



Università degli Studi di Padova

Conceptual Design and the Entity-Relationship Model

Basi di Dati

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Constraints in the entity-relationship model

Documentation



- The Entity-Relationship (ER) model provides several constructs that impact on both the intensional level (schema) and the extensional level (instance)
 - Entity
 - Attribute of entity
 - Relationship
 - Role
 - Attribute of relationship
 - Generalization [not covered in the lectures]
 - Identification constraints
 - Cardinality constraints
 - Other constraints

The ER model allows us to express the conceptual schema representing the mini-world in graphical form







Entity

Each entity has a **name** which **univocally identify** it in the schema

In the ER diagram, an entity is represented by a rectangle which contains the name of the entity

We use the **classification abstraction** to create entities



At extensional level an entity consist of a set of objects called instances (or occurrences) of the entity

Therefore, if in a schema S an entity e is defined, in each instance i of the schema
 S, the entity e is associated with a set of objects, also called the extension of e in the instance i of S

instance:
$$I \times S \rightarrow I$$

(i,e) \mapsto instance(i,e) = { e_1, e_2, \dots, e_n }

An instance e_i of an entity is not a value that identifies an object but it is the object itself

In the conceptual schema we represent only the entities and not their instances

Entity: Example of Extensional Semantics



Relationship





A relationship represents an association among two or more entities. The number of entities participating in a relationship is called the degree of the relationship.



Each relationship has a name which univocally identify it in the schema

In the ER diagram, a relationship is represented by a rhombus which contains the name of the relationship

We use the **association abstraction** to create relationships





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Each relationship has a name which univocally identify it in the schema

In the ER diagram, a relationship is represented by a rhombus which contains the name of the relationship

We use the **association abstraction** to create relationships



At **extensional** level a binary relationship **r** between entities **e** and **f** consists of the pairs $r_k = (e_i, f_j)$ such that e_i is an instance of **e** and f_j is an instance of **f**. Each pair is an instance (or occurrence) of the relationship **r**

Therefore, if in a schema S a relationship r is defined between the entities e and f, in each instance i of the schema S, the relationship r is associated with a set of pairs, also called the extension of r in the instance i of S

```
instance: I \times S \rightarrow I \times I
(i, r) \mapsto instance(i, r) \subseteq instance(i, e) \times instance(i, f)
= \{(e_1, f_1), (e_2, f_2) \dots, (e_n, f_n)\}
```

In the conceptual schema we represent only the relationships and not their instances











(Binary) Relationships: Beware!







(Binary) Relationships: Beware!





(Binary) Relationships: Beware!





N-ary Relationship



A relationship with degree higher than 2 is called **n-ary**

Order is a ternary relationship among Supplier, Product, and Department



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Recursive Relationship





Recursive Relationship



• We specify the **role** played by an entity when it participates more than once to a relationship



At **extensional** level an n-ary relationship **r** among entities **e**₁, **e**₂, ..., **e**_n (not necessarily distinct) with roles **u**₁, **u**₂, ..., **u**_n (all distinct), respectively, consists of a set of labeled n-uples

$$r_k = (U_1 : e_{1,i}, U_2 : e_{2,j}, \dots, U_n : e_{n,h})$$

such that $e_{1,i}$ is an instance of e_1 , $e_{2,j}$ is an instance of e_2 , and $e_{n,h}$ is an instance of e_n . Each n-uple is an instance of the relationship **r**

The role of an entity must be explicitly specified in the ER diagram when it participates more than once in a relationship. When it is not explicitly specified, i.e. when the entity participates only once to the relationship, we implicitly assume that the role coincides with the name of the entity

Attribute





An attribute of an entity is a local property of that entity, relevant for the application. An attribute maps each instance of an entity to a value belonging to a set called domain



Each attribute has a **name** which **univocally identify** it in the entity

In the ER diagram, an attribute is represented by a circle with the name of the attribute, connected to the entity the attribute belongs to

the domain of the attribute is typically omitted in the ER diagram but it is reported in the data dictionary (see later on)

We use the **aggregation abstraction** to create attributes

Entity Attribute: Extensional Semantics

At extensional level an attribute is a (total) function which maps each instance of the entity e to a value belonging to a domain D.

Therefore, if in a schema S an entity e and an attribute a of e on a domain D are defined, in each instance i of the schema S, for each instance e_i of the entity e, there exists a unique value v_j in the domain D associated to e_i

instance: $I \times S \rightarrow I \times D$ (i,a) \mapsto instance(i,a) \subseteq instance(i,e) $\times D$ $= \{(e_1, v_1), (e_2, v_2) \dots, (e_n, v_n)\}$

 $\forall e_i \in instance(i, e), \exists ! v_j \in D | (e_i, v_j) \in instance(i, a)$

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a: instance(i, e) $\rightarrow D$ $e_i \mapsto v_j$

Attribute: Example of Extensional Semantics























- It may happen that, for a given attribute, you cannot associate a value with an instance of an entity
 - but the definition of attribute requires to have a value associated with each instance of an entity
- To address this issue we define a special value, called NULL

NULL is not one of the "ordinary" values of a domain **D**

- "unused values" may not exist
- "unused values" may change over time
- you need to treat such "unused values" as special cases in the applications
 - "unused values" would be different from domain to domain



Value undefined: an appropriate value for a given instance does not exist

- Master Degree does not apply to those people who have not attended university
- Value not available: an appropriate value for a given instance exists but it is not known in a given moment
 - You may not know the Age of a Person
- **Value unknown**: an appropriate value for a given instance may or may not exist
 - A Person may or may not have an home phone number



• Attributes can be defined also over composite domains




An attribute of a relationship is a local property of that relation, relevant for the application. An attribute maps each instance of a relationship to a value belonging to a set called domain



Each attribute has a **name** which **univocally identify** it in the relationship

In the ER diagram, an attribute is represented by a circle with the name of the attribute, connected to the relationship the attribute belongs to

An attribute of a relationship r among entities e₁, e₂, ..., e_n models a property not of e₁, not of e₂, ..., not of e_n but of the association among e₁, e₂, ..., e_n as represented by r



- At extensional level an attribute is a (total) function which maps each instance of the relationship r to a value belonging to a domain D.
- Therefore, if in a schema **S** a relationship **r** and an attribute **a** of **r** on a domain **D** are defined, in each instance **i** of the schema **S**, for each instance $r_k = (e_{1,i}, e_{2,j}, \ldots, e_{n,h})$ of the relationship **r**, there exists a unique value v_j in the domain **D** associated with r_k

instance:
$$| \times S \rightarrow | \times D$$

(i,a) \mapsto instance(i,a) \subseteq instance(i,r) $\times D$
 $= \{(r_1, v_1), (r_2, v_2) \dots, (r_n, v_n)\}$

 $\forall r_i \in instance(i, r), \exists ! v_j \in D|(r_i, v_j) \in instance(i, a)$



- At extensional level an attribute is a (total) function which maps each instance of the relationship **r** to a value belonging to a domain **D**.
- Therefore, if in a schema **S** a relationship **r** and an attribute **a** of **r** on a domain **D** are defined, in each instance **i** of the schema **S**, for each instance $r_k = (e_{1,i}, e_{2,j}, \ldots, e_{n,h})$ of the relationship **r**, there exists a unique value v_j in the domain **D** associated with r_k

a: instance(i, r)
$$\rightarrow D$$

 $r_i \mapsto v_j$









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Attribute of N-ary Relationship: Example of Extensional Semantics



Integrity Constraints



An integrity constraint is a rule expressed on the schema (intensional level) that specifies a condition which must be met for each instance (extensional level) of the schema

Cardinality constraints on relationships

- Cardinality constraints on attributes
- Identification constraints on entities
- Other constraints (external)



A cardinality constraint refers to a role *u* of an entity *e* in a relationship *r* and it expresses a lower bound and an upper bound to the number of instances of the relationship *r* to which each instance of the entity *e* can take part with the role *u*





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Relevant cardinalities are: 0, 1, N

Minimum cardinality:

- 0 means "optional participation"
- 1 means "mandatory participation"

Maximum cardinality:

- 1 means: "the entity can participate at maximum once to the relationship"
- **N** mean: "the entity can participate many times to the relationship"



Binary relationships can be classified according to their cardinality constraints

- One-to-One relationship: each instance of an entity is associated with one and only one instance of another entity
- One-to-Many relationship: each instance of an entity is associated with one or more instances of another entity
- Many-to-Many relationship: one or more instances of an entity are associated with one or more instances of another entity





Example of One-to-Many Relationships



Example of Many-to-Many Relationships







By definition, an instance of the **Teach** relationship is a triple

 $t_k = (s_i, c_j, t_h) \in instance(i, Speaker) \times instance(i, Course) \times instance(i, Topic)$

Even if the participation of the Topic entity is optional, it cannot exist an instance of the Teach relationship without an instance of the Topic entity

$$t_k = (s_i, c_j, \bullet)$$

In other terms, you cannot use Teach to express the fact that a Speaker will give a Course but the Topics are not fixed yet





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 t_k

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$$k_0 \to k_1 \to k_2 \to k_3 \to \ldots \to k_{n-1} \to k_n$$









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A cardinality constraint on an attribute of an entity (relationship) expresses a lower bound and upper bound to the number of values associated with each instance of the entity (relationship).





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Relevant cardinalities are: 0, 1, N

Minimum cardinality:

0 means the attribute is optional

Maximum cardinality:

N means the attribute is **multi-valued**

If the constraint is not explicitly specified, the cardinality of the attribute is (1, 1), i.e. it is mandatory


Simple attributes

$\mathsf{D} \subseteq \mathsf{A}$

where A is a domain of "atomic" values

Multi-valued attributes

$$\mathsf{D} \subseteq \mathcal{P}(\mathsf{D}')$$

where D' is a domain of simple attributes and $\mathcal{P}(\bullet)$ is the power set

Optional attributes

 $\mathsf{D} \subseteq \mathcal{P}(\mathsf{D}')$ $\mathsf{NULL} \mapsto \varnothing$

where **D'** and $\mathcal{P}(\bullet)$ are as above



An identification constraint for an entity *e* defines an identifier for the entity, that is a set of properties (attributes or relationships) which allow us to uniquely identify all the instances of an entity.

There does not exist two different instances of the entity which have the same value on all the properties which constitute the identifier

 Any number of identification constraints can be defined on an entity but at least one





An identifier of an entity e can be

- Internal, i.e. constituted by only attributes of e with cardinality (1, 1)
- External, i.e. constituted by attributes of e AND by roles in relationships where e participates OR just by roles in relationships where e participates, provided that all the involved attributes and roles have cardinality (1,1)
- Notation for internal identifiers:
 - In case of identifier constituted by a single attribute, its circle is filled in
 - In case of identifier constituted by more attributes, a line with a black circle connects all the involved attributes

Notation for external identifiers:

A line with a black circle connects all the involved attributes and/or roles

Example of Internal Identifier (1/2)



instance(i, Car) = $\{c_1, c_2, c_3\}$ instance(i, Car.Plate) = $\{(c_1, CZ \ 421 \ LK), (c_2, MK \ 9651 \ AB), (c_3, BG \ 529 \ BV)\}$ instance(i, Car.Model) = $\{(c_1, Alfa \ MiTo), (c_2, Audi \ A3), (c_3, Citroen \ C3)\}$ instance(i, Car.Color) = $\{(c_1, Red), (c_2, Red), (c_3, White)\}$

Example of Internal Identifier (2/2)



 $instance(i, Person) = \{p_1, p_2, p_3\}$ $instance(i, Person.FirstName) = \{(p_1, Mario), (p_2, Giovanni), (p_3, Mario)\}$ $instance(i, Person.LastName) = \{(p_1, Rossi), (p_2, Bianchi), (p_3, Rossi)\}$ $instance(i, Person.BirthDate) = \{(p_1, 23-05-1975), (p_2, 12-01-1967), (a_3, 15-04-1984)\}$ $instance(i, Person.Income) = \{(p_1, 18.000), (p_2, 20.000), (p_3, 20.000)\}$



Example of External Identifier



 $\begin{aligned} &\text{instance}(i, \text{Student}) = \{s_1, s_2, s_3\} \\ &\text{instance}(i, \text{University}) = \{u_1, u_2\} \\ &\text{instance}(i, \text{Student.FirstName}) = \{(s_1, \text{Mario}), (s_2, \text{Giovanni}), (s_3, \text{Mario})\} \\ &\text{instance}(i, \text{Student.LastName}) = \{(s_1, \text{Rossi}), (s_2, \text{Bianchi}), (s_3, \text{Rossi})\} \\ &\text{instance}(i, \text{Student.BadgeNumber}) = \{(s_1, 419366), (p_2, 512344), (s_3, 419366)\} \\ &\text{instance}(i, \text{University.Name}) = \{(u_1, \text{Università degli Studi di Padova}), (u_2, \text{Politecnico di Milano})\} \\ &\text{instance}(i, \text{University.City}) = \{(u_1, \text{Padova}), (u_2, \text{Milano})\} \\ &\text{instance}(i, \text{Enroll}) = \{(s_1, u_1), (s_2, u_1), (s_3, u_2)\} \\ &\text{instance}(i, \text{Enroll.Date}) = \{((s_1, u_1), 21-09-2010), ((s_2, u_1), 19-09-2011), ((s_3, u_2), 19-09-2011)\} \end{aligned}$





Weak Entity: entity types that do not have key attributes of their own

Weak entities are identified by being related to specific entities from another entity type in combination with one of their attributes values (externally identified)

Weak entities always have a total participation constraint with respect to their identifying relationship

Not every existence dependency results in a weak entity





Number





The ER schema allows us to grasp all the main types of relations and constraints among the data in the mini-world and provides us graphical means to express them

However not all the constraints fall into the set of the pre-defined ones

The documentation of an ER schema also contains all the additional constraints, called external (to the ER diagram) constraints, expressed as

mathematical notation

natural language assertion, as un-ambiguous as possible

Documentation





In addition to the ER diagram, the conceptual schema is documented by the so-called data dictionary

The data dictionary consists of a set of tables describing:



Relationships

Attributes

External Constraints



Entity	Description	Attributes	Identifiers
Name	Description	Attribute names, domain, description	Attribute names



Relationship	Description	Component Entities	Attributes
Name	Description	Entity Names	Attribute names, domain, description

Generalization and Specialization



The IS-A relation (subset relation) is defined between two entities, called superclass and subclass, and it means that each instance of the subclass is also an instance of the superclass.





At extensional level, the **IS-A** relation requires that, in each instance **i** of a schema **S** such that

e₁ IS-A e₂

the following constraint is complied with

 $\mathrm{instance}(i,e_1)\subseteq\mathrm{instance}(i,e_2)$

From the definition, it follows that the IS-A relation is reflexive and transitive (but not symmetric)















Each property of the superclass is also a property of the subclass and it is not represented (twice) in the ER diagram. The subclass may have additional properties.

By "property" we mean

Attributes

Relationships

Integrity constraints





Each instance of Person has an Age
Each instance of Student is an instance of Person

therefore

Each instance of **Student** has an **Age**



Example of Attribute Inheritance





Example of Attribute Inheritance





Example of Attribute Inheritance





Each instance of **Person** can take part to any number of instances of **Play**

Each instance of Student is an instance of Person

therefore

Each instance of **Student** can take part to any number of instances of **Play**



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Inheritance of IS-A Relation: Transitivity



The IS-A relation is inherited too. This means that the IS-A relation is transitive (in addition to being reflexive)

Each instance of Student is an instance of Person

Each instance of Erasmus is an instance of Student

therefore

Each instance of Erasmus is an instance of Person



The generalisation consists of a super class extended by several subclasses, that is we have several IS-A relations, according to a single criterion.



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If in a schema **S** a generalisation between superclass **p** and subclasses **f**₁, **f**₂, ..., **f**_n is defined, then in each instance **i** of the schema **S** it must hold:

$\begin{aligned} & \text{instance}(i, f_1) \subseteq \text{instance}(i, p) \\ & \text{instance}(i, f_2) \subseteq \text{instance}(i, p) \end{aligned}$

$instance(i, f_n) \subseteq instance(i, p)$



The inheritance principle holds also in the case of generalisations

- each property (attributes, relationships, integrity constraints) of the superclass is also a property of all the subclasses and it is not drawn in the ER diagram.
 Subclasses may have additional properties.
- Two constraints may hold for generalisations
 - **completeness**: each instance of the superclass must be an instance of at least one subclass

$instance(i, f_1) \cup istanze(i, f_2) \cup \ldots \cup instance(i, f_n) = instance(i, p)$

disjointness: each instance of the superclass can be a member of at most one of the subclasses

instance(i,
$$f_i$$
) \cap instance(i, f_j) = \emptyset , $1 \le i, j \le n, i \ne j$

Completness and Disjointness

Complete and disjoint generalisation, a.k.a. partition



Not complete but disjoint generalisation






Completness and Disjointness

Complete and not disjoint generalisation





Not complete and not disjoint generalisation



Basi di Dati, A.Y. 2024/2025 BD in "Computer Engineering" Different Generalisations on the Same Entity



 The same entity can be a superclass in different generalisations created according to different criteria

 There is no link between two different generalisations because they correspond to different criteria



Generalisation and IS-A Relation







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