Methods and Models for Combinatorial Optimization

Lab exercise - Part II

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For the combinatorial optimization problem described in Part I, it is required to:

- design and implement an ad-hoc optimization algorithm, as an alternative to solving the implemented mathematical programming model. Any meta-heuristic can be developed, as well as any of the approaches presented for the Travelling Salesman Problem (e.g., a constraint generation or a cut-and-branch approach based on separating sub-tour elimination constraints). You can also keep inspiration from any method you can find in literature for related problems, if it is related to the content of the course: if you decide to start from some algorithm you find in literature, *please ask to the teacher before* starting the implementation;
- develop your own algorithm. It is allowed (in particular for non-computer scientists) to use of available optimization libraries like Matlab genetic algorithms, or Python libraries. Of course, you can find ready-to-use code for the TSP but, in this case, you should add some functionalities to the available code (e.g. some more initialization options, intensification/diversification phases, incremental evaluations, ad-hoc mutations etc.);
- test the performance of the implemented method, present the computational results and compare the results to the ones obtained with the implemented mathematical programming model in Part I (use the same instances generated for Part I). Typical questions to be addressed during the performance test are: what are the running times? what is the gap with respect to the optimal solution? It is better to use the proposed heuristic or the mathematical programming model? etc. Notice that you should have more than one instance per size, so that average results should be provided. Moreover, in case the implemented algorithm has randomized components, you should either have a large number of instances, or rerun several (e.g. 10) times the algorithm on the same instance and collect statistics (average times or performance, standard deviations, min, max etc.);
- recall, in the previous point, that any required calibration is a *predeployment* activity, that has to be performed among the test actions (just a rough tuning is required);
- write a final report (10-20 pages) where you describe how you implemented the mathemarical programming model (some implementation details, for example, about the maps used to access variables, or how you created variables and constraints), some design issue concerning the algorithm of Part II (**not** the general heuristic or branch-and-bound that one can find in the notes or in a book, **but** how the method was customized), the feature of any used libraries (where applicable), the overall parameter tuning activity, and the computational results (summarizing tables and some comments) of both Part I and Part II, and their comparison.