## **Superconductive Materials**

**Part 11** Basic Principle of SRF

#### Outline

#### In this lecture we will address these questions:

- Why is important the R&D on accelerating cavities?
- Superconductivity means no resistance. Why can't we reduce the losses to zero?
- Why is niobium the material choice which requires costly helium cooling?
- What are the fundamental and technical limitations of niobium SRF cavities?
- What are possible future materials and what are the challenges? *(next lesson)*



#### And now finally...

# ... **RF Superconductivity**



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## **Surface Resistance of Superconductors**

Superconducting currents are transported by Cooper pairs formed of two electrons

Flow without friction  $\rightarrow$  DC supercurrents are lossless

At **T** > **0 K** there is a small fraction of unpaired electrons  $n_n(T) \propto e^{-\Delta/k_B T}$ 

Cooper pairs have a finite inertia. Under RF fields a timevarying E-field is induced in the material. **Normal electrons see this field, move and dissipate** 







#### **Basic ingredients for RF superconductivity**

- Two fluid model (Gorter-Casimir)
- Maxwell electrodynamics
- London equations

#### Basic assumptions of two fluid model

- all free electrons of the superconductor are divided into two groups:
- superconducting electrons of density n<sub>s</sub>
- normal electrons of density n<sub>n</sub>
- The total density of the free electrons is  $n = n_s + n_n$
- As the temperature increases from 0 to  $T_{\rm c}$ , the density n<sub>s</sub> decreases from n to 0

 $n_s / n_n = 1 - \left(T/T_c\right)^4$ 

Close to 0 K:







## **Electrodynamics of normal conductors**

$$E = E_0 e^{i\omega t}$$

We can derive the **skin depth** starting from the fundamental equation of electrodynamics:

Linear and isotropic Maxwell's equations + Drude's model . Material's equation +  $\nabla \cdot \boldsymbol{E} = \frac{\rho}{\varepsilon_0}$  $\nabla \times \boldsymbol{E} = -\frac{\partial \boldsymbol{B}}{\partial t}$  $\boldsymbol{D} = \varepsilon_0 \varepsilon \boldsymbol{E}$  $I = \sigma E$  $\boldsymbol{B} = \mu_0 \mu \boldsymbol{H}$  $\nabla \cdot \boldsymbol{B} = 0$  $\nabla \times \boldsymbol{H} = \boldsymbol{J} + \frac{\partial \boldsymbol{D}}{\partial t}$ 



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## Skin depth





### Skin depth (2)

$$\nabla^2 H = i\sigma\mu_0\mu\omega H$$

#### Solution (semi-infinite slab):

$$H_{y} = H_{0}e^{-x/\delta}e^{-ix/\delta}$$
$$E_{z} = -\frac{(1+i)}{\sigma\delta}H_{y}$$

# $E_z(x,t)$ Н, (х У

#### AC fields penetrate a thickness $\delta$ (the skin depth) $\delta$ =



#### Surface impedence

$$Z = \frac{E_{\parallel}}{H_{\parallel}} = R_s + iX_s$$
Surface reactance
Surface resistance

#### For the semi-infinite plane conductor:

$$Z_{n} = \frac{|E_{z}|}{H_{y}} \xrightarrow{E_{z} = -\frac{(1+i)}{\sigma\delta}H_{y}} Z_{n} = \frac{1+i}{\sigma\delta}$$
$$R_{s} = X_{s} = \frac{1}{\sigma\delta} = \sqrt{\frac{\mu_{0}\mu\omega}{2\sigma}}$$



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### Anomalous skin effect

What happen at low T (and high frequency)?

 $R_s = \frac{1}{\sigma\delta}$ 

 $\sigma(1)$  increases  $\bullet$   $\delta$  decreases  $\bullet$ 

The skin depth (the distance over which fields vary) can become less than the mean free path of the electrons (the distance  $J(x) \neq \sigma E(x)$  they travel before being scattered)





## **Anomalous skin effect (2)**

**Non local relationship** introduced by Reuther and Sondheimer:

$$\boldsymbol{J} = \frac{3\sigma}{4\pi\ell} \int \frac{\boldsymbol{r}(\boldsymbol{r}\cdot\boldsymbol{E})e^{-r/\ell}}{r^4} d^3\boldsymbol{r}$$

Non-locality enters the problem when the response to a field can only be determined correctly by integrating over a volume of the size of  $\ell^3$  (3D case), where  $\ell$  is comparable to or longer than the distance  $\delta$ , the depth over which the **E**-field varies



#### Surface resistance - some numbers

#### For Cu @ 300 K and 1.5 GHz:

 $\sigma$  (300 K) = 5.8 x 10<sup>7</sup> 1/Ωm  $\mu_0$ =1.26x10<sup>-6</sup> Vs/Am  $\mu$ =1

$$\delta = \sqrt{\frac{2}{\mu_0 \mu \sigma \omega}} = 1.7 \ \mu m \qquad \qquad R_s = \frac{1}{\sigma \delta} = 10 \ m\Omega$$



### Surface resistance - some numbers (2)

#### Surface resistance of Cu at 1.5 GHz as a function of temperature

 $R_s(300 \text{ K}) \cong 10 \text{ m}\Omega$ 

 $R_s(4.2 \text{ K}) \cong 1.3 \text{ m}\Omega$ 

RRR =  $\sigma(4.2K)/\sigma(300K)$  = 300

...in spite of the **resistivity** decreasing by a factor 300 from 300 K to 4.2 K, R<sub>s</sub> only decreases by a factor of ~8!





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Electrodynamics of SC is the same as NC, only that we have to change  $\sigma \rightarrow \sigma_1$ - *i*  $\sigma_2$ 

Penetration depth:

pth: 
$$\delta = \sqrt{\frac{2}{\mu_0 \sigma \omega}} = \frac{1}{\sqrt{\mu_0 \omega \sigma_2}} \sqrt{\frac{2i}{1 + i \sigma_1 / \sigma_2}} \cong (1 + i) \lambda_L \left( 1 - i \frac{\sigma_1}{2\sigma_2} \right)$$
$$\sigma_1 << \sigma_2 \text{ for SC at } T << T_c$$

For Nb:  $\lambda_{L}$  = 36 nm compared to  $\delta$  = 1.7 µm for Cu at 1.5 GHz



Recall the definition of the surface impedance: Z

$$Z = \frac{|E_{\parallel}|}{\int_{0}^{\infty} J(x)dx} = \frac{E_{\parallel}}{H_{\parallel}} = R_{s} + i X_{s} = \sqrt{\frac{i\omega\mu_{0}}{\sigma}}$$

$$R_{s} = \frac{1}{2}\mu_{0}^{2}\omega^{2}\sigma_{1}\lambda_{L}^{3}$$
Normal Fluid channel
$$Z_{s} = R_{s} + iX_{s}$$

$$I_{s}$$
Superfluid channel
$$X_{s} = \omega\mu_{0}\lambda_{L}$$

$$L_{s}: \text{ kinetic inductance}$$

$$Z = R_s + i X_s = \sqrt{\frac{i\omega\mu_0}{\sigma}} = \sqrt{\frac{\omega\mu_0}{\sigma_1}} (\varphi_- + i\varphi_+)$$

$$\varphi_{\pm}^{2} = \frac{y}{1+y^{2}} \left( \sqrt{1+y^{2}} \pm 1 \right) \qquad y = \frac{\sigma_{1}}{\sigma_{2}}$$
For a SC  $\sigma_{1} << \sigma_{2} \rightarrow y <<1$ 

$$\varphi_{-} = \sqrt{\frac{y^{3}}{2}} \qquad \varphi_{+} = \sqrt{2y}$$

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 $R_s = \frac{1}{2}\mu_0\omega^2\sigma_1\lambda_L^3$ 

 $R_s \propto \omega^2$  use low-frequency cavities to reduce power dissipation

#### $R_s$ temperature dependence



$${f n_s}$$
 (T)  $\propto$  1-(T/T<sub>c</sub>)<sup>4</sup> near T<sub>c</sub>  
 $\sigma_1$  (T)  $\propto$   ${f n_n}$  (T)  $\propto$  e<sup>-( $\Delta$ /KBT)</sup> at T<c

$$R_s \propto \omega^2 \lambda_L^3 \ell e^{-\Delta/k_B T}$$



 $T < T_c/2$ 

## **Rs within BCS theory**

High-K SC

Mattias and Bardeen (1958) used time dependent perturbation theory to derive  $R_s$  for weak RF fields

Within this theory no simple formula can be derived. Several approximate formula can be found in the literature for some limits. A good approximation of  $R_{BCS}$  in the dirty limit for T<Tc/2 and  $\omega$ < $\Delta\hbar$  is:

"Dirty" SC



$$R_{BCS} \cong \frac{\mu_0^2 \omega^2 \lambda_L^3 \sigma_n \Delta}{k_B T} \ln \left[ \frac{C_1 k_B T}{\hbar \omega} \right] \exp \left( -\frac{\Delta}{k_b T} \right)$$





#### **Rs within BCS theory**

There are numerical codes (Halbritter, 1970) to calculate  $R_{BCS}$  as a function of w, T and material parameters (x<sub>0</sub>, I<sub>L</sub>, T<sub>c</sub>, D, I)

#### SRIMP

This webpage calculates BCS surface resistance under wide range of conditions, and is based on a program by Jurgen Halbritter. [J. Halbritter, Zeitschrift for Physik 238 (1970) 466]

Enter material parameters below, and click submit to calculate the BCS surface resistance. Results are given in a new window.

Please be aware that frequencies much lower than 1 MHz may cause substantial processing times (depending on the user's computer).

Submit	
Frequency (MHz):	1300
Transition temperature (K):	9.2
DELTA/kTc:	1.86
London penetration depth (A):	330
Coherence length (A):	400
RRR:	300
Accuracy of computation:	.001
Temperature (of operation):	2

#### **Results:**

Resistance (Ohm): Diffuse Reflection:



 $R_{BCS}$  Nb  $\approx 20 n\Omega$ 

Penetration Depth (um): 0.037746828693838295

#### **Input Parameters:**

Frequency (MHz):	1300
Transition temperature (K):	9.2
DELTA/kTc:	1.86
London penetration depth (A):	330
Coherence length (A):	400
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Accuracy of computation:	0.001
Temperature (of operation):	2

#### http://www.lepp.cornell.edu/~liepe/webpage/researchsrimp.html



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## BCS vs two fluid model

The treatment within BCS theory and two-fluid model give qualitatively similar results

Quantitatively they can differ by an order of magnitude

The BCS treatment gives qualitatively correct results for low field

To treat experimental data approximate formulae are useful, e.g.

 $R_{\rm S} = \frac{\omega^2 A}{T} \exp\left(-\frac{\Delta}{k_b T}\right) \qquad \qquad R_{\rm S} = \frac{\omega^2 A}{T} \exp\left(-\frac{1.76T_c}{T}\right)$ 

Here A accounts for all material parameters



$$R_{\rm BCS} = \omega^2 \lambda^3 \sigma_0 \mu_0^2 \exp\left(-\frac{\Delta}{k_b T}\right)$$

#### This equation implies $R_s$ :

- Has a minimum for medium purity
- Is proportional to  $\omega^2$
- Decreases exponentially with temperature
- Vanishes as  $T \rightarrow 0$  K
- Is independent of RF field strength

# In the following we will compare these assumptions to experimental data and modify the formula if necessary



## Material purity dependence of R<sub>s</sub>

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The dependence of the penetration depth on  $\boldsymbol{\ell}$  is approximated as  $\lambda(\ell) \approx \lambda_L \sqrt{1 + \frac{\pi \xi_0}{2\ell}}$  $\boldsymbol{\sigma}_1 \propto \boldsymbol{\ell}$ 



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$$R_{\rm BCS} = \omega^2 \lambda^3 \sigma_0 \mu_0^2 \exp\left(-\frac{\Delta}{k_b T}\right)$$

#### This equation implies $R_s$ :

- $\checkmark$  Has a minimum for medium purity
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  - Is independent of RF field strength





Measurement of the surface resistance at low field of niobium at three frequencies with the Quadrupole Resonator



$$R_{\rm BCS} = \omega^2 \lambda^3 \sigma_0 \mu_0^2 \exp\left(-\frac{\Delta}{k_b T}\right)$$

#### This equation implies $R_s$ :

- $\checkmark$  Has a minimum for medium purity
- Is proportional to  $\omega^2$
- Decreases exponentially with temperature
- X Vanishes as T→0 K
  - Is independent of RF field strength



### The residual resistance

For Nb R<sub>res</sub> (~1-10 n $\Omega$ ) dominates R<sub>s</sub> at low frequency (f < ~750 MHz) and low temperature (T < ~2.1 K)

#### Possible contributions to $R_{res}$ :

- Trapped magnetic flux and thermal currents
- Lossy oxides, metallic hydrides
- Normal conducting precipitates
- Grain Boundaries
- Interface Losses
- Magnetic Impurities



B. Aune et al., Phys. Rev. STAB 3 (2000) 092001.



## **Trapped Magnetic Flux**

- Well understood contribution to  $R_{\rm res}$
- When a cavity is cooled down in an ambient DC magnetic field not all flux is expulsed Incomplete Meissner effect
- In fact fields of a few  $\mu T$  (order earth magnetic field) can be completely trapped
- In cryomodules thermal currents can cause additional magnetic fields which can be trapped



## **Trapped magnetic flux**

When a cavity is cooled down in an ambient DC magnetic field not all flux is expulsed - Incomplete Meissner effect

Trapped magnetic field can also result from thermoelectric currents

Dissipation due to oscillating vortex segments, driven by the RF field





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### **Trapped Magnetic Flux Measurements**



FIG. 1. Comparison between the perfect Meissner effect and the suppression of the flux expulsion due to flux pinning.

## Typical levels of trapped magnetic flux in cavities are between 100-1000 nT





Experimental configuration used at Fermilab on Bulk cavities



#### **Trapped Flux - Real Example**





A. Romanenko, A. Grassellino, O. Melnychuk, D. A. Sergatskov, J. Appl. Phys. 115, 184903 (2014)



#### Cooldown procedure influence Rs



### **Normal conducting precipitates**

#### Islands of NbH precipitates at the surface

- Bulk hydrogen conc. > 10 wt.ppm
- Cooling rate < ~1 K/min between 90 150 K



B. Bonin and R. W. Roth, *Proc.* 5<sup>th</sup> SRF Workshop, Hamburg, Germany, 199, p. 210.



F. Barkov, A. Romanenko, and A. Grassellino, Phys. Rev. ST Accel. Beams 15, 122001 (2012)



## The residual resistance



Point contact tunneling experiments on Nb and Nb<sub>3</sub>Sn have found finite density of states (DOS) inside the energy gap

The physics remains not fully understood, however subgap states will yield a finite  $R_{\rm S}({\rm OK})$  irrespective of physical mechanism

A. Gurevich Supercond. Sci. Technol. 30 (2017) 034004



$$R_{\rm BCS} = \omega^2 \lambda^3 \sigma_0 \mu_0^2 \exp\left(-\frac{\Delta}{k_b T}\right)$$

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- X Vanishes as T→0 K
  - Is independent of RF field strength



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- Decreases exponentially with temperature
- X Vanishes as T→0 K
  - Is independent of RF field strength ?



$$R_{\rm BCS} = \omega^2 \lambda^3 \sigma_0 \mu_0^2 \exp\left(-\frac{\Delta}{k_b T}\right)$$

#### This equation implies $R_s$ :

- $\checkmark$  Has a minimum for medium purity
- Is proportional to  $\omega^2$
- Decreases exponentially with temperature
- $\mathbf{X}$  Vanishes as  $T \rightarrow 0$  K
- Is independent of RF field strength

Not only do  $R_{BCS}$  and  $R_{res}$  depend on the RF field strength there can also be additional extrinsic losses limiting the cavity performance



## **Performance of SRF cavities**

There are two parameters which define the performance of an SRF cavity: **quality factor** and the **accelerating gradient** 



There are two principal ways to increase performance: Shape and material optimization



## **RF critical field: superheating field (H<sub>sh</sub>)**



**Penetration and oscillation of vortices** under the RF field gives rise to strong dissipation and the **surface resistance of the order of R**<sub>s</sub> in the normal state

The Meissner state can remain metastable at higher fields,  $H > H_{c1}$  up to the superheating field  $H_{sh}$  at which the Bean-Livingston surface barrier for penetration of vortices disappears and the Meissner state becomes unstable

#### H<sub>sh</sub> is the maximum magnetic field at which a type-II superconductor can remain in a true non-dissipative state not altered by dissipative motion of vortices



### **Superheating Field: theory**

Weak dependence of *H*<sub>sh</sub> on non-magnetic impurities

$$H_{sh}(T) \cong c(\kappa)H_c\left[1-\left(\frac{T}{T_c}\right)^2\right]$$

 $c(\kappa)$  the ratio of the superheating field and the thermodynamic critical field



T. Yogi, G. J. Dick, and J. E. Mercereau. Critical rf magnetic fields for some type-i and type-ii superconductors. Phys. Rev. Lett., 39(13):826–829, Sep 1977.



## **Superheating Field: experimental results**

Use high-power (~1 MW) and short (~100 µs) RF pulses to achieve the metastable state before other loss mechanisms kick-in

#### **RF magnetic fields higher**

than Hc<sub>1</sub> have been measured in both Nb and Nb<sub>3</sub>Sn cavities. H<sub>RF</sub> in Nb<sub>3</sub>Sn is << predicted H<sub>sh</sub>





#### **Superheating Field - real world**





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### **SRF Cavities Extrinsic Limitations**

- Mechanical Vibrations
- Multipacting
- Thermal breakdown (Quench)
- Field Emission



$$E_{acc} = 0.29 B_p$$
 for TESLA type cavities



#### **Performance limitations**





## **Multipacting**

#### Resonant process with emission of electrons from the surface of the cavity

Multipacting is characterized by an exponential growth in the number of electrons in a cavity Multipacting requires 2 conditions:

- Electron motion is periodic (resonance condition): cavity frequency = *n* x cyclotron frequency
- Impact energy is such that secondary emission coefficient is >1





## Multipacting (power curves)





## Multipacting (Q VS E<sub>acc</sub>)





## How to removes multipacting

1. Preventive strategy



#### 2. Healing strategy





## **T-Map experiment**

Use temperature map to look for quench mechanism/site:







Niobium

surface



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### **T-Map experiment**

#### First quench site disappears after many quenches:





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## **T-Map experiment**

#### **Observe quenches happening in two different spots:**





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#### **Performance limitations**





## **Quench (Thermal Breakdown)**

#### Localized heating at normal-conducting defects Local magnetic field enhancement at sharp edges





## **Thermal Breakdown**

#### Quench is the final limitation set by the critical field of the material

A quench can however occur at much lower fields if the magnetic field locally exceeds the critical field or the temperature exceeds the critical temperature at sub mm size defects of high resistivity

At high fields these defects will heat up its surrounding area above  $T_c$  and a normal conducting area will spread causing a quench









## **Cures for Quench**

#### **Prevention: avoid the defects**

- Use material with high thermal conductivity: high purity niobium or niobium on copper cavities
- Careful electron beam welding or seamless cavities
- Eddy-current scanning of Nb sheets

#### Post processing

- In production usually the cavity is chemically etched again
- Big defects with sizes of 1 mm can be mechanically grinded away. This requires knowledge of the quench position from online diagnostics during cold test and optical inspection afterwards



### **Quench localization and visualization**

#### Quench sites can be located with temperature mapping



#### Afterwards the location can be visualized with an optical inspection system





## **Cavity Quench**





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Superconductive Materials

11 Basic principles of SRF

### Near quench behavior

• Measure temperature of sensor near the quench point as field is increased





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#### **Performance limitations**





### **Field emission**

• Under high RF fields electrons can be released from the surface and accelerated





Field emitters found on dissected cavities (size 0.5-10µm with sharp edges)

• Released electrons will impact on the cavity wall creating x-rays and heating

#### $\rightarrow$ Reduced Q-value





## **Cures for Field Emission**

#### **Prevention:**

Semiconductor grade acids and solvents

High Pressure Rinsing with ultra-pure water

Clean-room assembly

Simplified procedures and components for assembly

Clean vacuum systems (evacuation and venting without re-contamination)

#### **Post-processing:**

Helium processing

High Peak Power (HPP) processing



## How to removes Field emission





Solution to field emission  $\rightarrow$  high pressure water rinsing (100 atm) and an **ultra-clean assembly**  $\rightarrow$  remove field emitters and preserve cleanliness



#### **SRF Cavities Intrinsic Limitations**





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## The hydrogen Q-disease

- If a cavity is cooled down slowly around 50-150K Q decreases
- Effect correlated to hydrides
- Some cavities recover after warm up to RT
- 800°C baking is always effective





#### **Performance limitations**

![](_page_61_Figure_1.jpeg)

![](_page_61_Picture_2.jpeg)

## The high field Q-slope

#### **Observations:**

- Strong decrease of  $Q_0$  above  $E_{acc} > 20 \text{ MV/m}$  (in Tesla cavities  $B_p > 85 \text{ mT}$ )
- Field emission not involved ( no e -, no X rays )
- T map: global heating in the area of max B-field
- Limitation by RF power supply or quench
- Seemingly a typical feature of **BCP** cavities
- Solved with EP instead of BCP and baking treatments

![](_page_62_Figure_8.jpeg)

![](_page_62_Figure_9.jpeg)

(L. Lilje et al. - SRF '99 - Santa Fe)

![](_page_62_Picture_11.jpeg)

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#### **Baking Effect on BCP Cavities**

- "in-situ" baking discovered on **BCP** cavity
- slope improvement ( $90 < T < 120^{\circ}C$ ) degradation ( $T > 150^{\circ}C$ )

![](_page_63_Figure_3.jpeg)

![](_page_63_Picture_4.jpeg)

### **Baking Effect on EP Cavities**

- Same phenomenon on E.P. cavities
- before baking: Q-slope identical to BCP
- after baking: **Q-slope improvement**

![](_page_64_Figure_4.jpeg)

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#### **Performance limitations**

![](_page_65_Figure_1.jpeg)

![](_page_65_Picture_2.jpeg)

#### **State of the art Nb cavities**

![](_page_66_Figure_1.jpeg)

- Nb is reaching fundamental limits in quality factor and accelerating gradient
- Unfortunately so far we can have only one or the other and only for elliptical niobium cavities.
- There is still margin for improvement of nonelliptical cavities.
- For performance far beyond the state of the art of elliptical cavities materials other than Nb need to considered

![](_page_66_Picture_6.jpeg)

#### **Recommanded Literature**

- R. Padamsee, J. Knobloch and T. Hays « RF Superconductivity for Accelerators », Wiley-VCH, 2008
- J. P. Turneaure, J. Halbritter, and H. A. Schwettman. « The surface impedance of superconductors and normal conductors: The Mattis-Bardeen theory. » Journal of Superconductivity 4.5 (1991): 341-355
- A. Gurevich « Theory of RF superconductivity for resonant cavities. » Superconductor Science and Technology, 30(3), 034004 (2017).
- SRF Tutorials

![](_page_67_Picture_5.jpeg)

![](_page_68_Picture_0.jpeg)