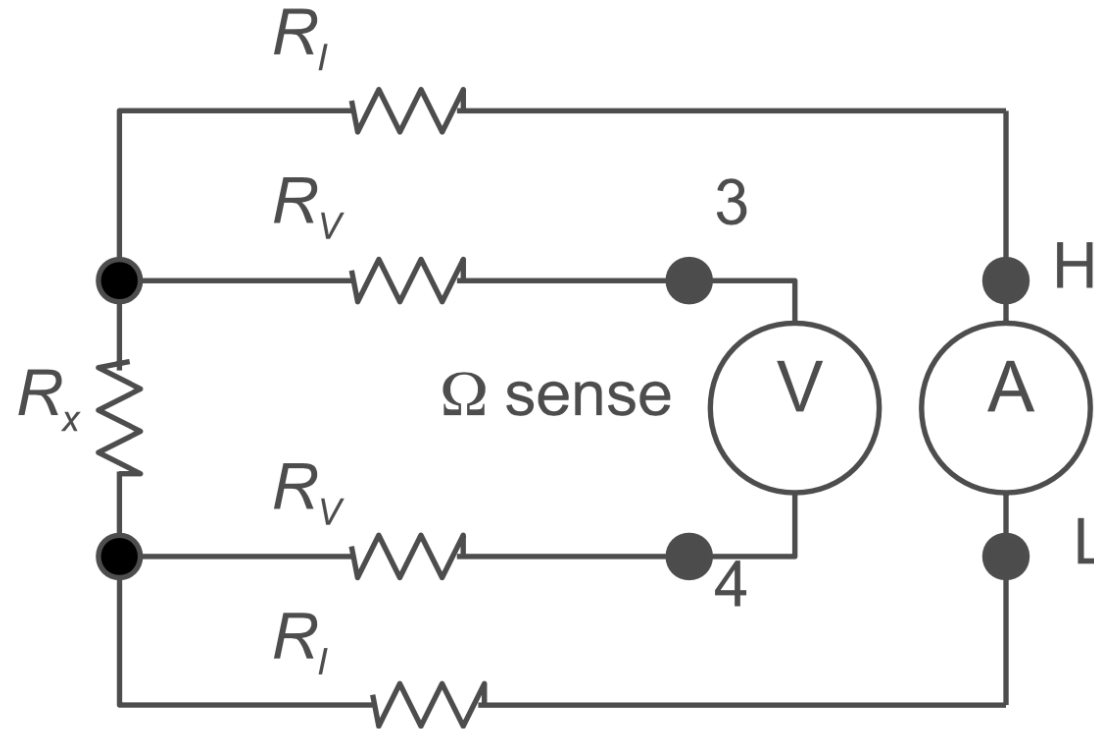


$$R_X = \frac{V_1}{V_2} R_{ref}$$



4-wire resistance measurements

- Avoiding the effects of **contact and conductor resistances** (some tens of mΩ)

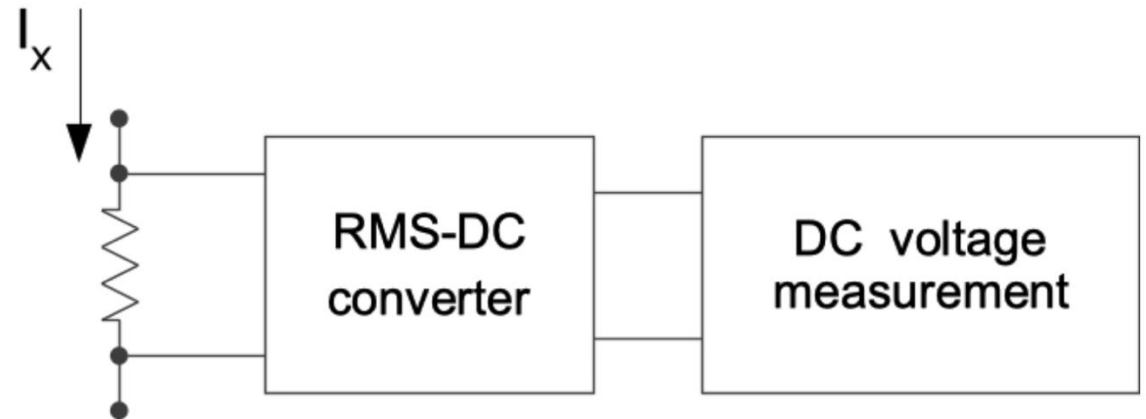


$$R_X = \frac{V_{34}}{I_{HL}} \text{ with } I_{34} = 0$$





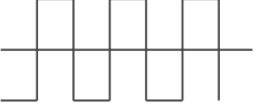
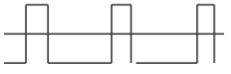
AC measurements

- AC voltage and current **Root Mean Square (RMS)** value
- Value of a corresponding DC voltage or current that produces the same **active power** on a resistor
- AC-coupled multimeter
- Other parameters:
 - Peak value X_{PK}
 - Conventional mean value X_M
 - Form Factor (FF) $\rightarrow X_{RMS}/X_M$
 - Crest Factor (CF) $\rightarrow X_{PK}/X_{RMS}$





AC measurements

$x(t)$				D = duty cycle 
X_{RMS}	$\frac{A_0}{\sqrt{2}}$	$\frac{A_0}{\sqrt{3}}$	A_0	$2A_0\sqrt{D(1-D)}$
X_m	$\frac{2A_0}{\pi}$	$\frac{A_0}{2}$	A_0	$4A_0[D(1-D)]$
X_{pk}	A_0	A_0	A_0	$2A_0\left(\frac{1}{2} + D - \frac{1}{2} \right)$
FF	$\frac{\pi}{2\sqrt{2}} \simeq 1.11$	$\frac{2}{\sqrt{3}} \simeq 1.15$	1	$\frac{1}{2\sqrt{D(1-D)}}$
CF	$\sqrt{2}$	$\sqrt{3}$	1	$\frac{\frac{1}{2} + D - \frac{1}{2} }{\sqrt{D(1-D)}}$



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