



UNIVERSITÀ DEGLI STUDI DI PADOVA

Network Science

A.Y. 23/24

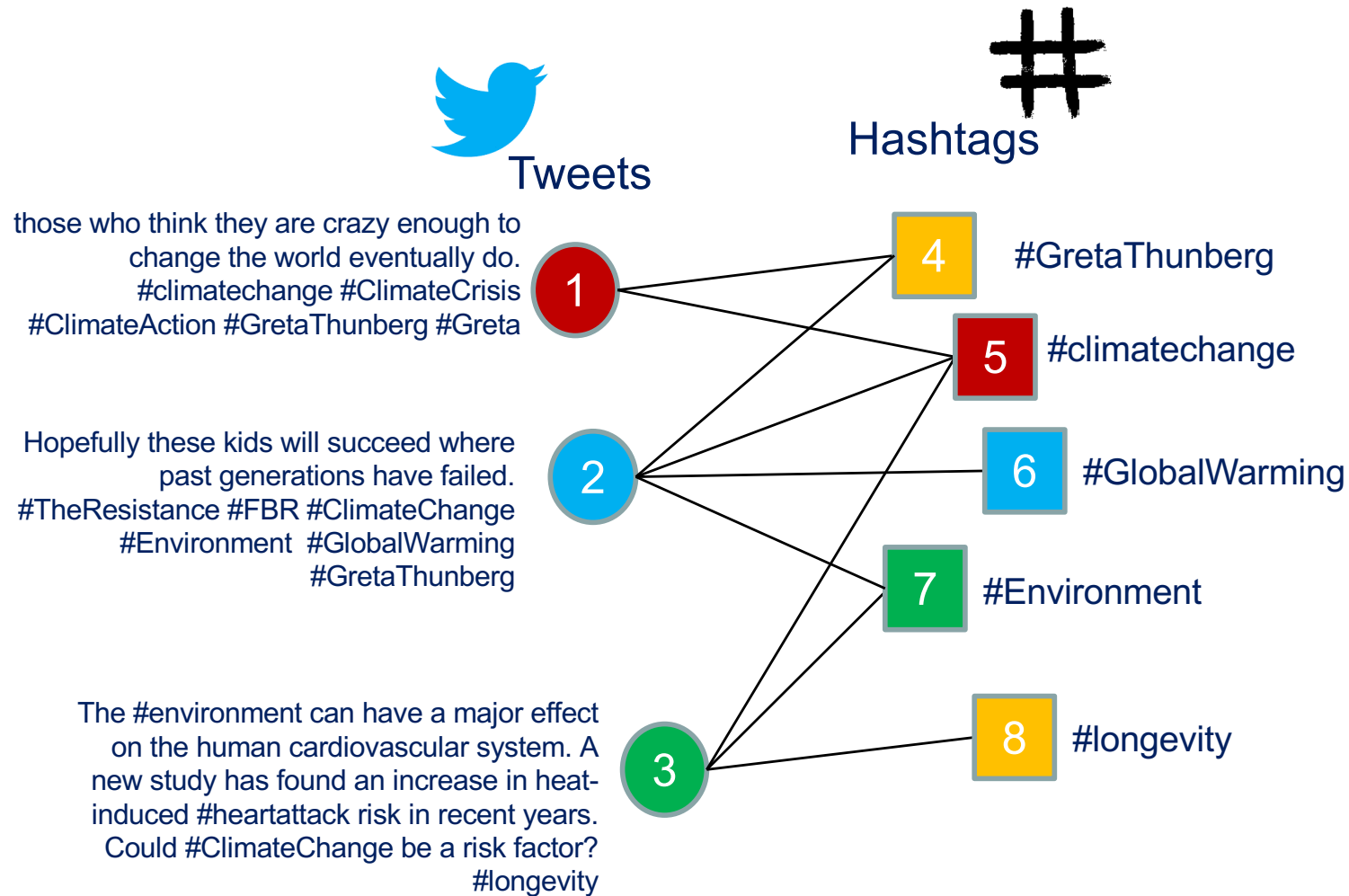
ICT for Internet & multimedia, Data science, Physics of data

Semantic networks

network science tools for their study



Conceptual picture of a semantic network on Twitter





- ❑ Data collection + polishing
- ❑ Building the semantic network (bipartite/projections)
- ❑ Topic (i.e., community) detection
 - ❑ Modularity & InfoMap
 - ❑ Non-negative matrix factorization (NMF)
 - ❑ Latent Dirichlet allocation (LDA)
 - ❑ Variational auto-encoders (VAE)
 - ❑ Embeddings and BERTopic

Data collection

how to get data from the Internet using APIs



no longer available unless you pay 5k\$ per month ☹️

<https://developer.twitter.com/en/portal/dashboard>

Twitter’s plan to cut off free data access evokes ‘fair amount of panic’ among scientists

Social media platform’s intent to increase revenue could end or limit many research projects

8 FEB 2023 · 4:35 PM ET · BY [KAI KUPFERSCHMIDT](#)

Twitter’s plan to charge researchers for data access puts it in EU crosshairs

Elon Musk’s social media giant plans to charge academics to access its data – in potential violation of Europe’s content rules

BY MARK SCOTT
MARCH 22, 2023



Academic researchers blast Twitter’s data paywall as ‘outrageously expensive’



By [Brian Fung](#), CNN

Published 11:40 AM EDT, Wed April 5, 2023



Reddit

Subreddit

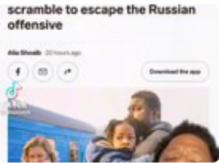
Search: ukraine

Sort: Time

r/blackoutukraine · Posted by u/One-Designer-9406 2 years ago

SPOILER


Racism in Ukraine is getting out of hand
#racisminukrain #ukrainewar #blackoutukraine



0 upvotes 0 comments

r/MapPorn · Posted by u/fpl123999 9 months ago

Ukraine war last 10 months in 15 seconds



2.3k upvotes 245 comments

Search: ukraine

r/ukrainewar · 3.5k Members
reddit for events of the Ukranian-Russian war ongoing since February 24, 2022. [Join](#)

r/UkraineWarVideoReport · 722k Members
Community Driven Videos/Photos/Updates and Discussion [Join](#)

r/RuZZiaUkrainewar · 321 Members
Unbiased reporting of the Russian Ukraine war. Please be respectful of Pro-Russian views as well as Pro-Ukrainian views. feel free to contribute [Join](#)


r/UkrainianConflict · 453k Members
News, analysis, discussion and investigative journalism documenting the ongoing conflict in Ukraine. [Join](#)



GET NEW REDDIT | MY SUBREDDITS | HOME - POPULAR - ALL - RANDOM - USERS | ASKREDDIT - GAMING - PICS - TODAYILEARNED - FUNNY - WORLDNEWS - NEWS - MOVIES - M

reddit | PREFERENCES | options | **apps** | RSS feeds | friends | blocked | password/email | delete | Upbeat-Lychee-6630 (1) |

developed applications



ns2023
personal use script

Qbdk-FkA9jSQB9T7drY8UQ

client_id

download reddit context for the network science course, at the unioversity of Padova, of which I am the instructor

username

Upbeat-Lychee-6630 (that's you!) [remove](#)

add developer:

secret **jtGPdqiaTj6hCWcvRPeS_nMNEEnVkwx** *client_secret*

name

description

about url

redirect uri

[delete app](#)

register
asap... will
be using this
in the 1st lab



Python Reddit API Wrapper – PRAW

<https://praw.readthedocs.io/en/stable/> (v7.7.1)

```
!pip install praw
```

```
import pandas as pd
import praw
reddit = praw.Reddit(client_id='Qbdk-FkA9jsQB9T7drY8UQ',
                    client_secret="jtGPdqiaTj6hCWcvRPeS_nMNEVkw",
                    user_agent='reddit scraper 1.0 by u/Upbeat-Lychee-6630',
                    check_for_async=False)
print(reddit.read_only)
```

True

```
df = pd.DataFrame([vars(post) for post in reddit.subreddit("all")
                  .search("#ukrainewar", sort='top', limit=10)])
```

```
df.to_excel('drive/MyDrive/Colab Notebooks/samples.xlsx',
           index=True)
```

your own description of your app,
including version and username

from Reddit apps

"relevance", "hot", "top",
"new", or "comments"

max 250
per call

can also add `time_filter =`
"all", "day", "hour", "month", "week", or "year"



there is a list of 116 entries per post,
on which you can choose!!!

from this you extract the date

	title	created	score	upvote_ratio	ups	num_comments	selftext
0	Damn...we blinked and missed the T-34 stage of...	1.666899e+09	10394	0.99	10394	738	
1	Finnish🇫🇮 volunteer sends greetings home from ...	1.680237e+09	2095	1.00	2095	57	
2	Guess having 5 trucks fall into your office ca...	1.663341e+09	1974	1.00	1974	88	
3	[META] Important - Russia-Ukraine Crisis/War: ...	1.645712e+09	1284	0.89	1284	1	Hi, /u/Anonim97 here.\n\nWe - as a mods of 40k...
4	V*tniks coping hard Over the counter offensive...	1.662956e+09	1081	1.00	1081	86	
...
0	Russia Ukraine War.	1.695349e+09	1	1.00	1	0	





Content Posting API

Display API

Research API

About Research API

Getting Started

Frequently Asked Questions

Codebook

API Reference

Query Videos

Query User Info

Query Video Comments

Query Videos

Request

HTTP URL	https://open.tiktokapis.com/v2/research/video/query/
HTTP Method	POST
Scopes	research.data.basic

Headers

Key	Type	Description
-----	------	-------------



TikTok Research API application received

Thank you for applying to gain access to TikTok's research APIs. We have received your application and will proceed with the review process. You will be notified of the result via email within 3-4 weeks. If you have any questions, please contact our Support team.



The screenshot shows the EnsembleData website homepage. At the top, there is a navigation bar with the EnsembleData logo and links for Home, Products, Documentation, and Pricing. The main content area features a large heading: "Social media scraping through simple APIs". Below the heading, there is a sub-heading: "Fetch data from TikTok, Instagram, YouTube through simple APIs. Real-time, fast, reliable and easy to integrate". At the bottom of the main content area, there are two buttons: "Get started" and "Documentation".

1 week trial period... register later on

The screenshot shows the GitHub repository page for EnsembleData/TikTokScraper. The repository is public and has 1 branch (main) and 0 tags. The commit history shows a recent commit by fracogno titled "Fix" with a commit message "upload tt logo". Below the commit history, there is a table of files and folders:

File/Folder	Commit Message
images	upload tt logo
src	Fix
Update README.md	

<https://github.com/EnsembleData/TikTokScraper>

Data preprocessing

how to polish raw data from the Internet



1. Superficial cleaning

Removing website links
Removing accented characters
Removing text inside square brackets
Removing moderator messages
Removing double spaces
Removing non-text special words and characters
Removing extra-used new lines
Limiting all the repetitions to two characters and removing the extra characters
Removing punctuation except main sentence punctuation
Removing sentences that represent the rules of the community

Fixing **contractions**
Removing **emoji**
Removing **hashtags** and **mentions**
Removing **numbers**
Lowercasing
Correct **spellings**

2. Subsentence

Tokenise subsentences

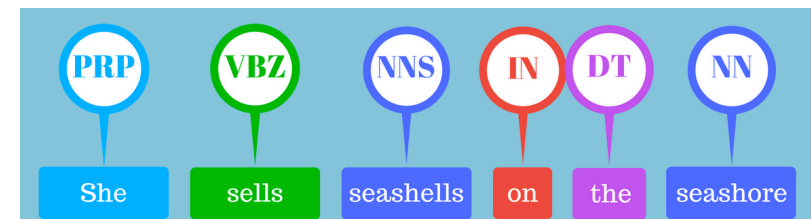
useful for long
text samples
(e.g., Reddit)

the bare minimum to
polish the text,
useful as an input to
sentiment analysis

3. Deep cleaning

Stop word removal
Word tokenization
POS tagging
Lemmatization

truly polished
text, useful for
building a
semantic
network





POS	description	example	POS	description	example
ADJ	adjective	big, old, green, incomprehensible, first	PART	particle	's, not,
ADP	adposition	in, to, during	PRON	pronoun	I, you, he, she, myself, themselves, somebody
ADV	adverb	very, tomorrow, down, where, there	PROPN	proper noun	Mary, John, London, NATO, HBO
AUX	auxiliary	is, has (done), will (do), should (do)	PUNCT	punctuation	., (,), ?
CONJ	conjunction	and, or, but	SCONJ	subordinating conjunction	if, while, that
CCONJ	coordinating conjunction	and, or, but	SYM	symbol	\$, %, §, ©, +, -, ×, ÷, =, :, 😊
DET	determiner	a, an, the	VERB	verb	run, runs, running, eat, ate, eating
INTJ	interjection	psst, ouch, bravo, hello	X	other	sfpkdspxmsa
NOUN	noun	girl, cat, tree, air, beauty	SPACE	space	
NUM	numeral	1, 2017, one, seventy-seven, IV, MMXIV			



title	true date	score	upvote_ratio	selftext	superficial cleaning	deep cleaning	
	created				title_sup_clean	title_deep_clean	title_deep_clean_pos
Damn...we blinked and missed the T-34 stage of...	2022-10-27	10390	0.99	NaN	damn we blinked and missed the t stage of the ...	damn blink miss t stage war	[damn ADV, blink VERB, miss VERB, t PROPN, sta...
Finnish🇫🇮 volunteer sends greetings home from ...	2023-03-31	2095	1.00	NaN	finnish volunteer sends greetings home from so...	finnish volunteer send greeting home	[finnish ADJ, volunteer NOUN, send VERB, greet...
Guess having 5 trucks fall into your office ca...	2022-09-16	1980	1.00	NaN	guess having trucks fall into your office can ...	guess have truck fall office significant emoti...	[guess VERB, have VERB, truck NOUN, fall VERB,...
[META] Important - Russia-Ukraine Crisis/War: ...	2022-02-24	1280	0.89	Hi, /u/Anonim97 here.\n\nWe - as a mods of 40k...	important russia ukraine crisis war info and ...	important russia ukraine crisis war info way help	[important ADJ, russia PROPN, ukraine PROPN, c...
V*tniks coping hard Over the counter offensive...	2022-09-12	1076	1.00	NaN	v tniks coping hard over the counter offensive...	tnik cope hard counter offensive traitor pfp lmao	[tnik NOUN, cope VERB, hard ADJ, counter NOUN,...
...



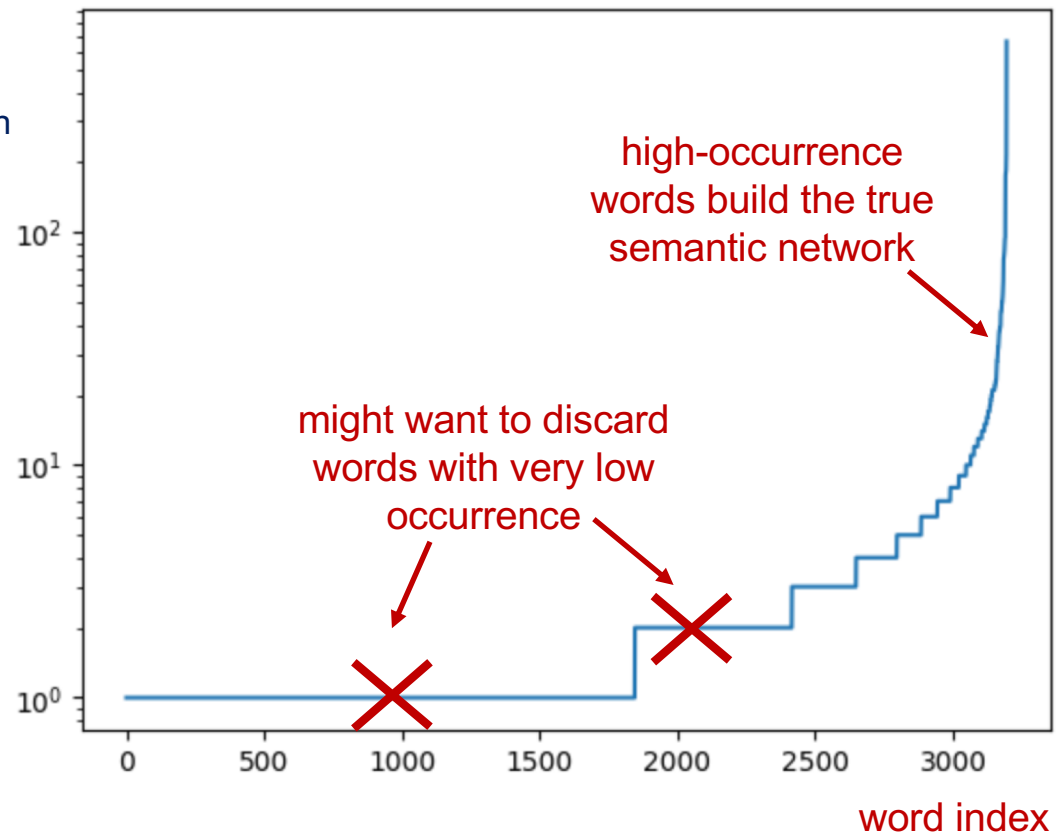
only ADJ, ADV, NOUN, PRON, PROPN, VERB kept



Example

always check words occurrences

occurrence
(i.e., number of
times it appears in
the documents)



Building the semantic network

bipartite and projected counterparts



Probability matrices linking words to documents

number of occurrences
of words in documents

$$N_{wd} = \begin{array}{cccc|l} 0 & 1 & 1 & 1 & \#globalwarming \\ 1 & 1 & 1 & 1 & \#climatechange \\ 1 & 0 & 1 & 0 & \#climateaction \\ 0 & 0 & 1 & 1 & \#gretathunberg \\ 1 & 0 & 1 & 1 & \#environment \end{array}$$

probability of words
given a documents

$$P_{w|d} = \begin{array}{cccc} 0 & \frac{1}{2} & \frac{1}{5} & \frac{1}{4} \\ \frac{1}{3} & \frac{1}{2} & \frac{1}{5} & \frac{1}{4} \\ \frac{1}{3} & 0 & \frac{1}{5} & 0 \\ 0 & 0 & \frac{1}{5} & \frac{1}{4} \\ \frac{1}{3} & 0 & \frac{1}{5} & \frac{1}{4} \end{array}$$

we identify a **document** probability $p_d = \begin{cases} \frac{1}{D} & \text{equally likely} \\ \frac{n_d}{\sum_d n_d} & \text{custom} \end{cases}$

we capture the **statistical** properties by normalizing by columns



Probability matrices projecting to words or documents

bipartite
network

joint probability of words
and documents

$$P_{wd} = P_{w|d} \text{diag}(p_d)$$

0	1/8	1/20	1/16
1/12	1/8	1/20	1/16
1/12	0	1/20	0
0	0	1/20	1/16
1/12	0	1/20	1/16

marginal probabilities

$$p_w = P_{wd} \mathbf{1} \quad p_d = P_{wd}^T \mathbf{1}$$

$$p_{w_1, w_2} = \sum_d p_{w_1|d} \cancel{p_{w_2|d}} p_{w_2, d}$$

$$P_{ww} = P_{wd} \text{diag}(p_d)^{-1} P_{wd}^T$$

$$p_w = P_{ww} \mathbf{1}$$

projection on words

projection on documents

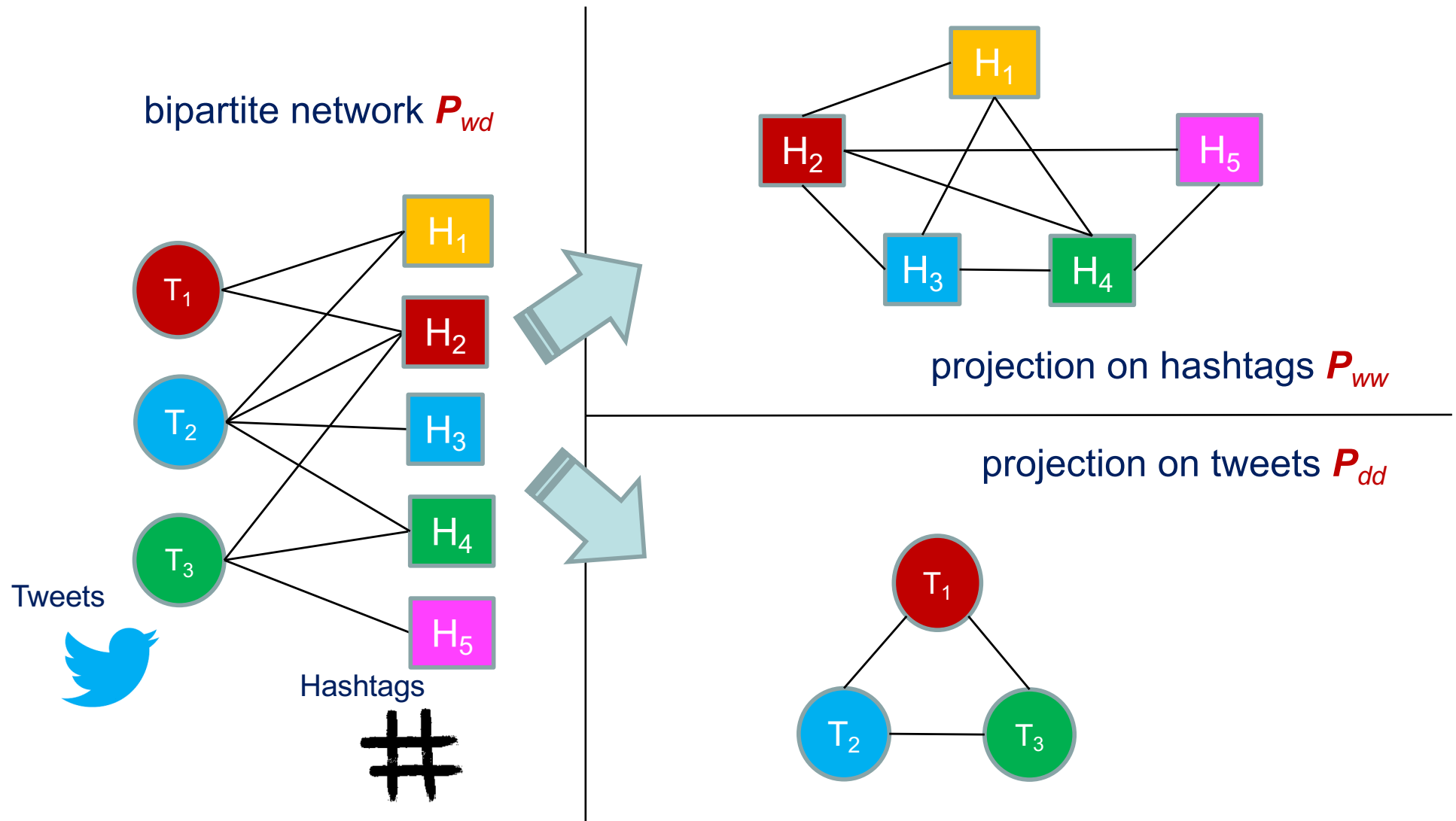
$$p_{d_1, d_2} = \sum_w p_{d_1|w} \cancel{p_{d_2|w}} p_{d_2, w}$$

$$P_{dd} = P_{wd}^T \text{diag}(p_w)^{-1} P_{wd}$$

$$p_d = P_{dd} \mathbf{1}$$

Bipartite and projected networks

a comparison





The role of TF-IDF

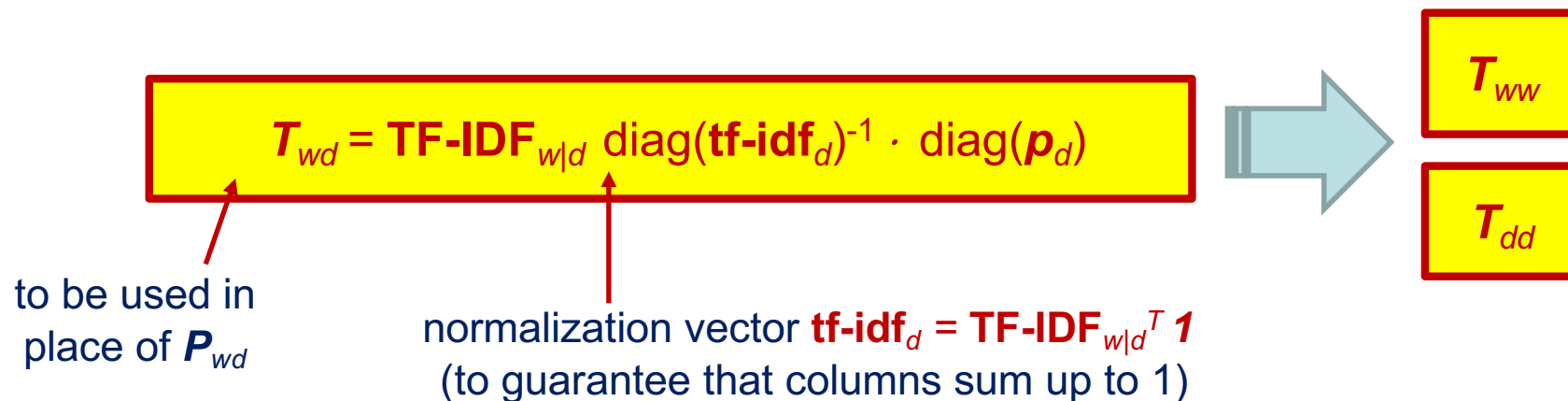
term frequency – inverse document frequency

term frequency =
frequency (probability) of
the word in the document

inverse document frequency =
(log) fraction of documents
that contain the word

$$\text{TF-IDF}_{w|d} = p_{w|d} \cdot -\log \left(\frac{\sum_d (n_{wd} > 0)}{D} \right)$$

- ❑ An heuristic
- ❑ **Punishes** words that appear in many documents
- ❑ **Enhances** words that are document specific



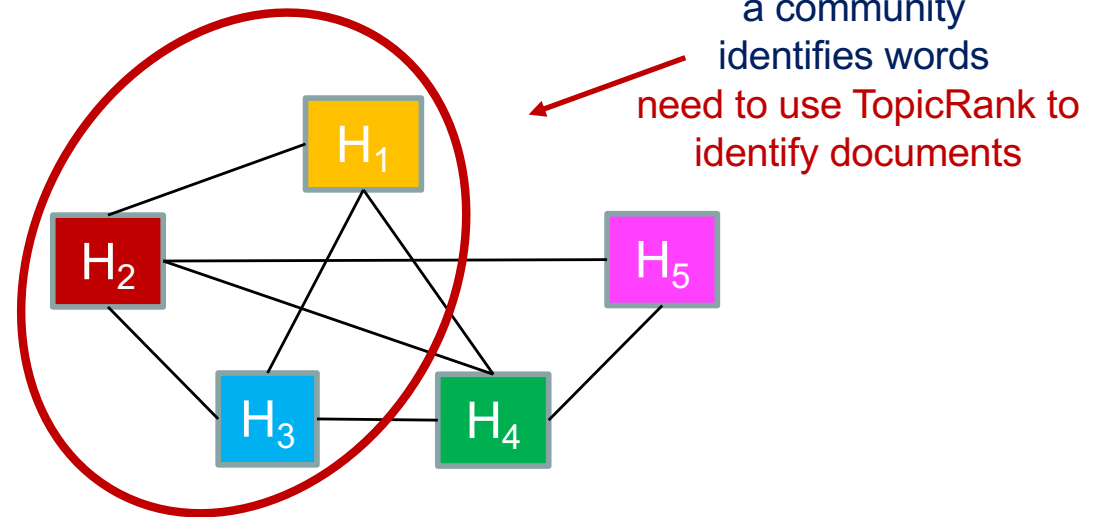
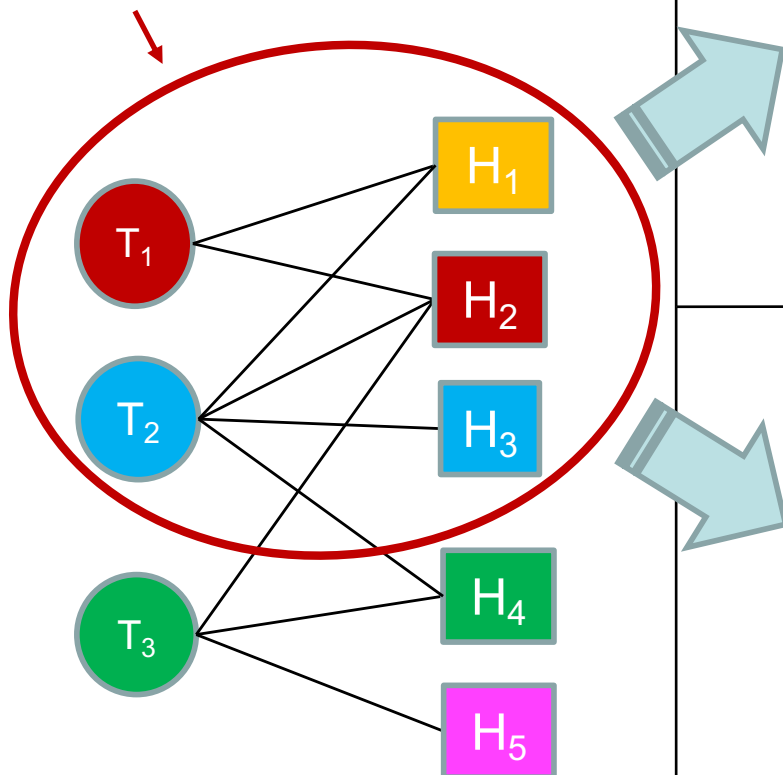
Topic detection

i.e., community detection in semantic networks



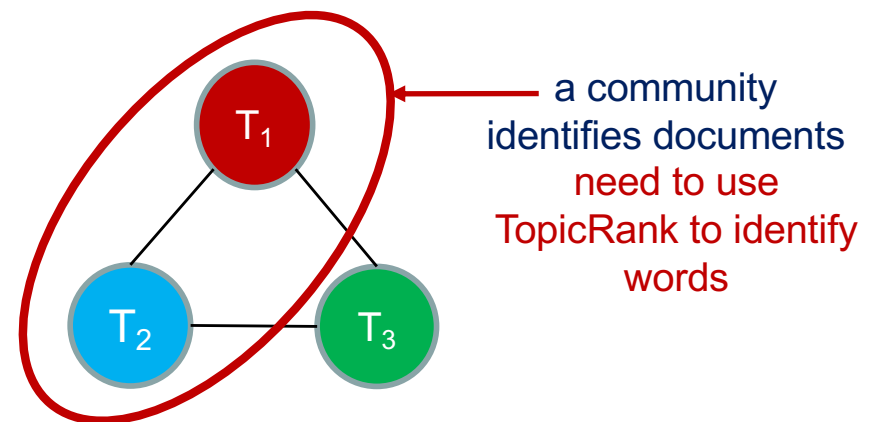
bipartite network P_{wd} or T_{wd}

a community identifies both documents and words



projection on words P_{ww} or T_{ww}

projection on documents P_{dd} or T_{dd}





Tweet 1 is assigned
to **Topic 1** !!!

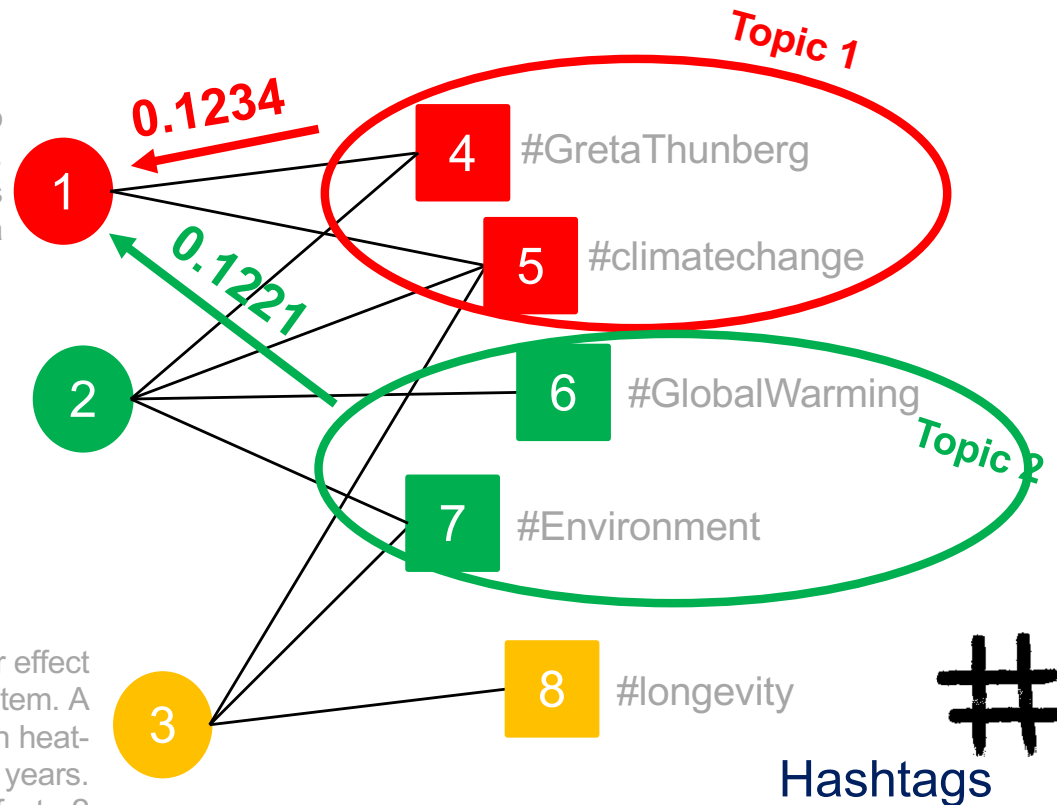


Tweets

those who think they are crazy enough to change the world eventually do.
#climatechange #ClimateCrisis
#ClimateAction #GretaThunberg #Greta

Hopefully these kids will succeed where past generations have failed.
#TheResistance #FBR #ClimateChange
#Environment #GlobalWarming
#GretaThunberg

The #environment can have a major effect on the human cardiovascular system. A new study has found an increase in heat-induced #heartattack risk in recent years. Could #ClimateChange be a risk factor?
#longevity





Normalized mutual information

a wrap-up in topic detection

statistical dependencies about
words and topics

$$P_{wt} = P_{wd} C^T$$



probability of a
topic

$$p_t = P_{wt}^T \mathbf{1}$$

fraction of knowledge related to
the topic that is explained by
words (equal to 1 if topics use
different words)

$$\text{NMI} = \frac{I(W;T)}{H(T)}$$





C topic assignment to be assessed for quality

$$P_{tt} = C P_{dd} C^T$$

can be interpreted as a probability matrix linking topics, its entries are the sum of the links of **A** from topic *i* to topic *j*

P_{11}	P_{12}	P_{13}
P_{21}	P_{22}	P_{23}
P_{31}	P_{32}	P_{33}

$$p_t = P_{tt} \mathbf{1}$$

can be interpreted as the probability vector of topics

modularity

$$Q = \sum_t (P_{tt} - p_t^2) < 1$$

to be maximized

normalized cut

normalized version

$$Ncut = 1 - \frac{\sum_t P_{tt}/p_t}{\sum_t 1} > 0$$

to be minimized



PageRank vector (ranking of documents)

$$\mathbf{r} = (1-c) \mathbf{P}_{d|d} \mathbf{r} + c \mathbf{1}/N$$

Here c_i
is the i th
row of \mathbf{C}

$$\mathbf{P}_{d|d} = \mathbf{P}_{dd} \text{diag}^{-1}(\mathbf{p}_d)$$

$$q_i = \left(1 - (1 - c) \frac{c_i \mathbf{1}}{N} \right) \mathbf{z}_i \mathbf{1} - c c_i \mathbf{P}_{d|d} \mathbf{z}_i^T$$

$$\mathbf{z}_i = c_i \text{diag}(\mathbf{r})$$

$$\text{InfoMap} = f(\mathbf{q}) + \sum_i f([q_i, \mathbf{z}_i])$$

normalized version

$$\frac{\text{InfoMap}}{f(\mathbf{r})} - 1$$

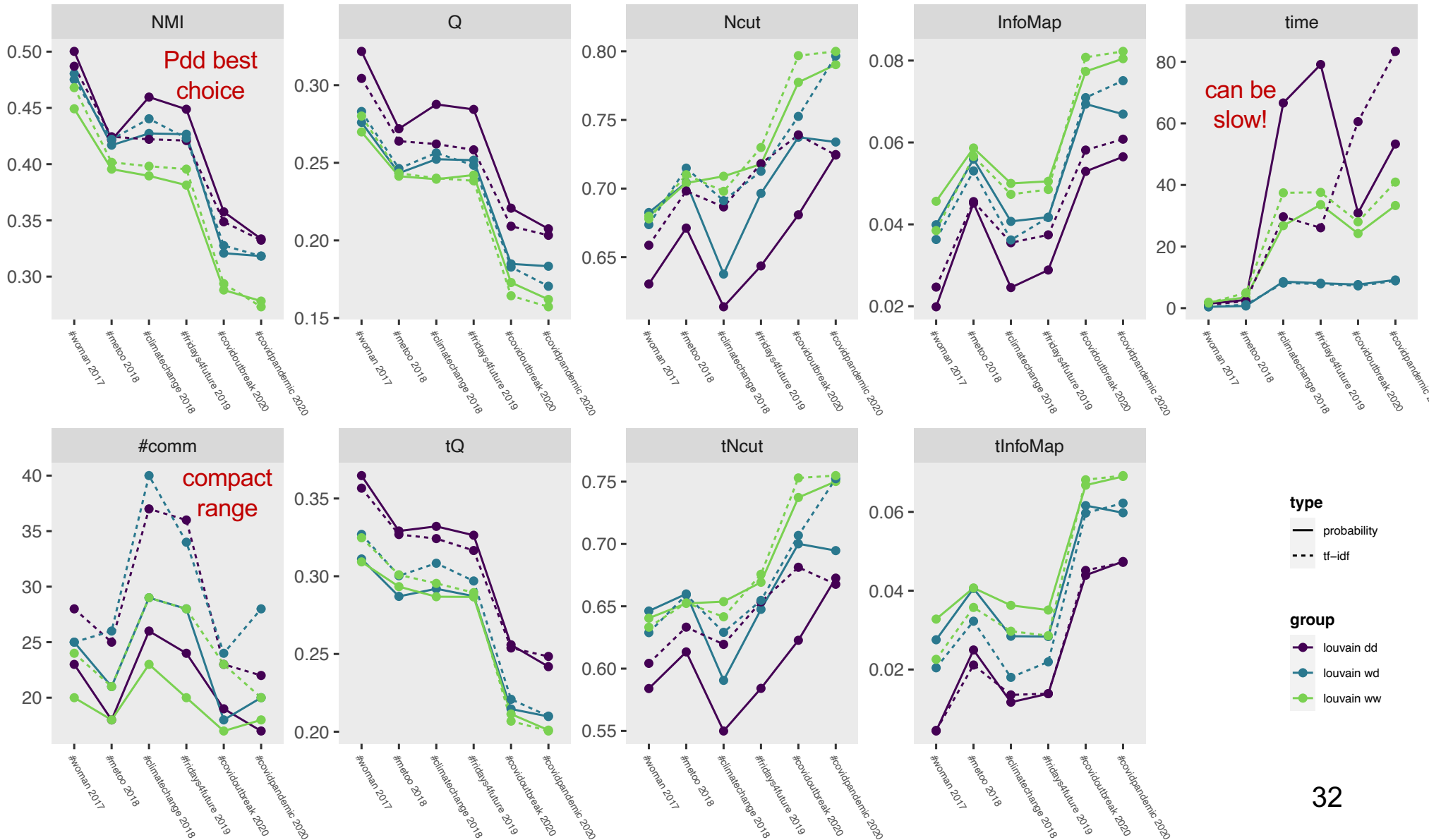
to be minimized

entropy function

$$f(\mathbf{x}) = - \sum_i x_i \log \left(\frac{x_i}{\sum_j x_j} \right)$$

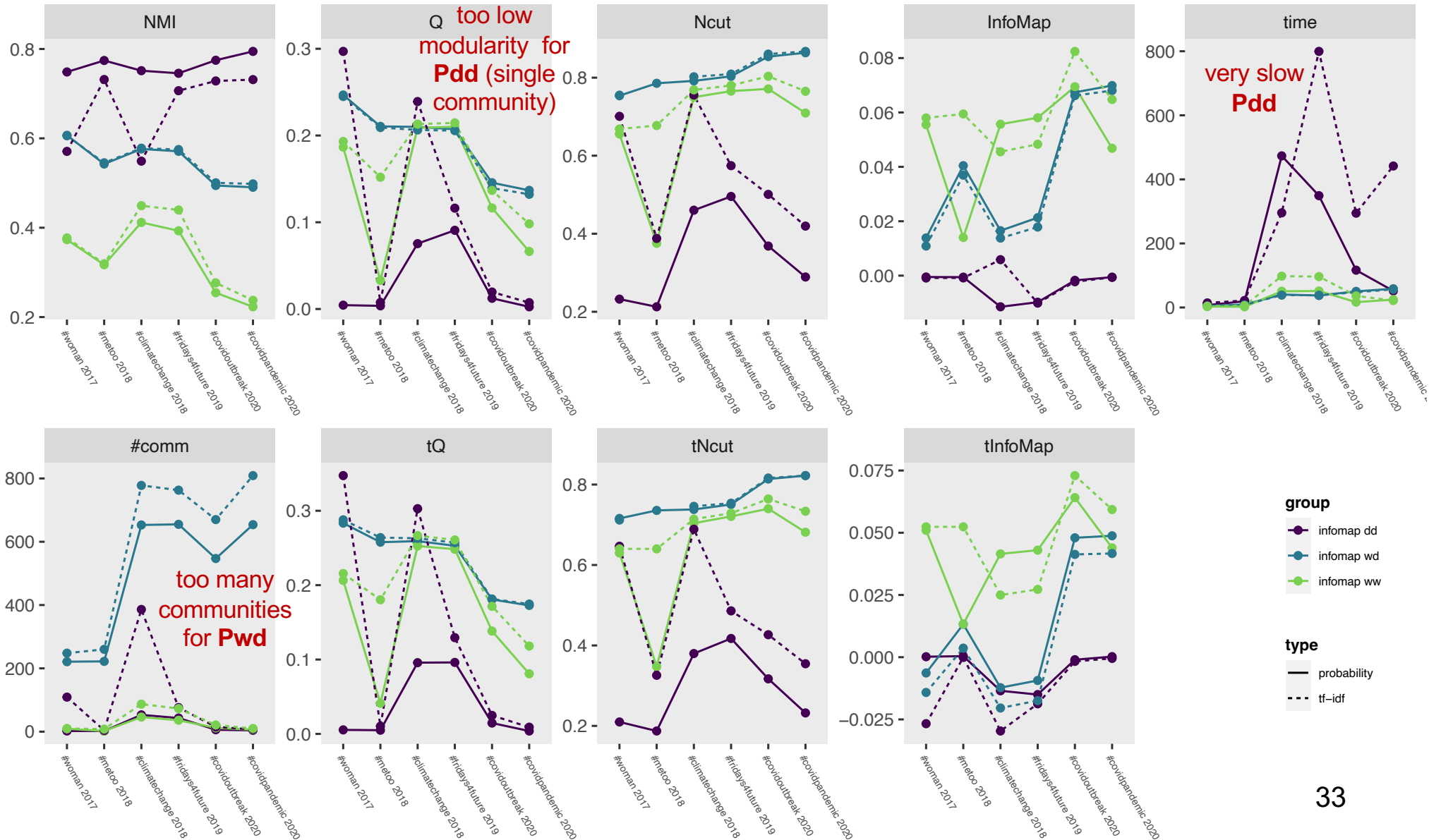


A comparison of the different approaches - Louvain



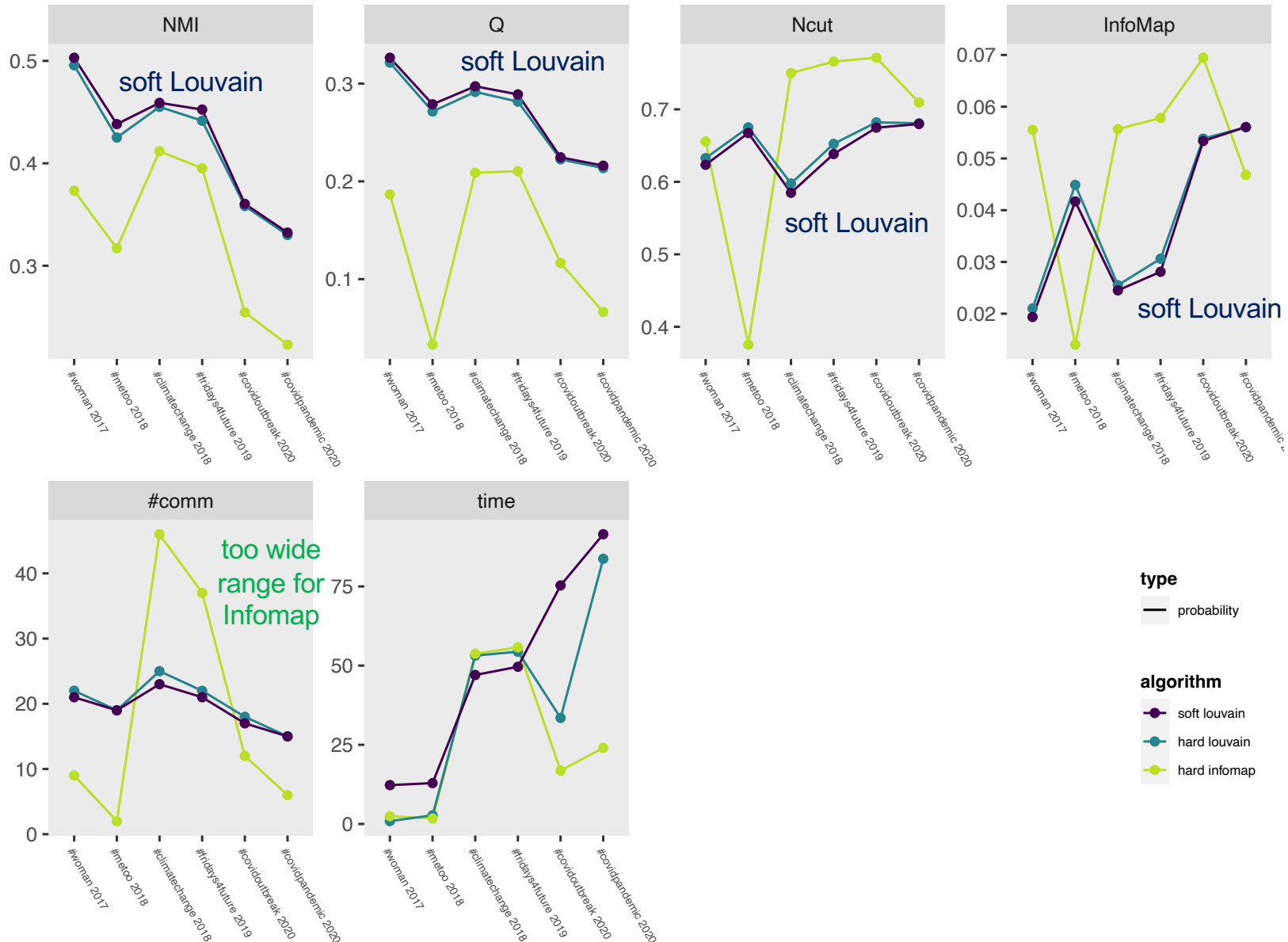


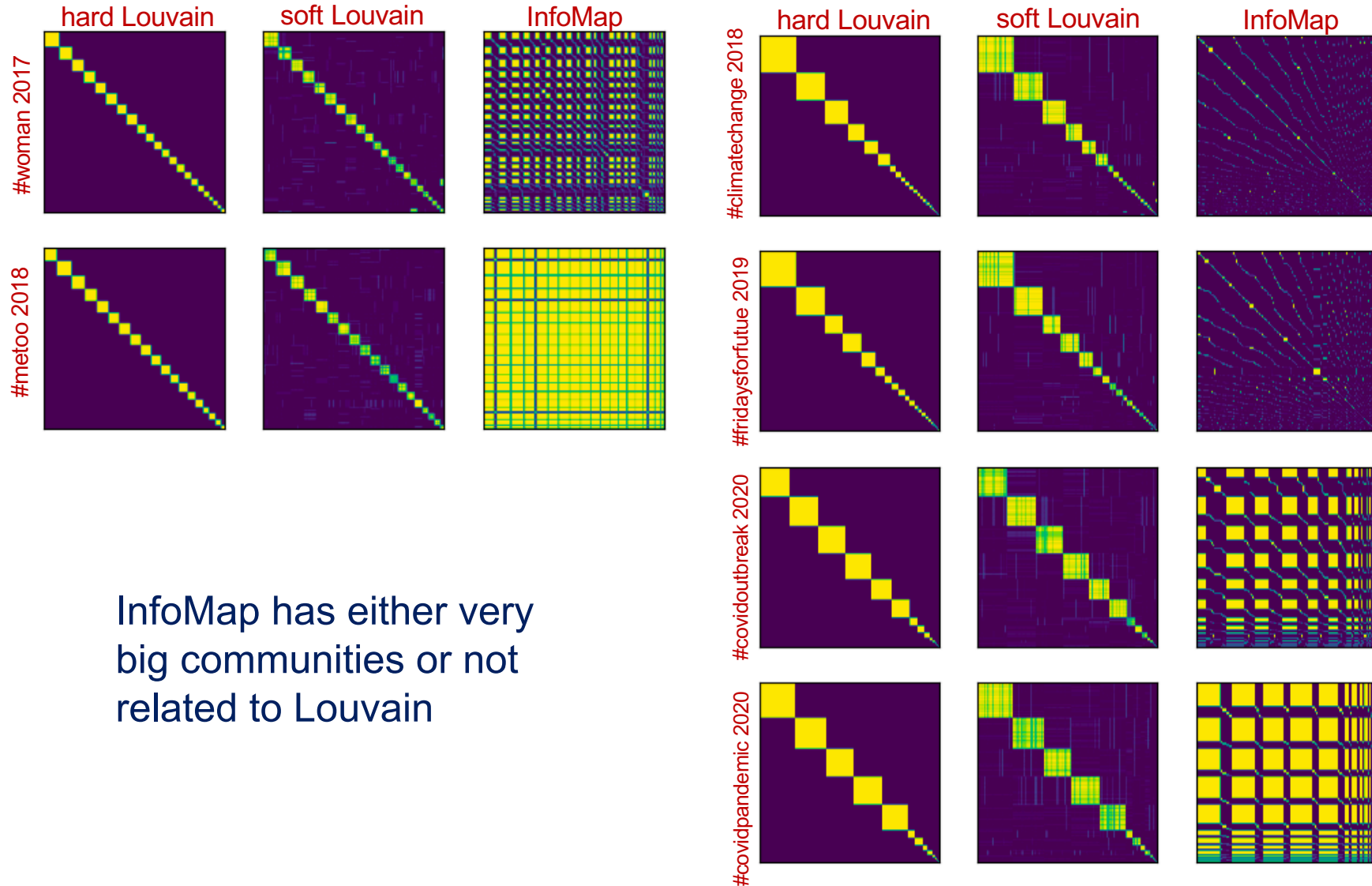
A comparison of the different approaches - Infomap





A comparison hard/soft Louvain Pdd versus InfoMap Pww





InfoMap has either very big communities or not related to Louvain



- ❑ Louvain Pdd – provides the best results
produces balanced clusters
- ❑ Louvain soft – slightly strengthens the result
- ❑ Bipartite networks – run much faster
but performance deteriorates
- ❑ InfoMap – not robust 😞
would be nice to see **BigCLAM** and **SBMs**
... your task! 😊

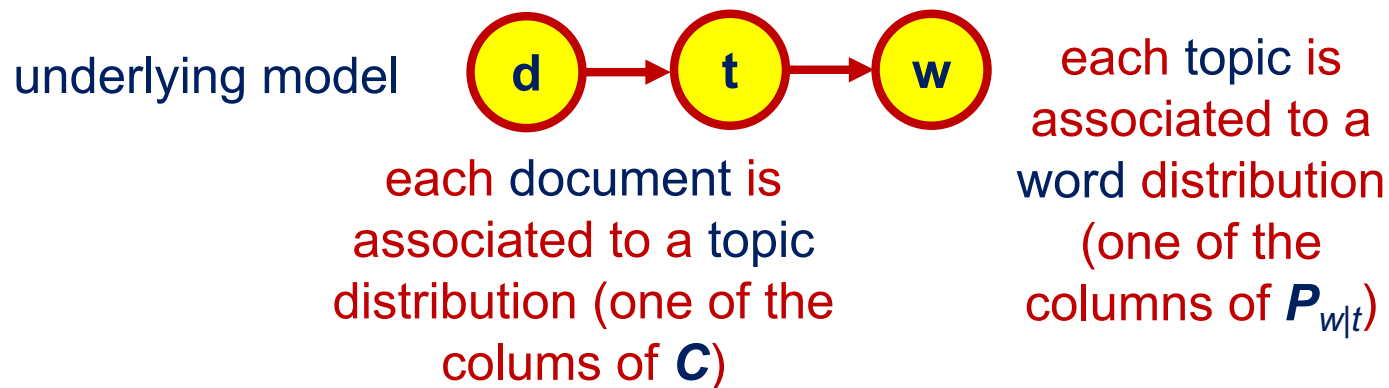
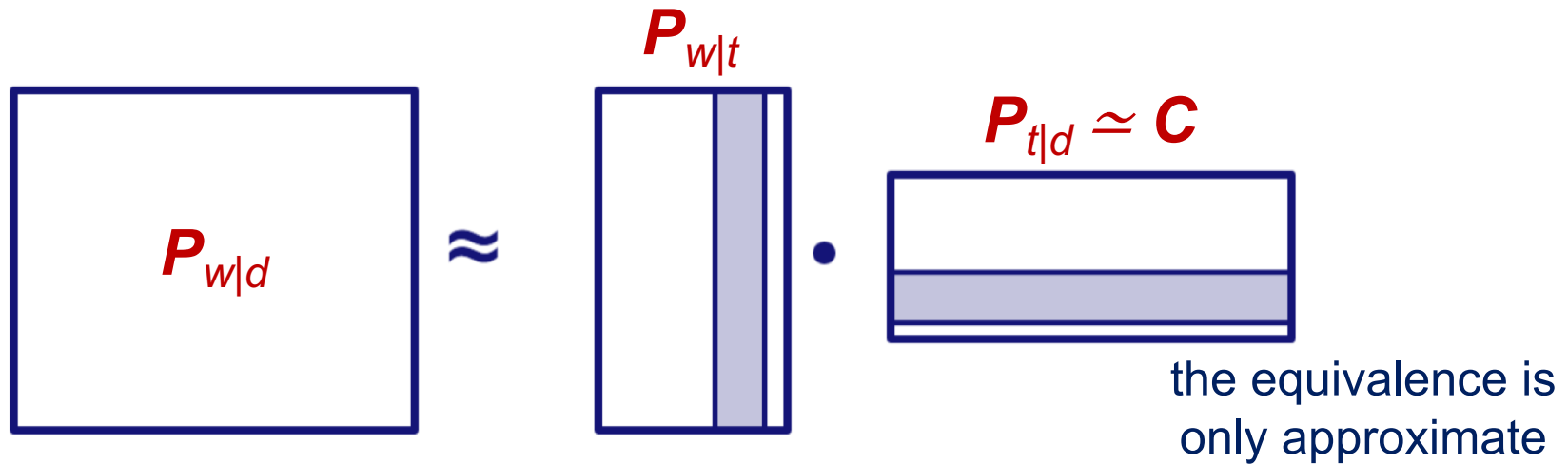
Non-negative Matrix Factorization

and its application to topic detection



NMF = nonnegative matrix factorization

rationale





$A = P_{w|d}$ is column stochastic

$$\operatorname{argmin}_{W \geq 0, H \geq 0} \sum_{ij} |A_{ij} - [WH]_{ij}|^2$$

minimizing the Frobenius norm does not ensure a column stochastic product WH

$$\operatorname{argmin}_{W \geq 0, H \geq 0} \sum_{ij} A_{ij} \log \left(\frac{A_{ij}}{[WH]_{ij}} \right) - A_{ij} + [WH]_{ij}$$

minimizing the generalized Kullback-Leibler divergence ensures a column stochastic product WH

$$f(y) = x \log \left(\frac{x}{y} \right) - x + y$$

$$f'(y) = -\frac{x}{y} + 1 = 0 \rightarrow y = x$$

Ho & Van Dooren. "Non-negative matrix factorization with fixed row and column sums." (2008)



```
from sklearn.decomposition import NMF  
Pwgd = Pwd/Pwd.sum(axis=0).flatten()
```

run on different number of topics, then choose
the best fit, e.g., according to modularity

```
# fit nmf model  $X = W \cdot H$   
model = NMF(n_components=i, init='nndsvd',  
            solver='mu', beta_loss='kullback-leibler')  
W = model.fit_transform(Pwgd)  
H = sps.csr_matrix(model.components_)  
# column normalized versions  
H = sps.diags(W.sum(axis=0).flatten())*H # Ptgd  
W = W/W.sum(axis=0).flatten() # Pwgt  
# community assignment C  
C = sps.csr_matrix(np.transpose(H/H.sum(axis=0).flatten()))
```

wisely initialize
for best
performance

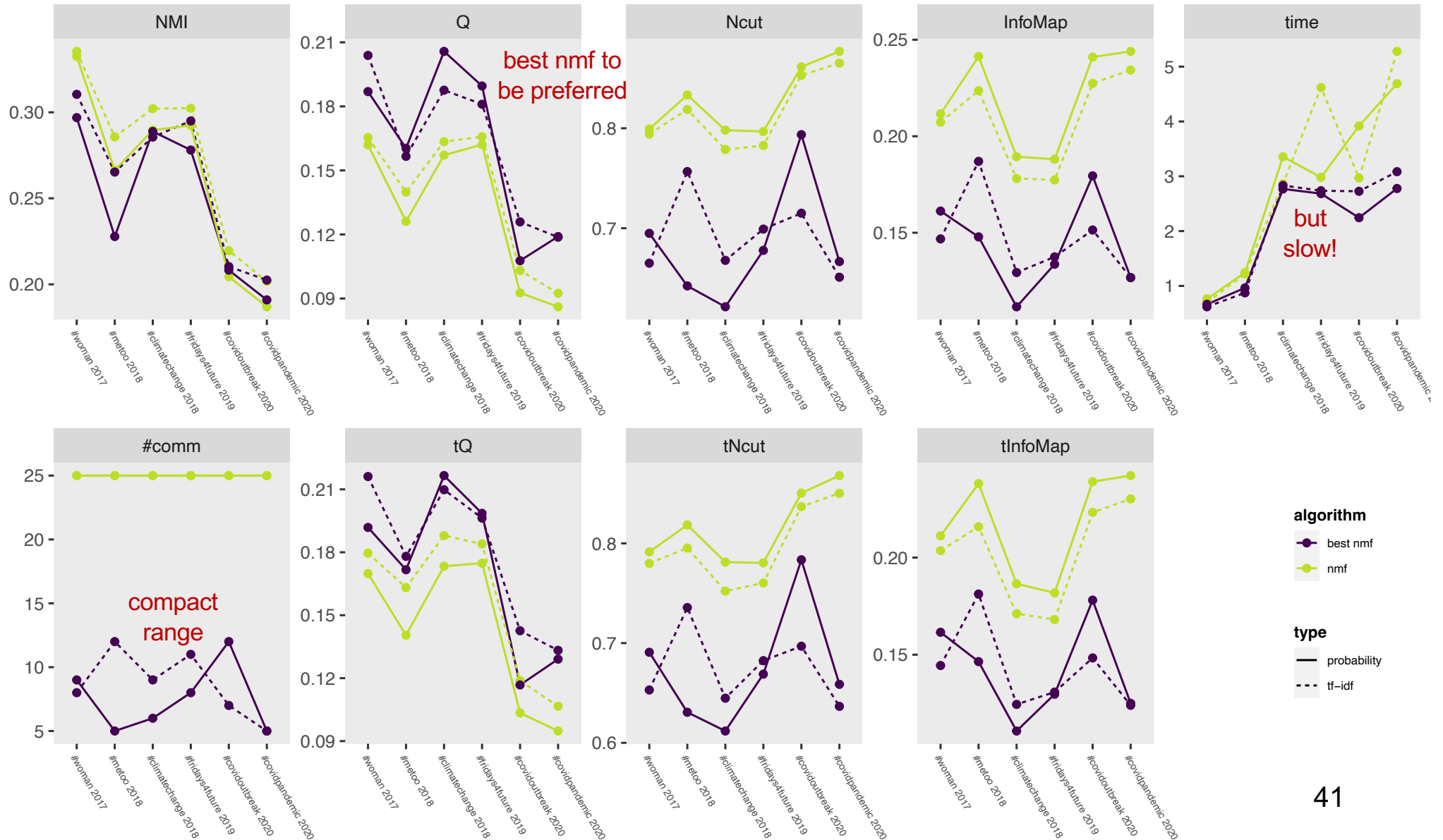
choose generalized
Kullback-Leibler
divergence, and the
related solver

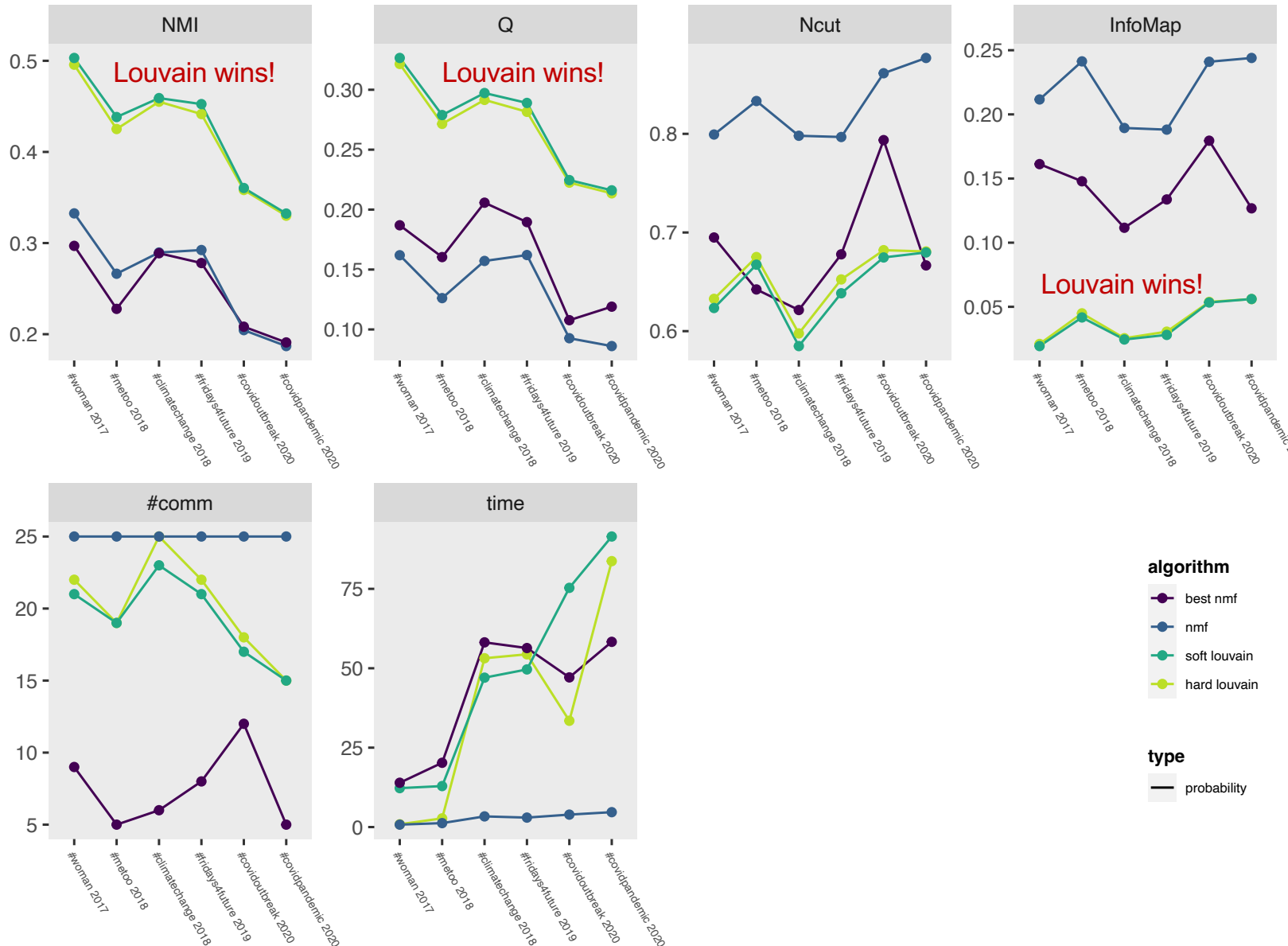
need to make W
column stochastic,
to have H column
stochastic too

force column stochasticity in H (not needed though)



A comparison of the different approaches



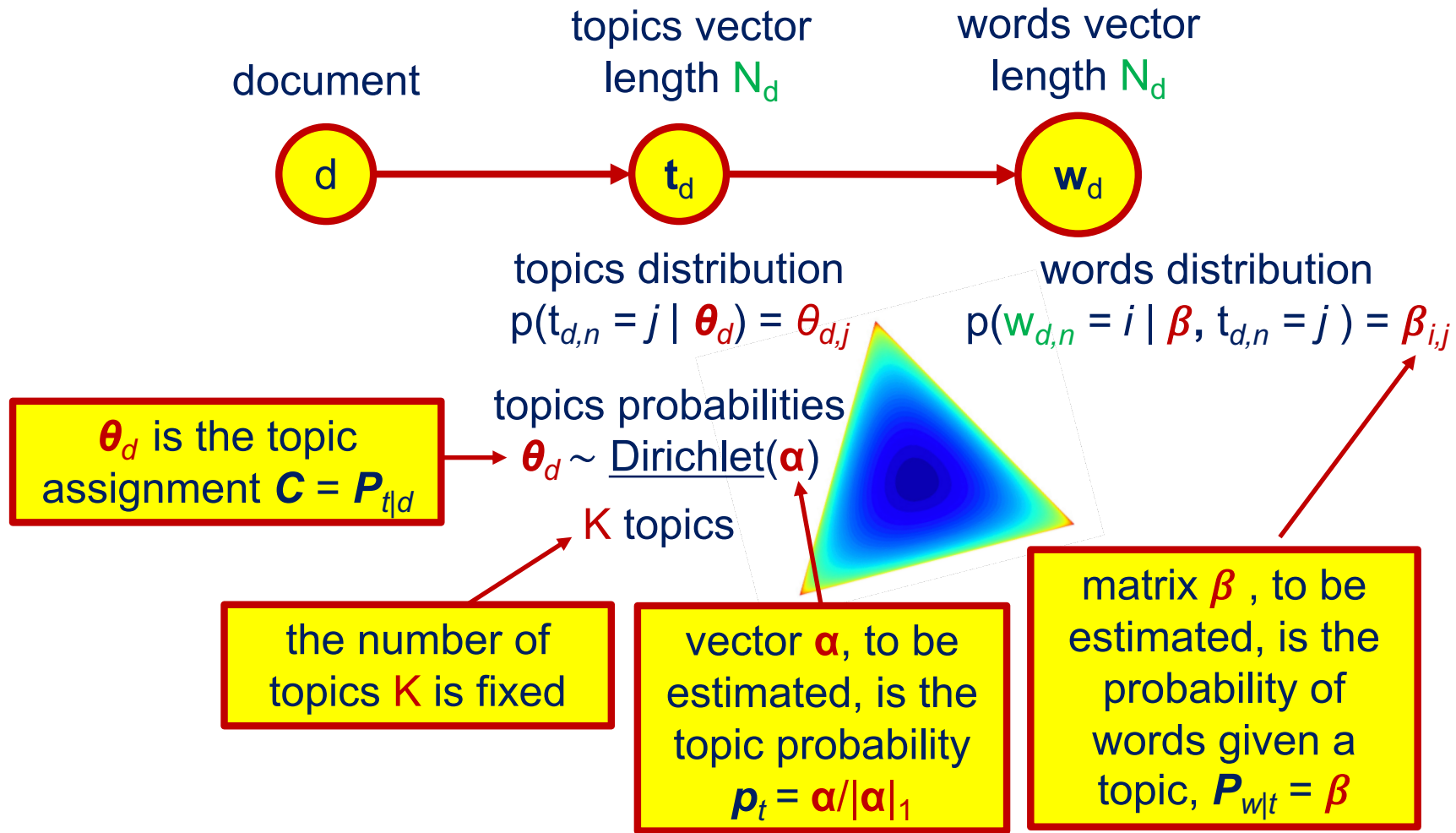




- ❑ Naturally provides a soft topic assignment
- ❑ NMF – not strikingly good
 - probably due to the fact that we want to express a sparse matrix through an eigenvector-like product with few eigenvectors (the fit is far from ideal)
- ❑ Comparison – with Louvain
 - much weaker
- ❑ Complexity – generally slow
 - need to test it for different numbers of topics ☹
 - fast for fixed topic number

Latent Dirichlet allocation

LDA = a stochastic model for topic detection





topics assignment probability (Dirichlet)

$$p(\boldsymbol{\theta}_d | \boldsymbol{\alpha}) = \frac{\Gamma(\sum_{k=1}^K \alpha_k)}{\prod_{k=1}^K \Gamma(\alpha_k)} \prod_{k=1}^K [\theta_{d,k}]^{\alpha_k - 1}$$

words probability

$$p(\mathbf{w}_d | \boldsymbol{\beta}, \boldsymbol{\theta}_d) = \prod_{n=1}^{N_d} [\boldsymbol{\beta} \boldsymbol{\theta}_d]_{w_{d,n}}$$

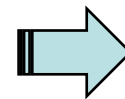
this dependence
between $\boldsymbol{\beta}$ and $\boldsymbol{\theta}$
is the trickiest part

overall probability

$$p(\text{corpus} | \boldsymbol{\alpha}, \boldsymbol{\beta}) = \prod_d \int p(\mathbf{w}_d | \boldsymbol{\beta}, \boldsymbol{\theta}_d) p(\boldsymbol{\theta}_d | \boldsymbol{\alpha}) d\boldsymbol{\theta}_d$$

target optimization

$$\operatorname{argmax}_{\boldsymbol{\alpha}, \boldsymbol{\beta}} p(\text{corpus} | \boldsymbol{\alpha}, \boldsymbol{\beta})$$



$$\mathbf{C} = \mathbf{P}_{t|d} = \boldsymbol{\theta}$$
$$\mathbf{P}_{wt} = \boldsymbol{\beta} \operatorname{diag}(\boldsymbol{\alpha} / |\boldsymbol{\alpha}|_1)$$

this is what we get



```
from sklearn.decomposition import LatentDirichletAllocation
```

```
# fit lda model
```

```
lda = LatentDirichletAllocation(n_components=i,  
                               learning_method="batch")
```

```
lda.fit(Mwd.T)
```

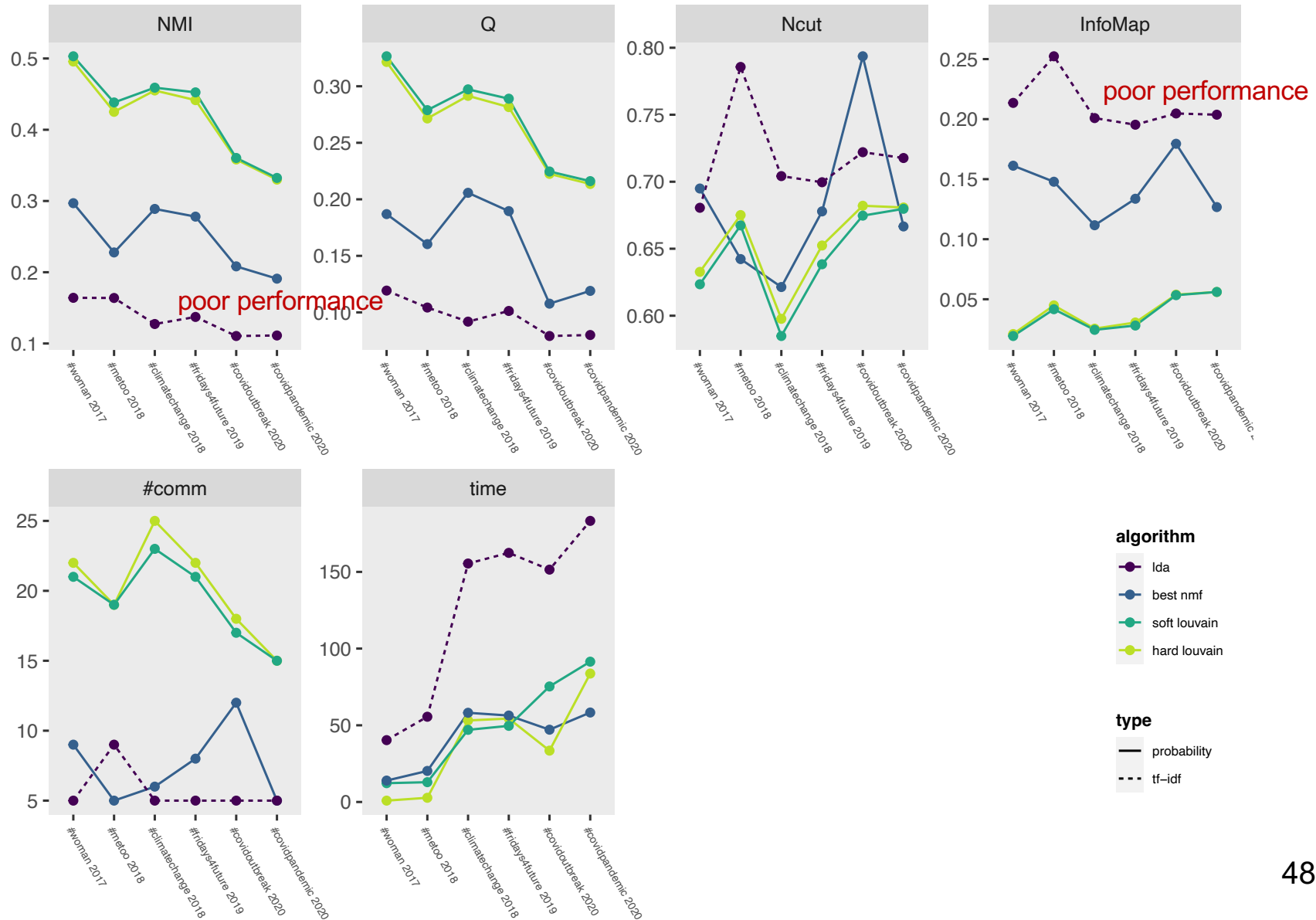
```
# community assignment C = Ptgd'
```

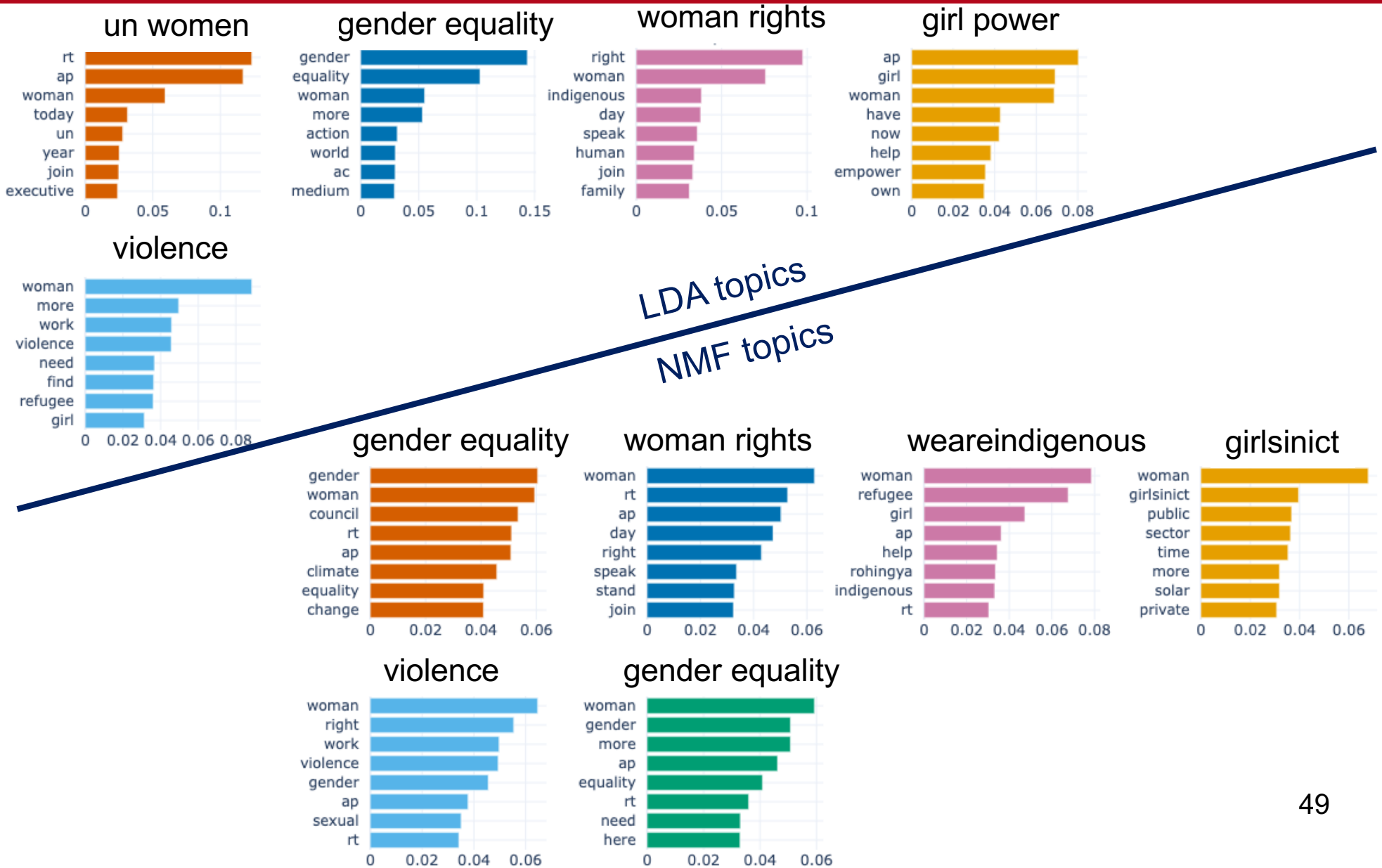
```
C = sps.csr_matrix(lda.transform(Mwd.T))
```

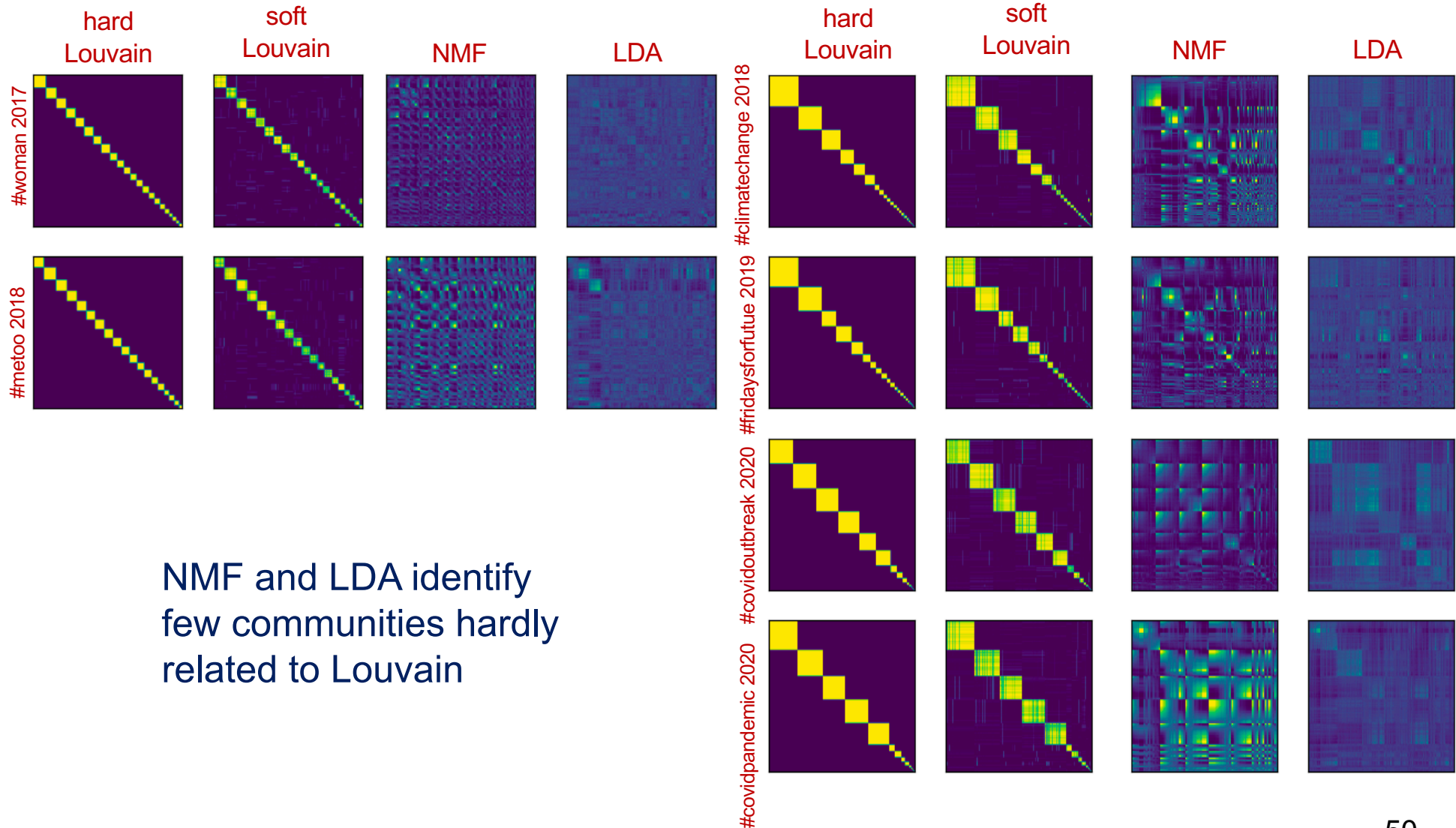
← initialise and fit model

← extract topic assignment

LDA







NMF and LDA identify
few communities hardly
related to Louvain



- ❑ Naturally provides a soft topic assignment
- ❑ LDA – not strikingly good
 - same eigenvector-like product as NMF
 - worse than NMF ... known issue ☹️
 - probably due to the **Dirichlet** assumption (questionable)
 - and the **variational inference** (suboptimum approach)
- ❑ Comparison – with Louvain
 - much weaker
- ❑ Complexity – generally slow
 - need to test it for different numbers of topics ☹️
 - fast for fixed topic number

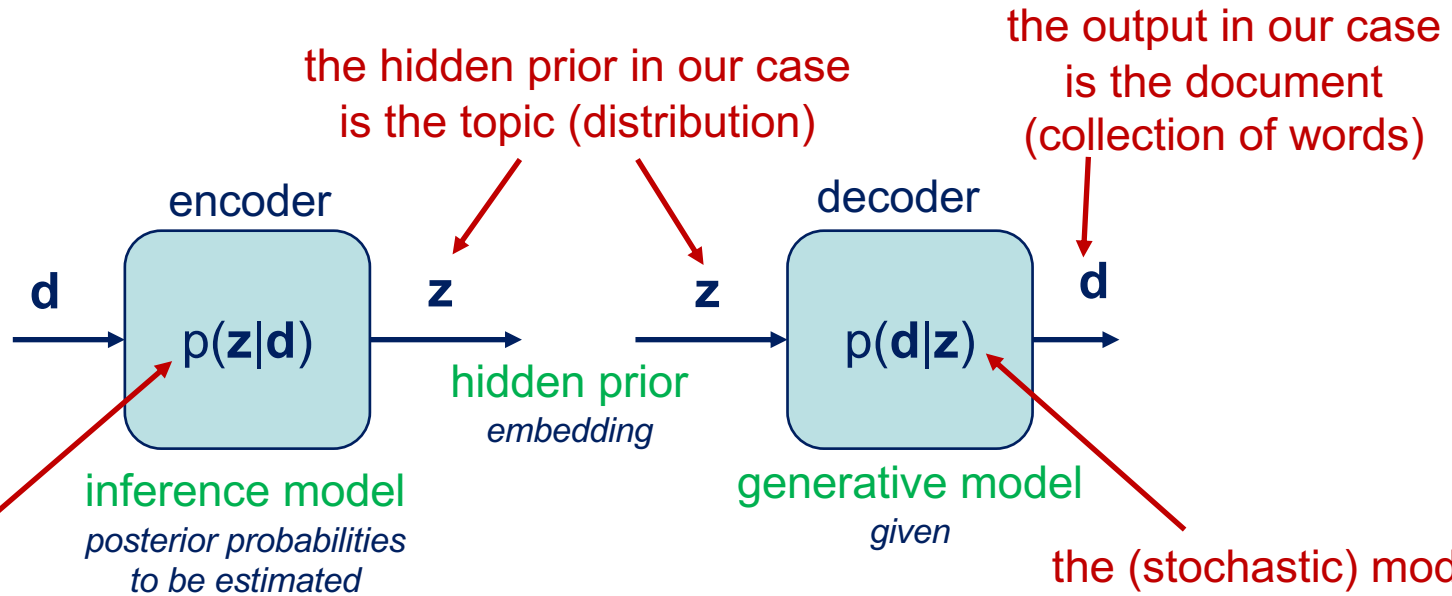
Variational Auto Encoders

an application to topic analysis



Variational Auto-Encoders

Kingma, Welling, "Auto-encoding variational Bayes," (2013)



but we are interested in the inverse link that, given a document tells what topic it is associated with

the (stochastic) model explains how a document is generated from a topic (distribution)

$$p(z|d) = \frac{p(d|z) p(z)}{p(d)} \cong q(z|d)$$

impossible to know in the closed form

needs an a-priori model for the embedding

is approximated by a simple alternative model

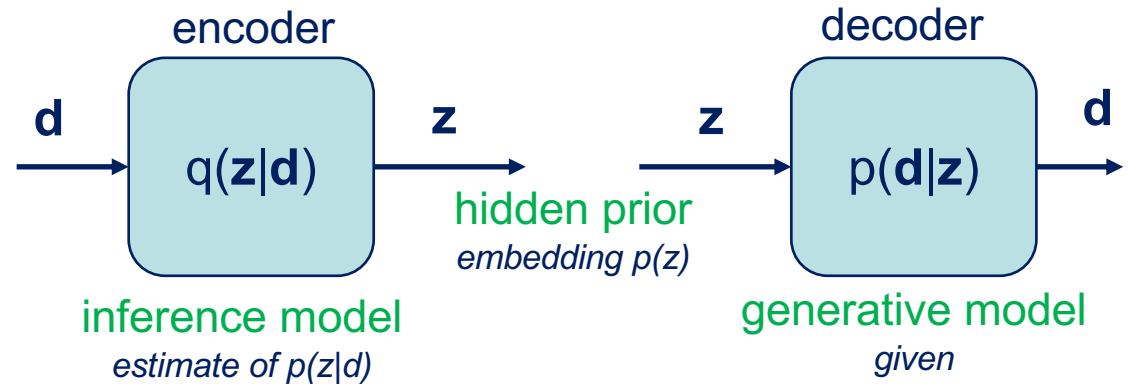


VAE optimization rationale

ELBO = evidence lower bound

ELBO

$$\mathcal{L}_{\theta, \phi}(\mathbf{d}) \leq \log p_{\theta}(\mathbf{d})$$



$$\mathcal{L}_{\theta, \phi}(\mathbf{d}) = \log p_{\theta}(\mathbf{d}) - D_{\text{KL}}\left(q_{\phi}(z|\mathbf{d}) \parallel p_{\theta}(z|\mathbf{d})\right)$$

$$= \int dz q_{\phi}(z|\mathbf{d}) \log \left(\frac{p_{\theta}(z, \mathbf{d})}{q_{\phi}(z|\mathbf{d})} \right)$$

$$= \underbrace{\int dz q_{\phi}(z|\mathbf{d}) \log \left(p_{\theta}(\mathbf{d}|z) \right)}_{\mathcal{L}_1} + \underbrace{\int dz q_{\phi}(z|\mathbf{d}) \log \left(\frac{p_{\theta}(z)}{q_{\phi}(z|\mathbf{d})} \right)}_{\mathcal{L}_2}$$

inference model
(approximate)

generative model
(given)

to be maximized wrt
parameters θ and ϕ
provides fitting on $p(\mathbf{z})$,
 $p(\mathbf{d}|\mathbf{z})$, and $q(\mathbf{z}|\mathbf{d})$

a-priori model
(given)



$$\underbrace{\int dz q_{\phi}(z|\mathbf{d}) \log \left(\frac{p_{\theta}(z)}{q_{\phi}(z|\mathbf{d})} \right)}_{\mathcal{L}_2}$$

both should have a simple parametrization on θ and ϕ

e.g., the Gaussian case

$$p_{\theta}(\mathbf{z}) = \frac{1}{\sqrt{\det(2\pi \text{diag}(\boldsymbol{\sigma}_{\theta}^2))}} \exp\left(-\frac{1}{2}(\mathbf{z} - \boldsymbol{\mu}_{\theta})^T \text{diag}^{-1}(\boldsymbol{\sigma}_{\theta}^2)(\mathbf{z} - \boldsymbol{\mu}_{\theta})\right)$$

$$q_{\phi}(\mathbf{z}|\mathbf{d}) = \frac{1}{\sqrt{\det(2\pi \text{diag}(\boldsymbol{\sigma}_{\phi}^2(\mathbf{d})))}} \exp\left(-\frac{1}{2}(\mathbf{z} - \boldsymbol{\mu}_{\phi}(\mathbf{d}))^T \text{diag}^{-1}(\boldsymbol{\sigma}_{\phi}^2(\mathbf{d}))(\mathbf{z} - \boldsymbol{\mu}_{\phi}(\mathbf{d}))\right)$$

$$\mathcal{L}_2(\theta, \phi) = \frac{1}{2} \sum_i \left[1 + \log\left(\frac{\sigma_{\phi,i}^2(\mathbf{d})}{\sigma_{\theta,i}^2}\right) - \frac{\sigma_{\phi,i}^2(\mathbf{d})}{\sigma_{\theta,i}^2} - \frac{(\mu_{\phi,i}(\mathbf{d}) - \mu_{\theta,i})^2}{\sigma_{\theta,i}^2} \right]$$



L1 ELBO function

approximated through Monte Carlo estimation

$$\underbrace{\int dz q_\phi(z|\mathbf{d}) \log(p_\theta(\mathbf{d}|z))}_{\mathcal{L}_1}$$

mostly too complex to be written in the closed form

solution: Monte Carlo approximation

$$\mathcal{L}_1(\theta, \phi) = \frac{1}{L} \sum_{\ell=1}^L \log(p_\theta(\mathbf{d}|\mathbf{z}_\ell))$$

samples generated according to the correct distribution

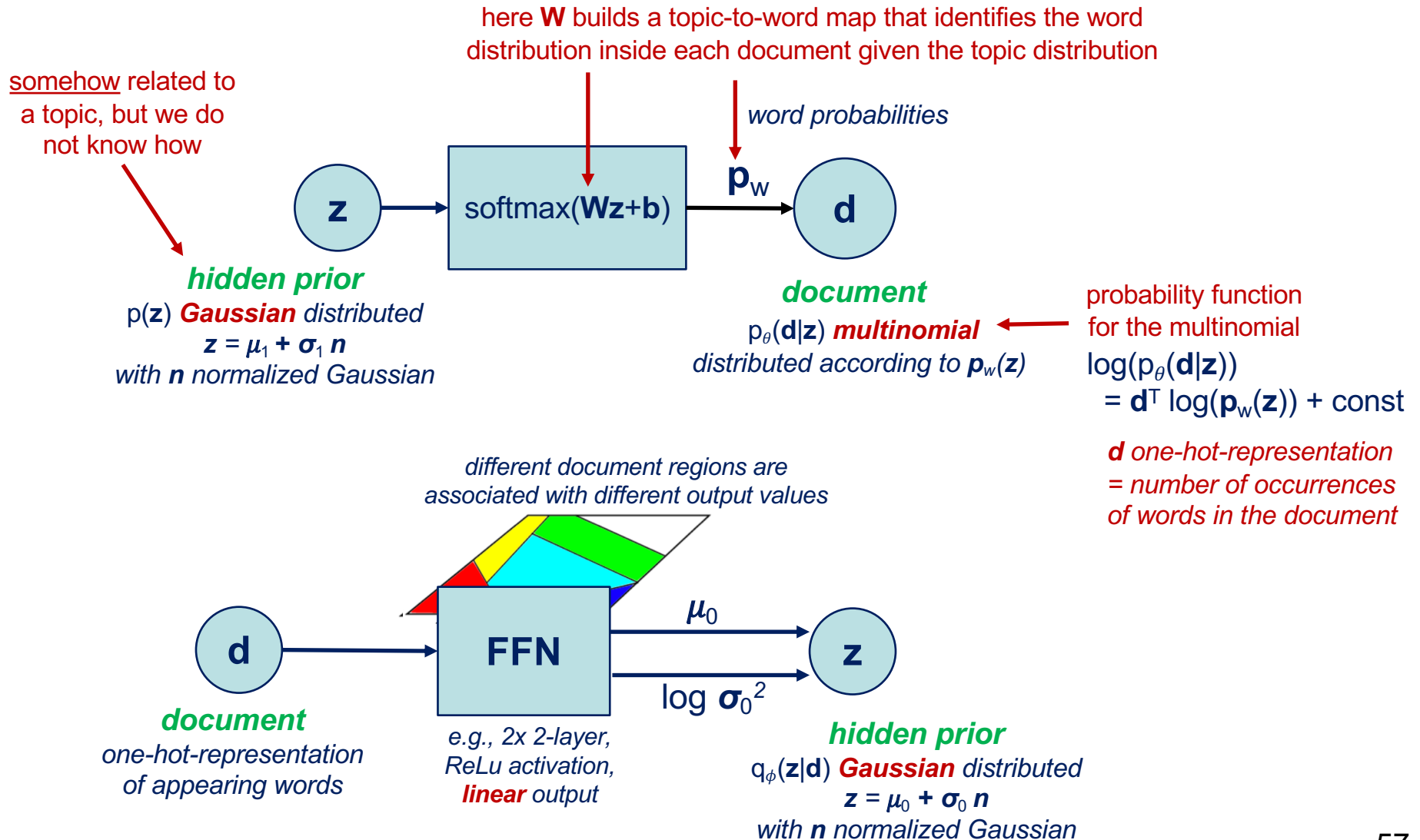
$$\mathbf{z}_\ell \sim q_\phi(\mathbf{z}|\mathbf{d})$$

e.g., the Gaussian case

$$\mathbf{z}_\ell = \boldsymbol{\mu}_\phi(\mathbf{d}) + \boldsymbol{\sigma}_\phi(\mathbf{d}) \mathbf{n}_\ell$$

need to generate these once, then use them throughout the process

$$\mathbf{n}_\ell \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$





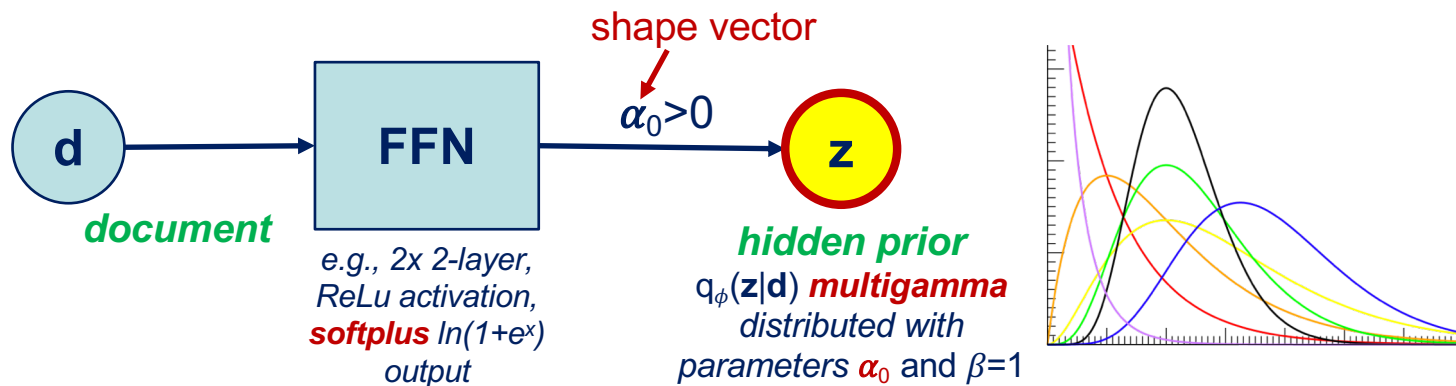
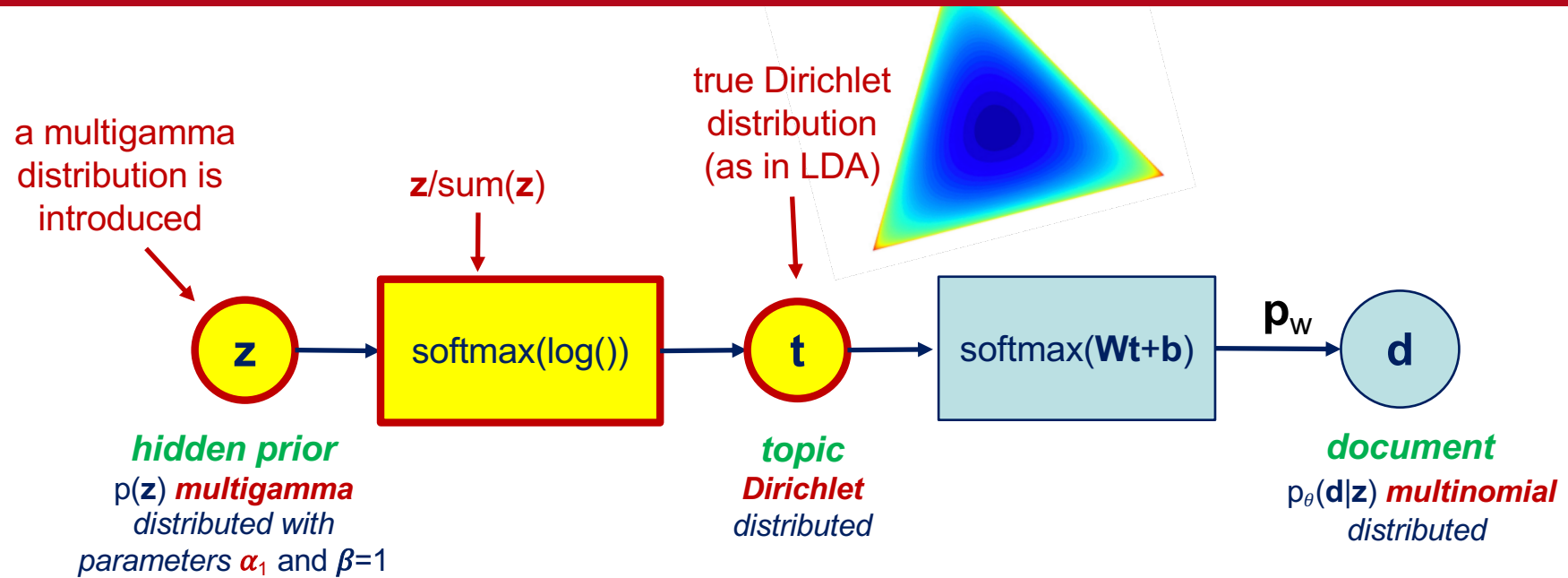
one-hot-representation of a document = number of occurrences of words in the document

$$\mathcal{L}(\theta, \phi) = \frac{1}{L} \sum_{\ell=1}^L \sum_m \mathbf{d}_m^T \log \left(\underbrace{\text{softmax}(\mathbf{b} + \mathbf{W}(\boldsymbol{\mu}_0(\mathbf{d}_m) + \boldsymbol{\sigma}_0(\mathbf{d}_m) \mathbf{n}_{m,\ell}))}_{\text{decoder map}} \right)$$

$$+ \frac{1}{2} \sum_m \sum_i 1 + \log \left(\frac{\sigma_{0,i}^2(\mathbf{d}_m)}{\sigma_{1,i}^2} \right) - \frac{\sigma_{0,i}^2(\mathbf{d}_m)}{\sigma_{1,i}^2} - \frac{(\mu_{0,i}(\mathbf{d}_m) - \mu_{1,i})^2}{\sigma_{1,i}^2}$$

a-priori model

Not very clear where the topic is, though!





one-hot-representation of a document = number of occurrences of words in the document

$$\mathcal{L}(\theta, \phi) = \frac{1}{L} \sum_{\ell=1}^L \sum_m \mathbf{d}_m^T \log \left(\underbrace{\text{softmax}(\mathbf{b} + \mathbf{W} \text{softmaxlog}(\mathbf{f}(\mathbf{u}_{m,\ell}, \boldsymbol{\alpha}_0(\mathbf{d}_m))))}_{\text{decoder map}} \right)$$

$$f(\mathbf{u}, \boldsymbol{\alpha}) = (\mathbf{u} \boldsymbol{\alpha} \Gamma(\boldsymbol{\alpha}_1))^{1/\alpha}$$

approx. uniform to multigamma map

normalized uniform samples

decoder model

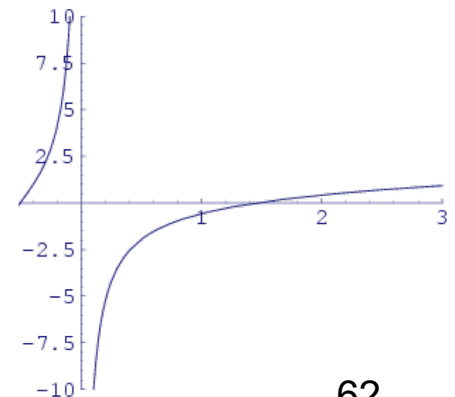
encoder model

$$+ \sum_m \sum_i \log \left(\frac{\Gamma(\alpha_{0,i}(\mathbf{d}_m))}{\Gamma(\alpha_{1,i})} \right) - (\alpha_{0,i}(\mathbf{d}_m) - \alpha_{1,i}) \psi(\alpha_{0,i}(\mathbf{d}_m))$$

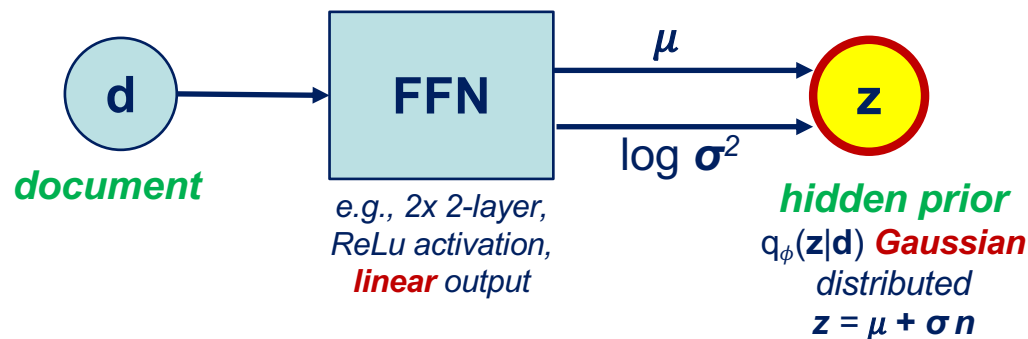
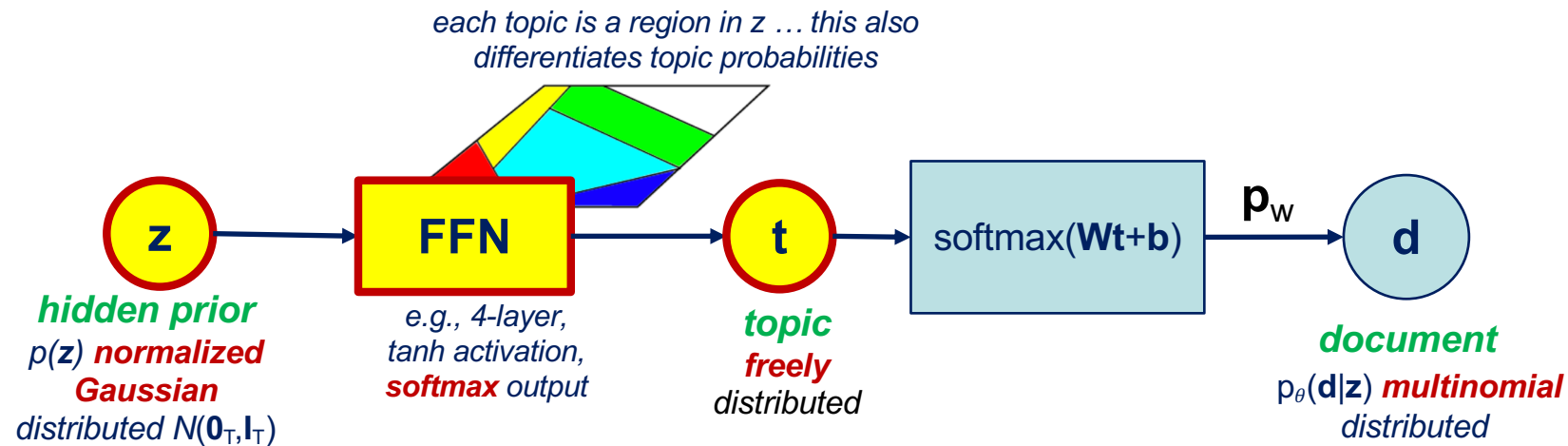
a-priori model

digamma function

$$\psi(x) = \frac{\Gamma'(x)}{\Gamma(x)}$$



Now we know where the topic is!



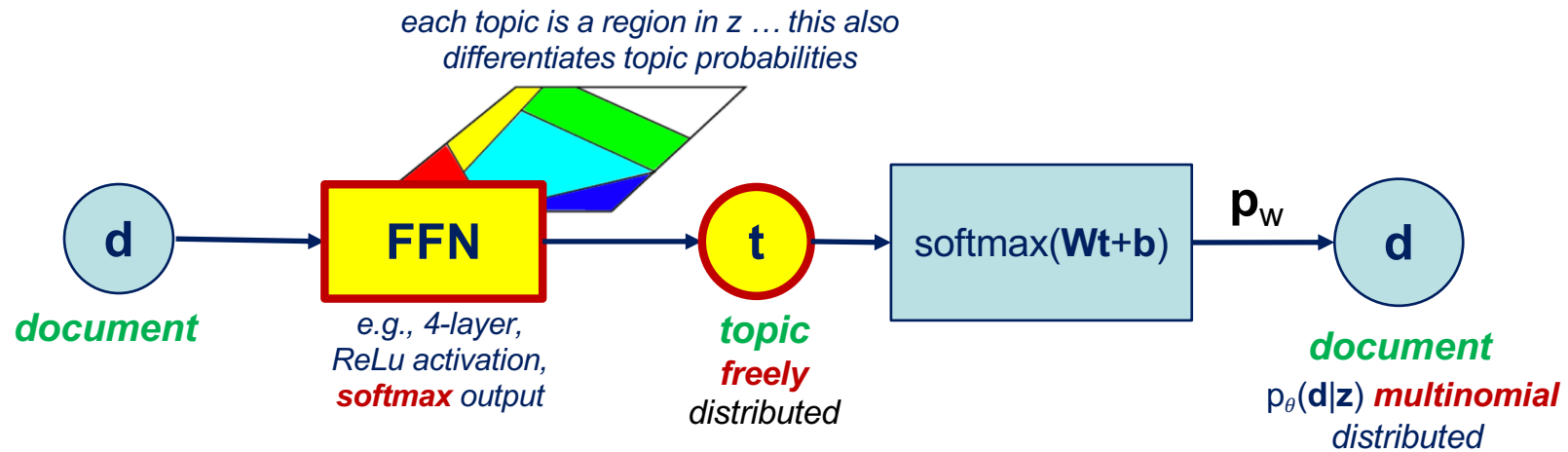


one-hot-representation of a document = number of occurrences of words in the document

$$\mathcal{L}(\theta, \phi) = \frac{1}{L} \sum_{\ell=1}^L \sum_m \mathbf{d}_m^T \log \left(\underbrace{\text{softmax}(\mathbf{b} + \mathbf{W} \text{FFN}_1)}_{\text{decoder map}}(\underbrace{\mu_0(\mathbf{d}_m) + \sigma_0(\mathbf{d}_m) \mathbf{n}_{m,\ell}}_{\text{normalized Gaussian samples}})) \right) + \frac{1}{2} \sum_m \sum_i 1 + \log(\sigma_{0,i}^2(\mathbf{d}_m)) - \sigma_{0,i}^2(\mathbf{d}_m) - (\mu_{0,i}(\mathbf{d}_m))^2$$

Our estimate of the **topic distribution** for the m th document!

$$\mathbf{c}_m = \frac{1}{L} \sum_{\ell=1}^L \text{FFN}_1(\mu_0(\mathbf{d}_m) + \sigma_0(\mathbf{d}_m) \mathbf{n}_{m,\ell})$$



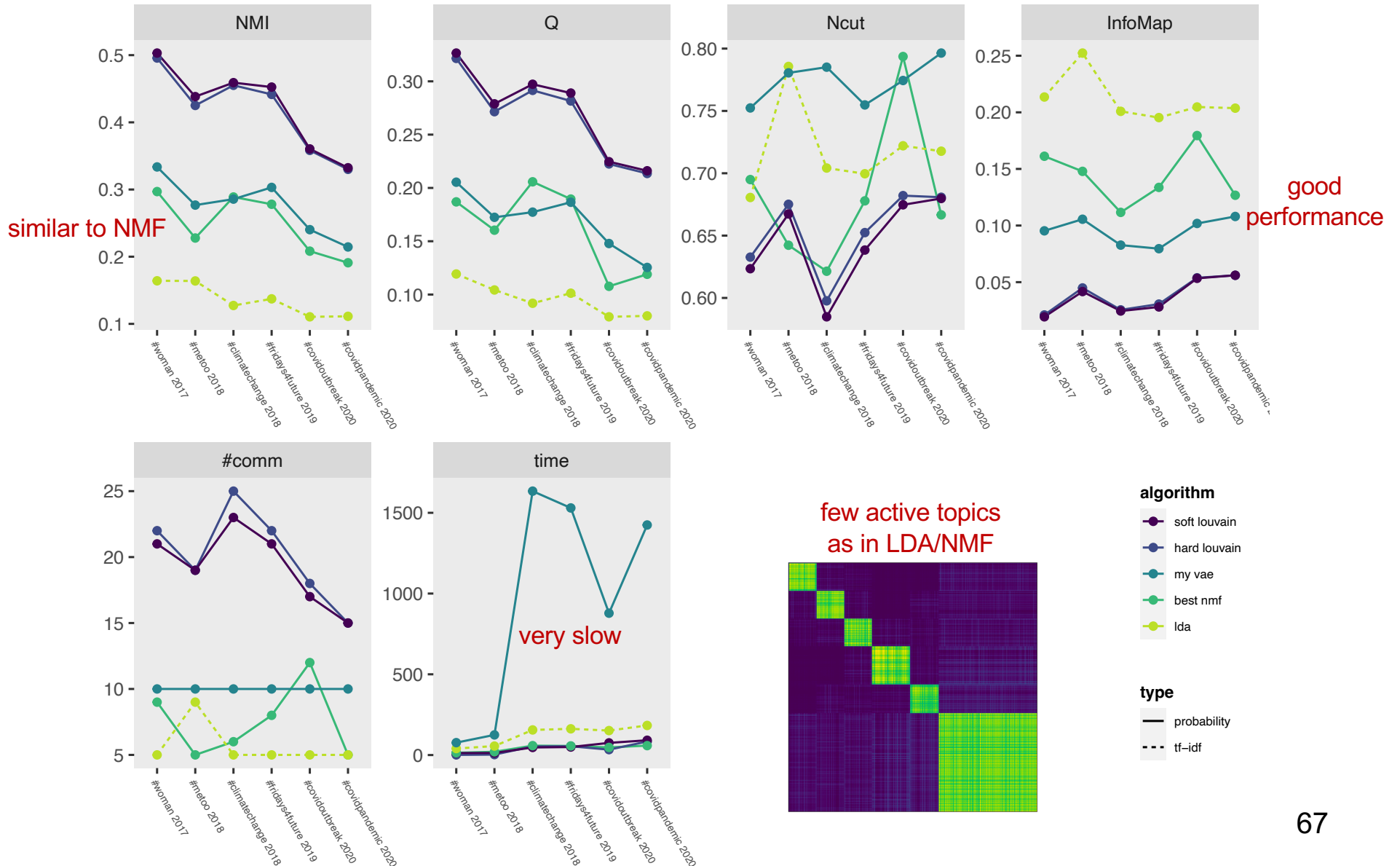
one-hot-representation of a document = number of occurrences of words in the document

decoder model encoder model

$$\mathcal{L}(\theta, \phi) = \sum_m \mathbf{d}_m^T \log(\text{softmax}(\mathbf{b} + \mathbf{W} \text{FFN}(\mathbf{d}_m)))$$



A comparison with NMF, LDA, and Louvain





- ❑ Naturally provides a soft topic assignment
- ❑ VAE – interesting approach
 - more flexible model than NMF or LDA
 - gives improvements
- ❑ Comparison – with Louvain
 - still far away
 - would be nice to see other **Deep Learning** approaches
 - ... your task! 😊

Transformer Architecture

with application to BERT, RoBERTa, OpenAI GPT



☰ Attention (machine learning)

Article [Talk](#)

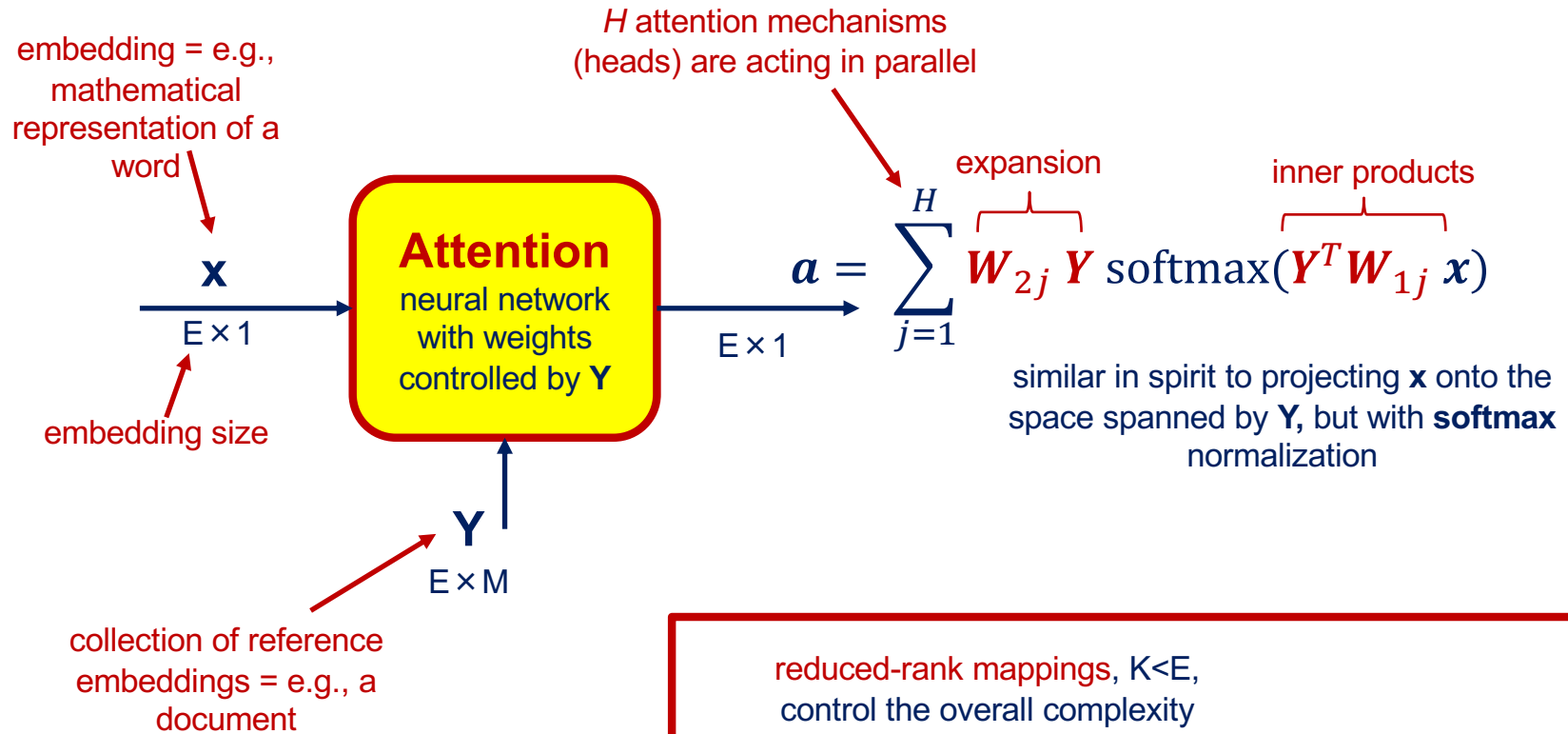
From Wikipedia, the free encyclopedia

In [artificial neural networks](#), **attention** is a technique that is meant to mimic [cognitive attention](#). This effect **enhances** some **parts of the input data while diminishing other parts** — the motivation being that the network should devote more focus to the important parts of the data, even though they may be small portion of an image or sentence. Learning which part of the data is more important than another depends on the context, and this is trained by [gradient descent](#).



The Attention Module

Vaswani, Ashish, et al. "Attention is all you need" (2017)



reduced-rank mappings, $K < E$, control the overall complexity

$$\mathbf{W}_{ij} = \mathbf{V}_{ij} \mathbf{U}_{ij}$$

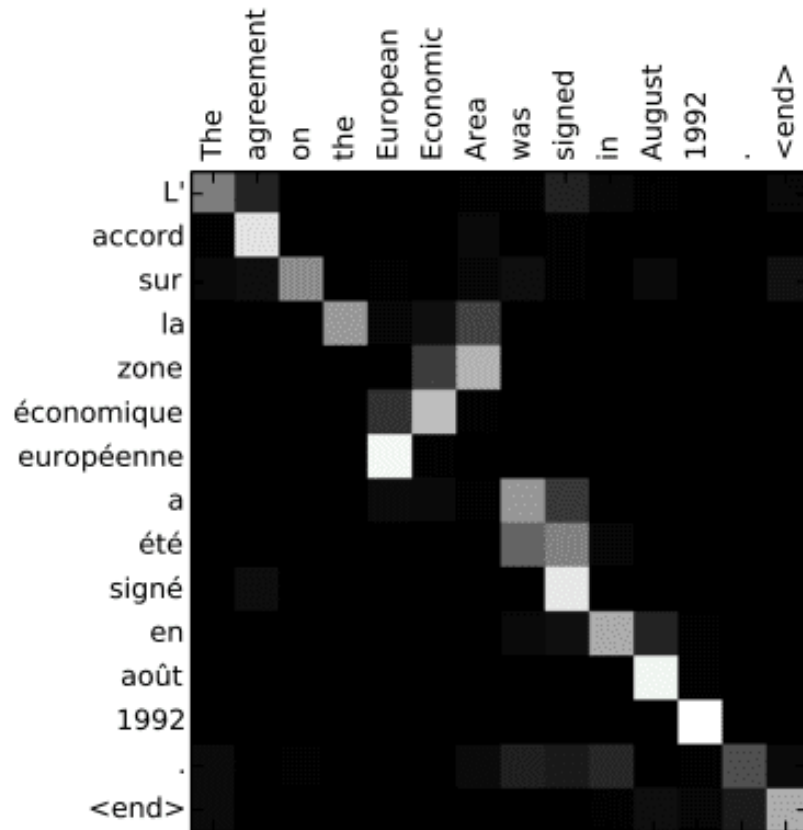
$E \times E$ $E \times K$ $K \times E$

overall complexity $4EKH$

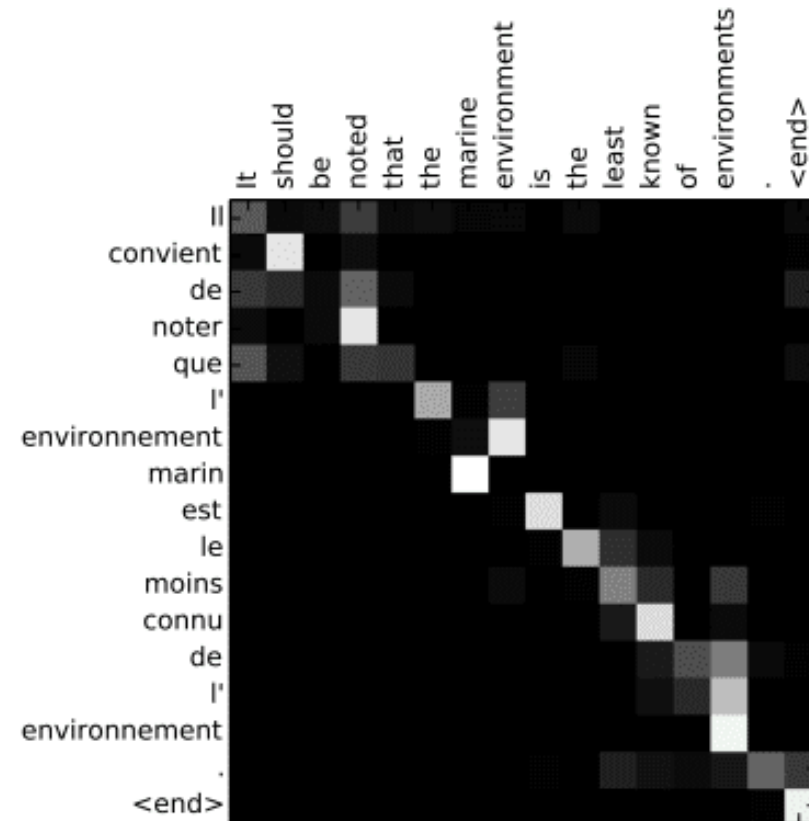


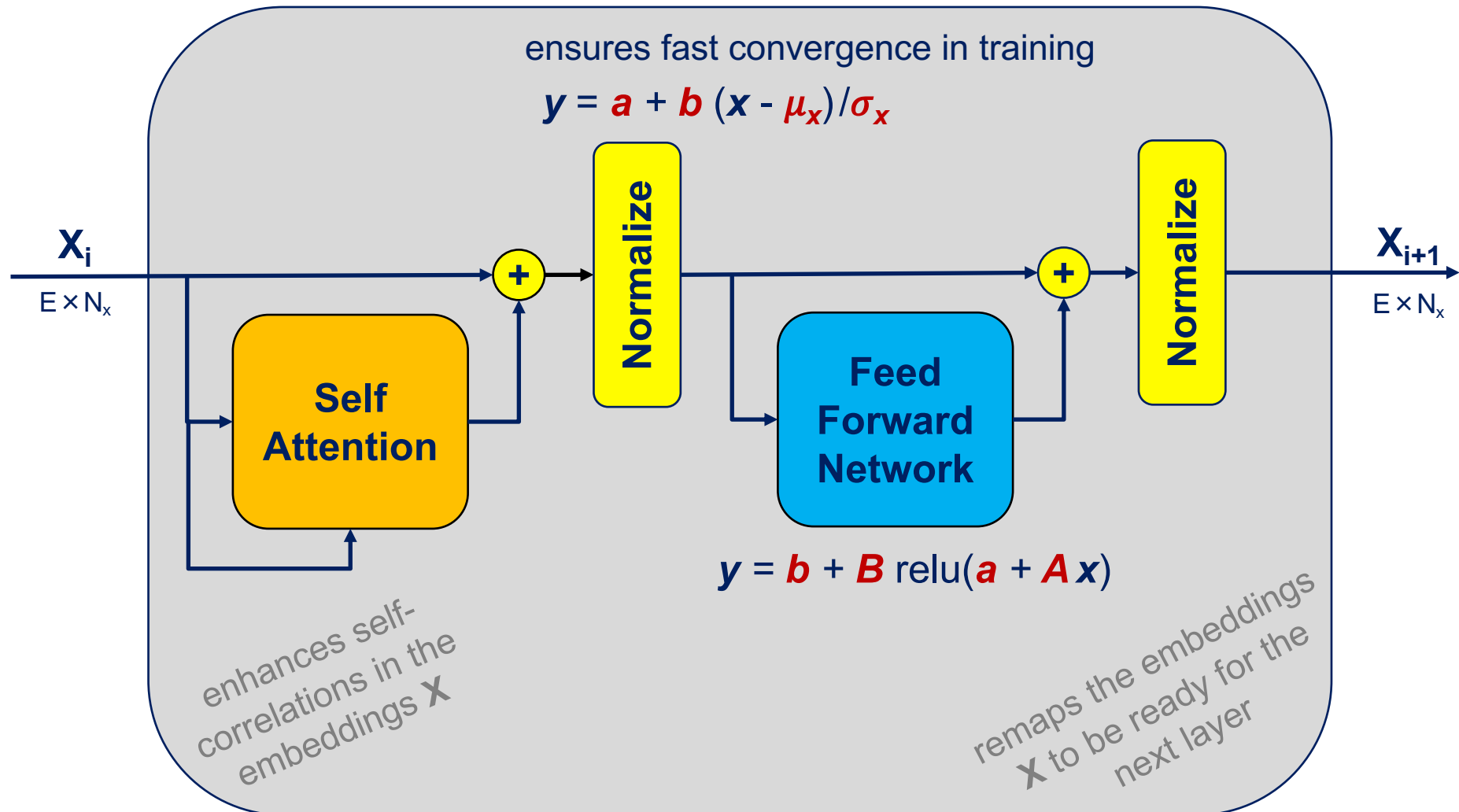
Visualizing Attention

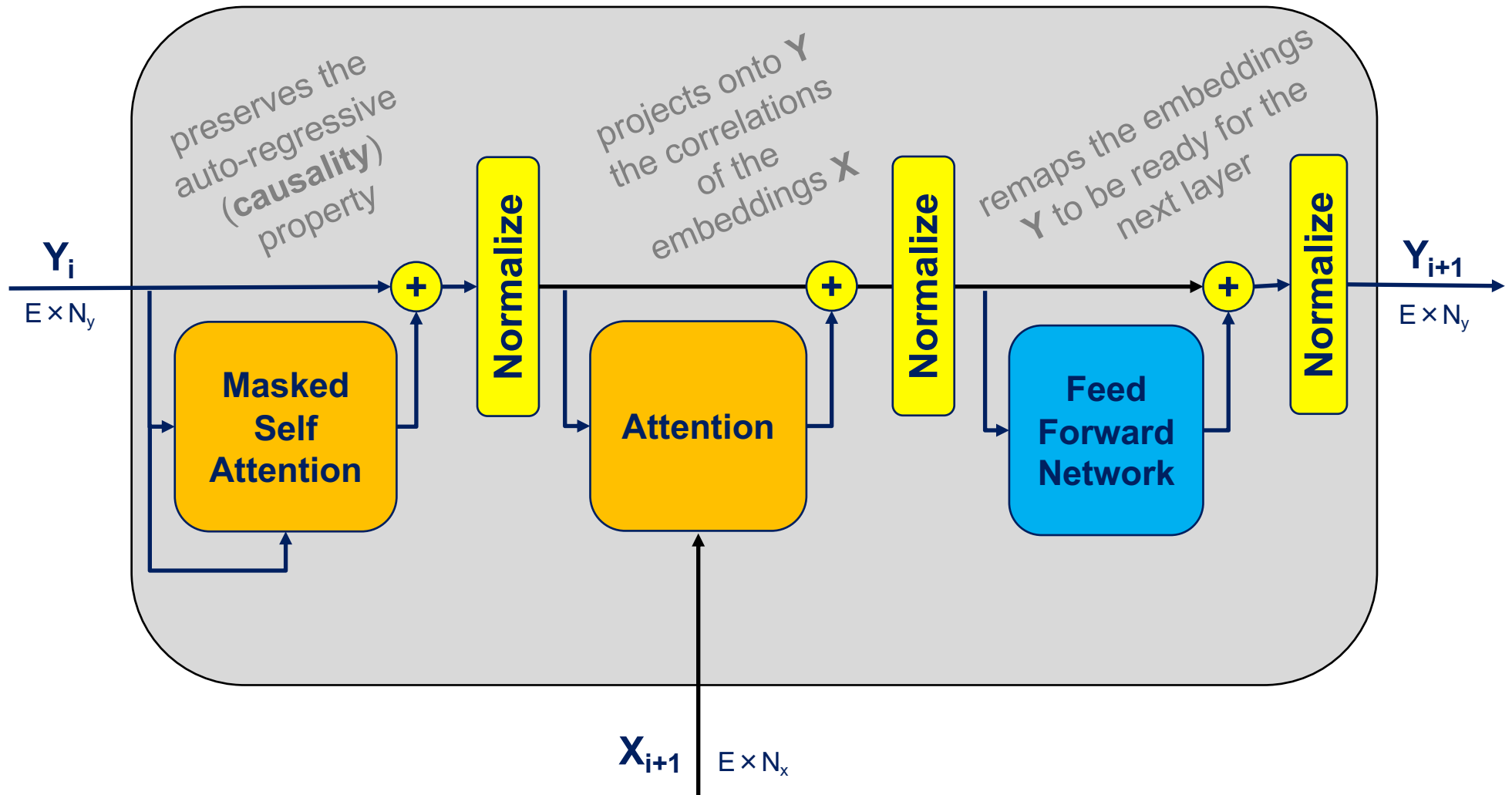
in a translation experiment (X English, Y French)



$$\text{softmax}(Y^T W_{1j} X)$$



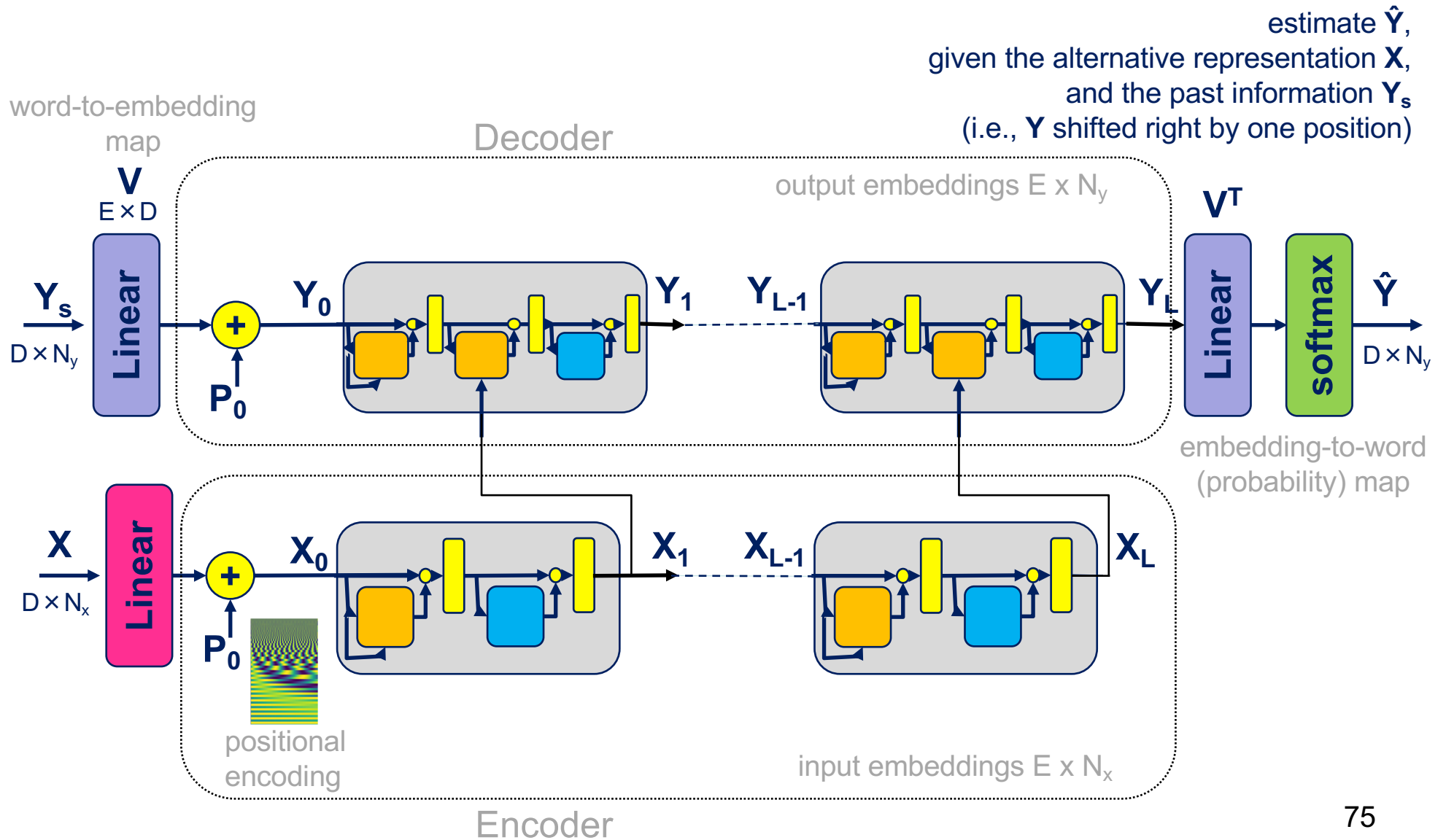






Transformer Architecture

Vaswani, Ashish, et al. "Attention is all you need" (2017)
Google's patent <https://patents.google.com/patent/US10452978B2/en>





The Annotated Transformer

Apr 3, 2018

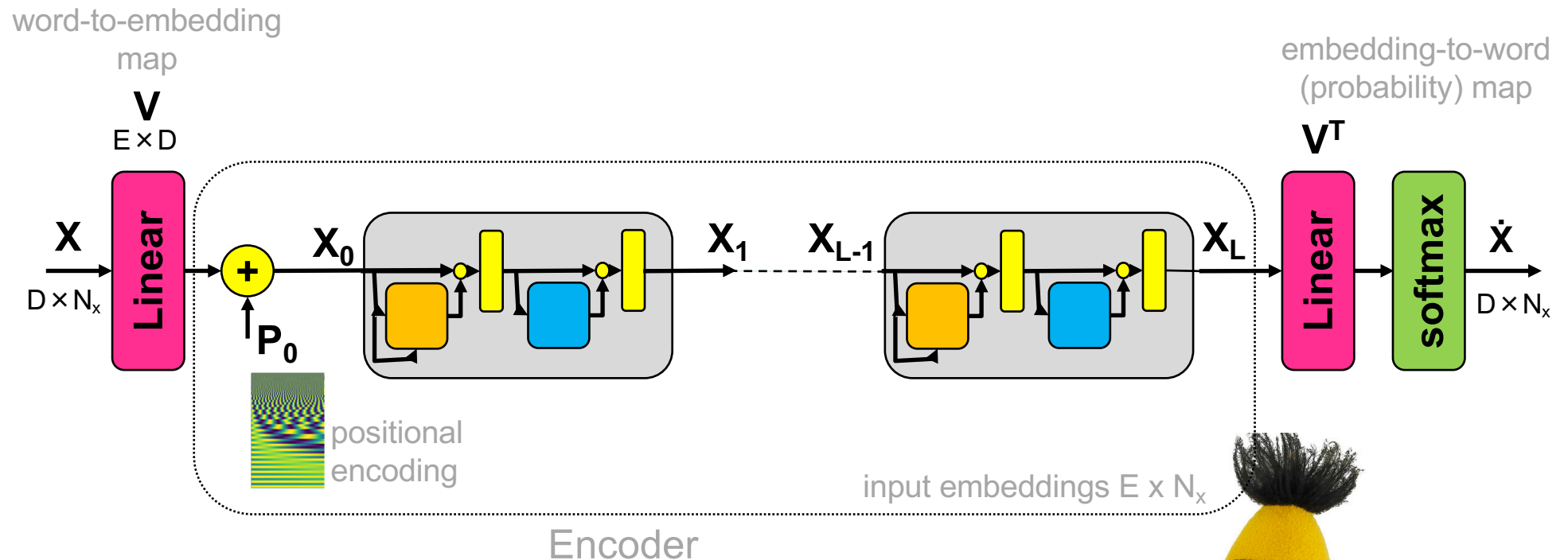
There is now a [new version](#) of this blog post updated for modern PyTorch.

```
from IPython.display import Image  
Image(filename='images/aiayn.png')
```

Attention Is All You Need



<https://github.com/google-research/bert>





BERT parameters

	Embeddings size E	Self-attention heads H	Head dimension K = E/H	FFN inner size I = 4E	Parameters per layer $12E^2+9E$	Layers L	Dictionary size D	Total parameters
BERT base	768	12	64	3072	7.1M	12	30.5K	110M
BERT large	1024	16	64	4096	12.6M	24	30.5K	340M



max tokens $N_x = 512$

Created by researchers at Google AI Language



BERT pre-training procedure

BooksCorpus (800M words) + English Wikipedia (2,500M words)

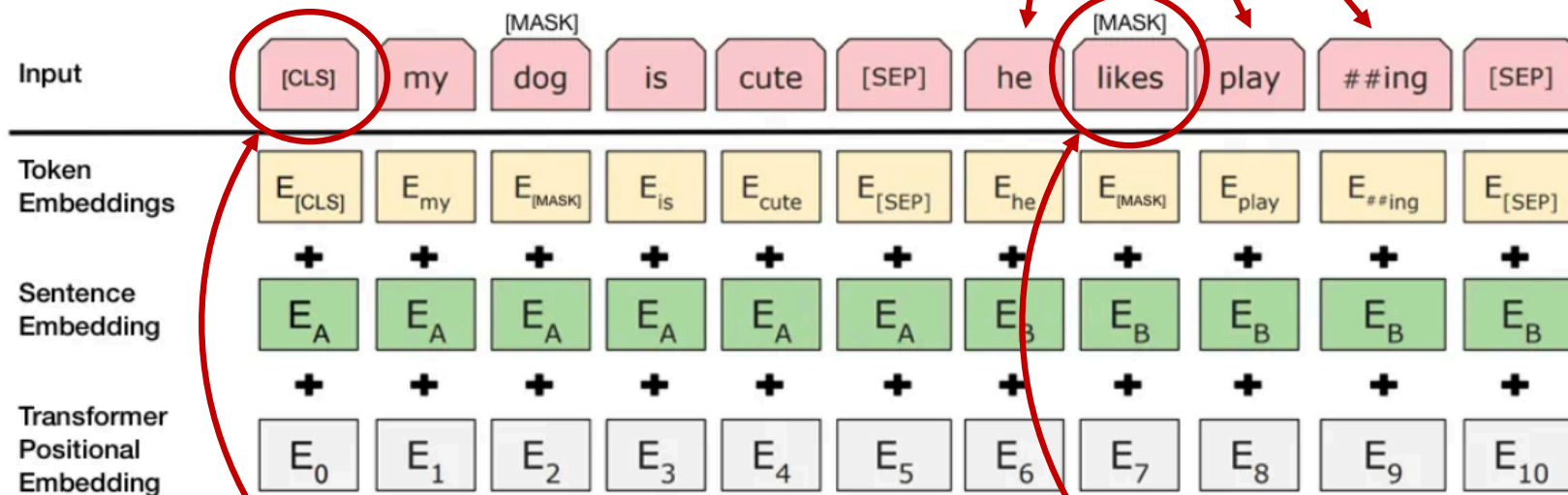
Masked Language Model

15% **masked tokens** replaced with:

- [MASK] token (80% of the times)
- Original token (10%)
- Random token (10%)

Next Sequence Prediction

- Next sequence (50% of the times)
- Random sequence (50%)



Output [CLS] fed into an additional output layer for softmax classification (of correct/wrong next sequence)

Output **masked tokens** fed into the output layer V^T and evaluated for probability of correct estimate



Larger training corpora (10x larger)

training on BookCorpus + Wikipedia and also CC-News, OpenWebText, Stories

Dynamic masking

training data was duplicated 10 times so that each sequence is masked in 10 different ways over the 40 epochs of training

Full-sentences without NSP loss

full sentences sampled contiguously from one or more documents, such that the total length is at most 512 tokens

Large mini-batches

A larger byte-level BPE (byte pair encoding) of 50K subword units

a hybrid between character- and word-level representations that allows handling the large vocabularies common in natural language corpora

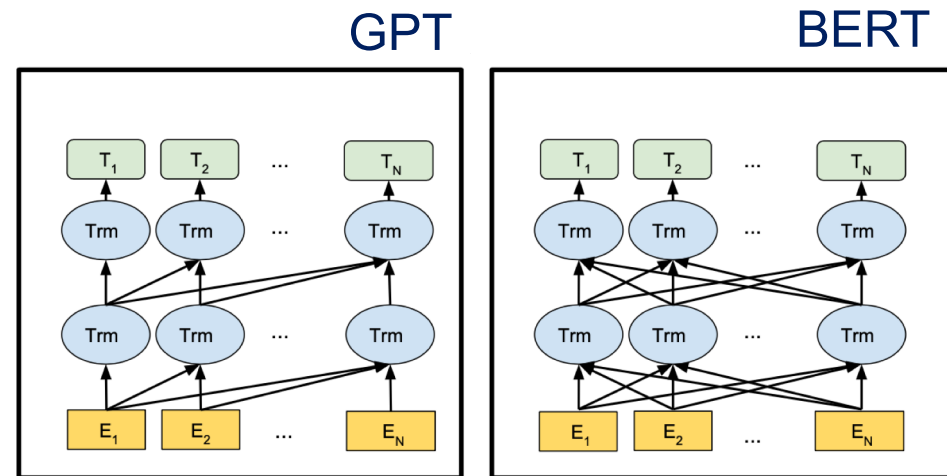
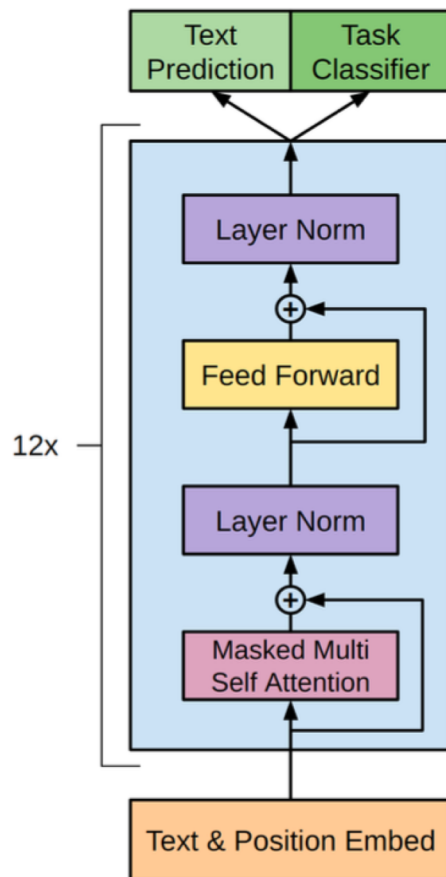


Generative Pre-Training (GPT)

Radford, Alec, et al. "Improving language understanding by generative pre-training." (2018)

(unsupervised) pre-training on **Language Modelling (no mask)**

$$L_1(\mathcal{U}) = \sum_i \log P(u_i | u_{i-k}, \dots, u_{i-1}; \Theta)$$



same parameters of BERT-base, but with **Masked Attention** trained on BookCorpus only



McCann et al. (2018)

language provides a flexible way to specify tasks, inputs, and outputs all as a sequence of symbols... it is therefore possible to **train a single model** with **sufficient capacity** to infer and perform many **different tasks**

model gets complex!



data gets larger!



Parameters	Layers	d_{model}	
117M	12	768	GPT, BERT-base
345M	24	1024	BERT-large
762M	36	1280	
1542M	48	1600	GPT-2

WebText

scraping all outbound links (45M links) from Reddit, a social media platform, which received at least 3 karma – exclude Wikipedia



increasingly larger data and model!

Model Name	n_{params}	n_{layers}	d_{model}	n_{heads}	d_{head}	Batch Size	Learning Rate
GPT-3 Small	125M	12	768	12	64	0.5M	6.0×10^{-4}
GPT-3 Medium	350M	24	1024	16	64	0.5M	3.0×10^{-4}
GPT-3 Large	760M	24	1536	16	96	0.5M	2.5×10^{-4}
GPT-3 XL	1.3B	24	2048	24	128	1M	2.0×10^{-4}
GPT-3 2.7B	2.7B	32	2560	32	80	1M	1.6×10^{-4}
GPT-3 6.7B	6.7B	32	4096	32	128	2M	1.2×10^{-4}
GPT-3 13B	13.0B	40	5140	40	128	2M	1.0×10^{-4}
GPT-3 175B or "GPT-3"	175.0B	96	12288	96	128	3.2M	0.6×10^{-4}

Layer normalization at the input (plus one at the output)

Sparse attention patterns

alternating dense and locally banded sparse attention patterns in the layers

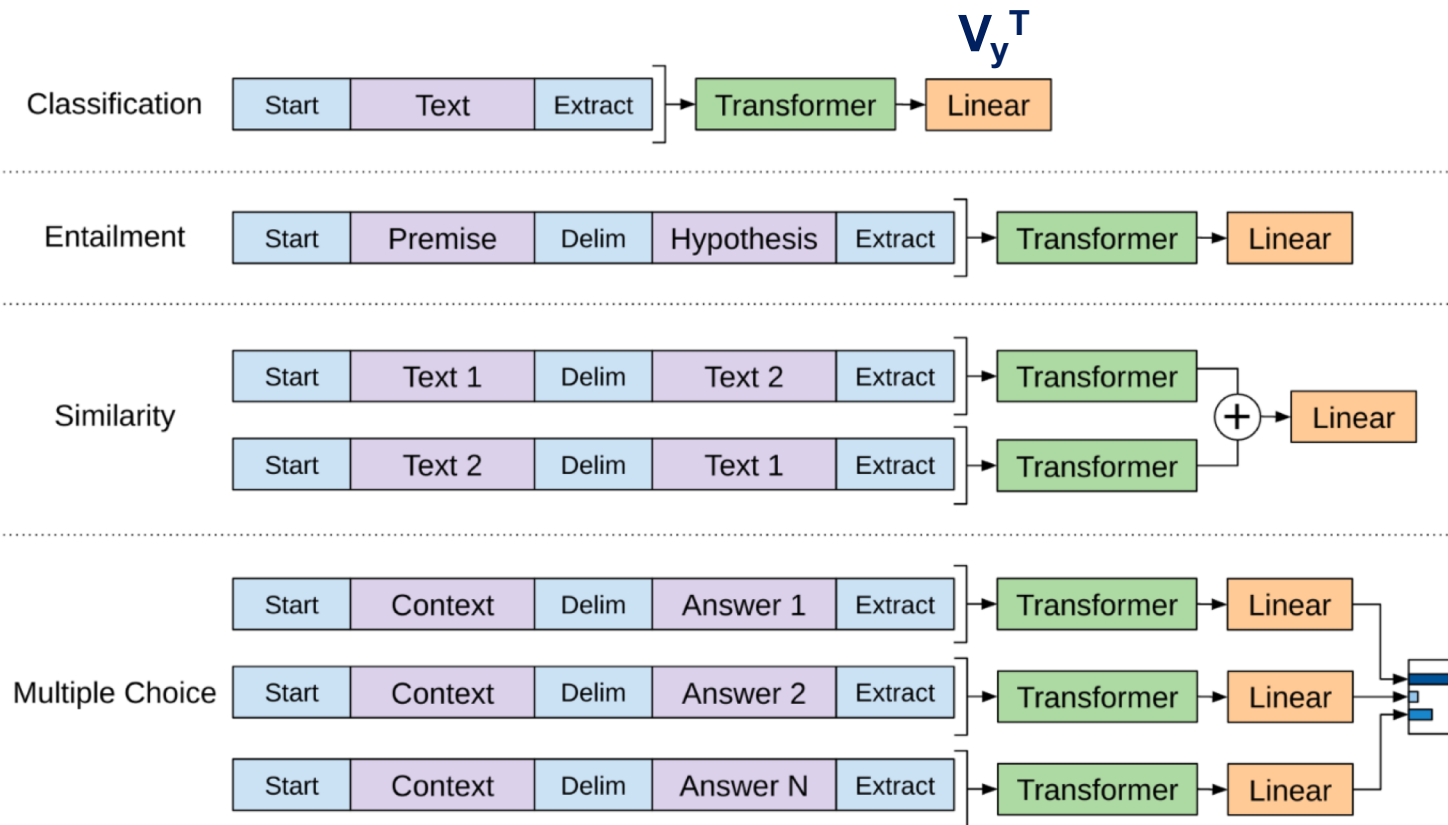
Byte-level BPE (byte pair encoding) of 50K subword units

also prevent BPE from merging across character categories (to avoid dog, dog!, dog?)

Modified initialization



$$\log \text{softmax}(\mathbf{V}_y^T \mathbf{X}_L) \quad \xrightarrow{\text{Language Modelling loss}} \quad L_2(\mathcal{C}) + \lambda * L_1(\mathcal{C})$$





Task	Description	Possible approach
Masked language prediction	predict masked words in a text	This is what BERT model is pre-trained for
Text classification or Sentiment analysis	assign a label to a given sequence of text	Apply linear transform+softmax on K classes , and train the model for the specific classification task
Text translation	translate a text	Need to pre-train a full Transformer Architecture for this task
Summarization	generate a summary of a document	GPT example: context given by a document; then generate 100 tokens by top-2 random sampling (Fan et al., 2018), i.e., take at each step the most likely next word at random among the top-2 candidates; finally select first 3 sentences as abstract
Question answering	answer a question	GPT example: the context of the language model is seeded with example question answer pairs which helps the model infer the short answer style of the dataset
Document question answering	answer a question on a given text	GPT example: context seeded by a text; then as for question answering
Conversational	ChatBot	InstructGPT/ChatGPT: Fine-tuned models using reinforcement learning from human feedback



Hugging Face

<https://huggingface.co/docs/transformers/v4.29.1/en/index>

State-of-the-art Machine Learning
for PyTorch, TensorFlow, and JAX



PyTorch



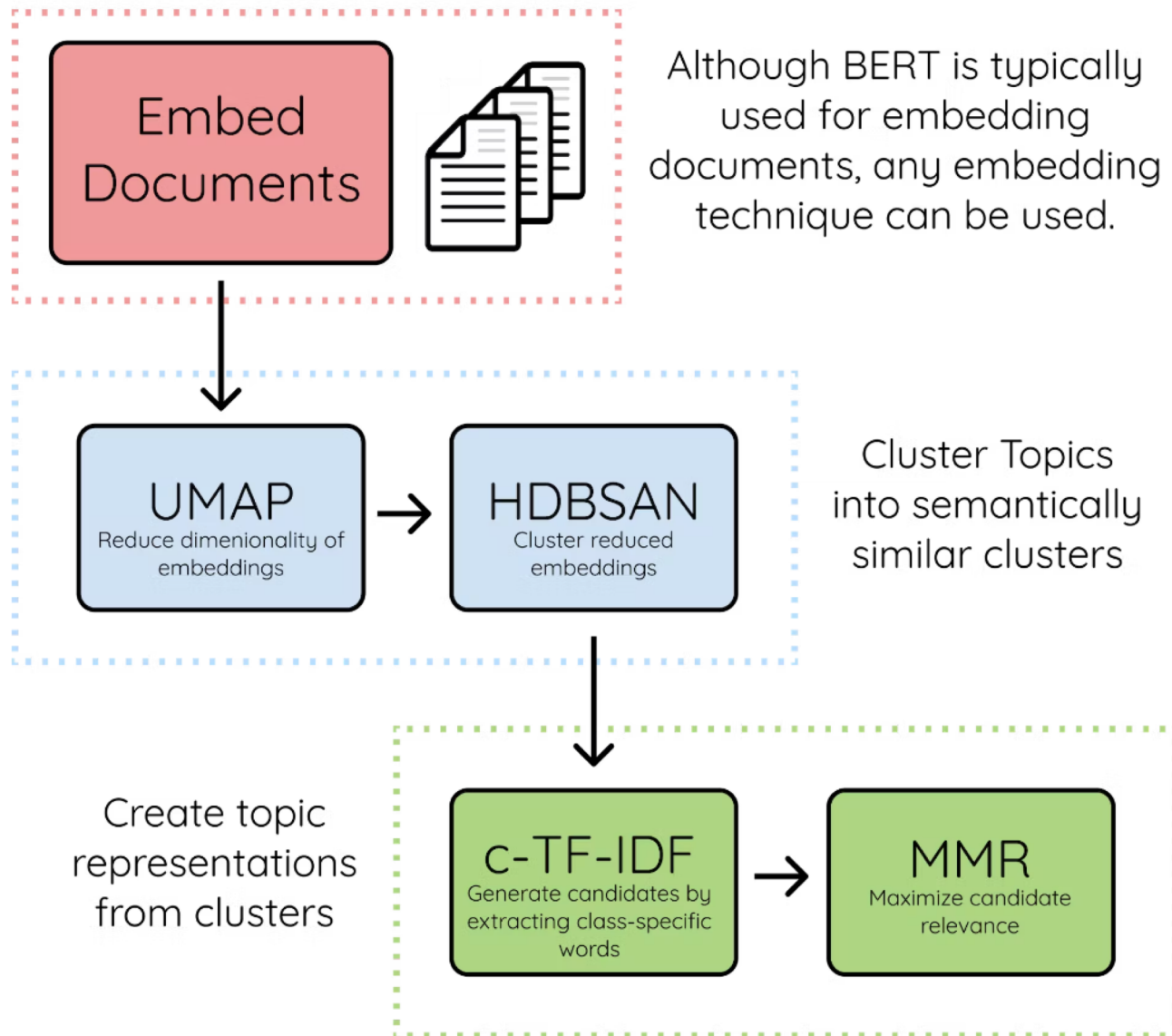
TensorFlow



ALBERT, BART, **BERT**, BigBird, BigBird-Pegasus, BioGpt, BLOOM, CamemBERT, CANINE, ConvBERT, CTRL, Data2VecText, DeBERTa, DeBERTa-v2, DistilBERT, ELECTRA, ERNIE, ErnieM, ESM, FlauBERT, FNet, Funnel Transformer, GPT-Sw3, **OpenAI GPT-2**, GPTBigCode, GPT Neo, GPT NeoX, GPT-J, I-BERT, LayoutLM, LayoutLMv2, LayoutLMv3, LED, LiLT, LLaMA, Longformer, LUKE, MarkupLM, mBART, MEGA, Megatron-BERT, MobileBERT, MPNet, MVP, Nezha, Nyströmformer, OpenLlama, **OpenAI GPT**, OPT, Perceiver, PLBart, QDQBert, Reformer, RemBERT, **RoBERTa**, RoBERTa-PreLayerNorm, RoCBert, RoFormer, SqueezeBERT, TAPAS, Transformer-XL, XLM, XLM-RoBERTa, XLM-RoBERTa-XL, XLNet, X-MOD, YOSO

BERT Topic

exploiting embeddings for topic detection





```
!pip install bertopic  
from bertopic import BERTopic  
from sentence_transformers import SentenceTransformer
```

```
sentence_model = SentenceTransformer("all-MiniLM-L6-v2")  
bert_model = BERTopic(embedding_model=sentence_model,  
                      min_topic_size=20, nr_topics='auto')
```

initialise model

```
docs = list(df2["text_sup_clean"])  
topics, probabilities = bert_model.fit_transform(docs)
```

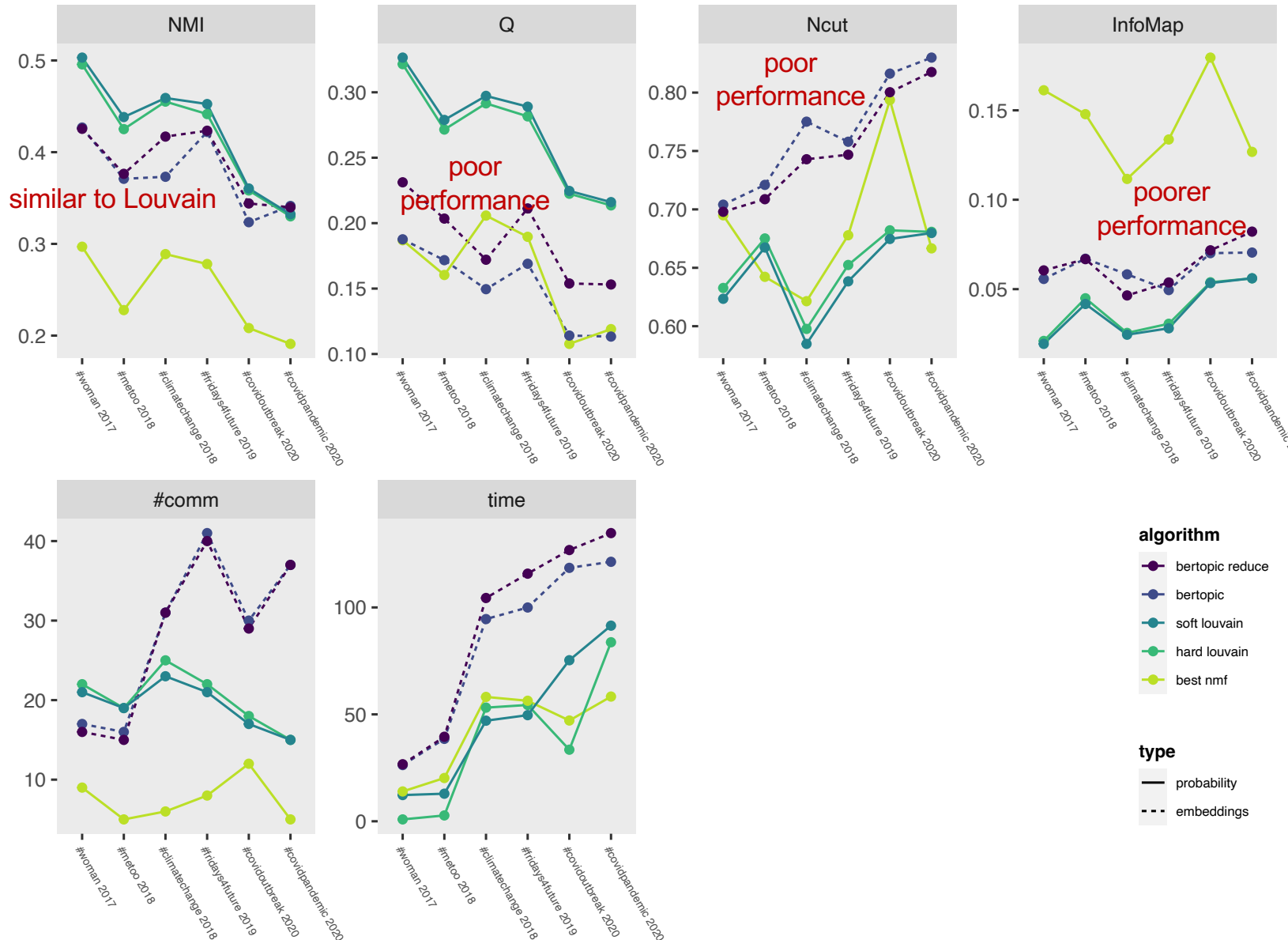
fit model

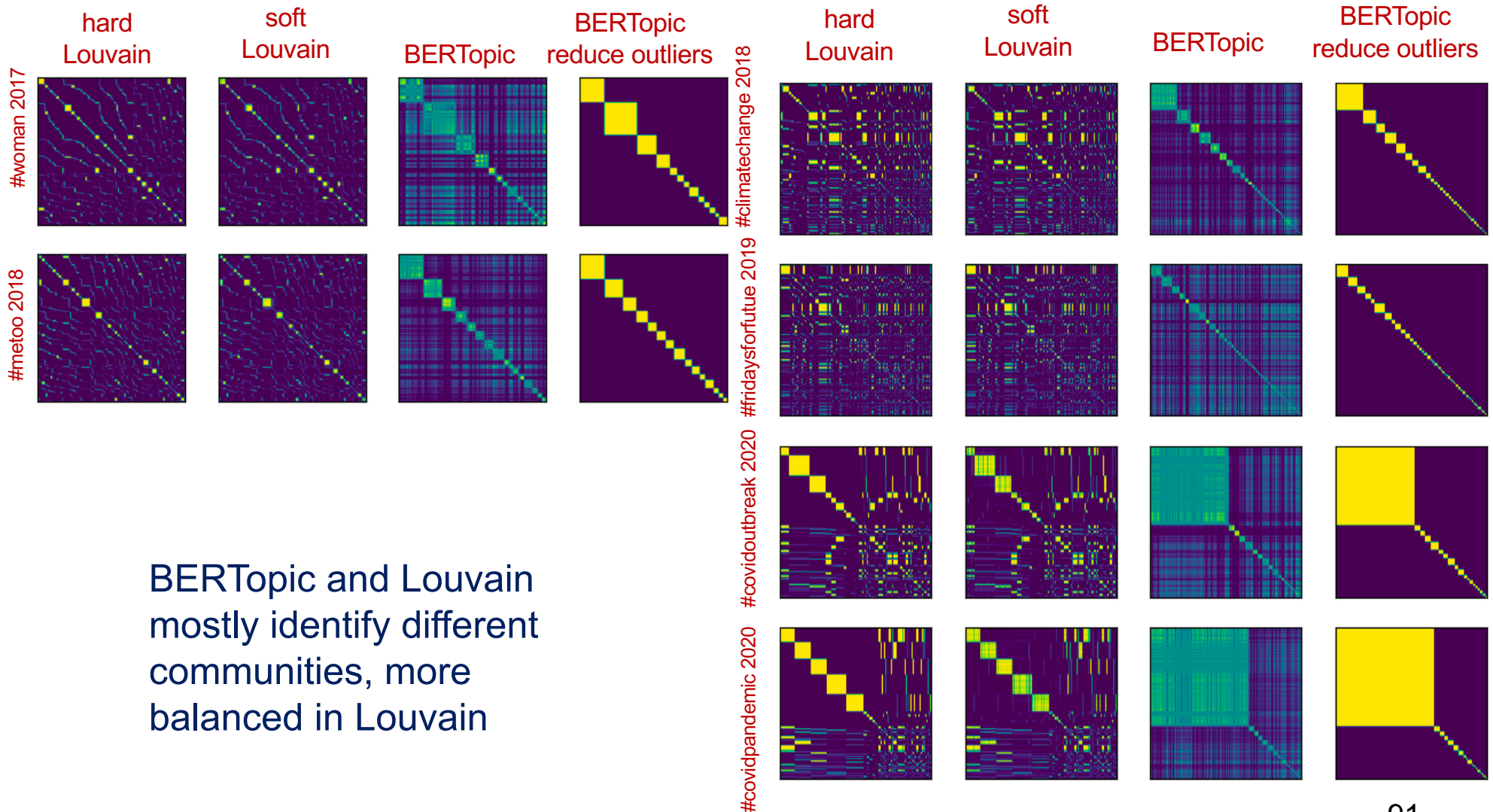
```
topics = bert_model.reduce_outliers(docs, topics)
```

reduce outliers

```
# extract community assignments  
C = sps.csr_matrix((len(topics), max(topics)+2))  
for i in range(C.shape[1]):  
    C[np.array(topics)==(i-1), i] = 1  
  
# remove zero assignments  
C = C[:, np.unique(scipy.sparse.find(C)[1])]
```

extract C from topic
assignment



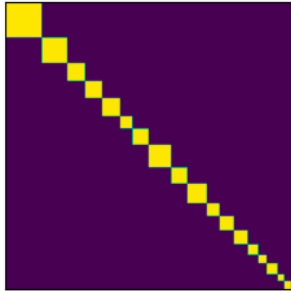




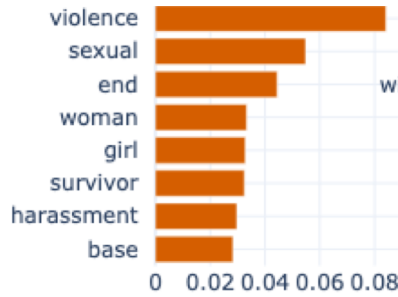
bert_model.visualize_documents(docs)

#metoo2018

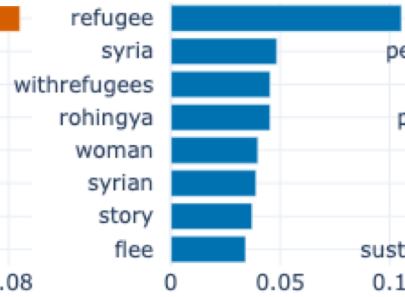




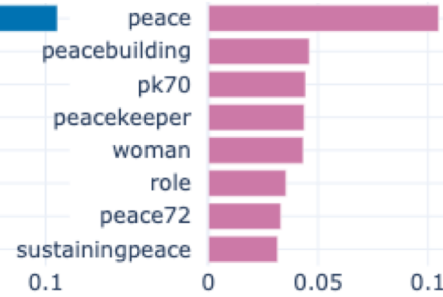
sexual violence



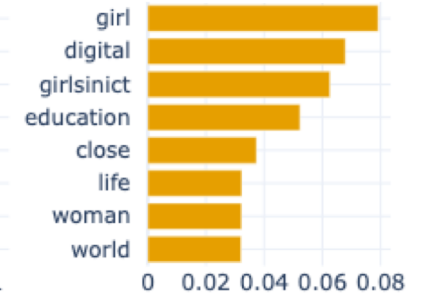
refugees



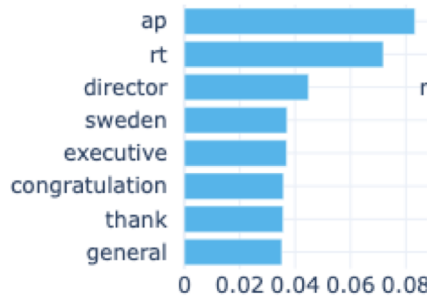
peace



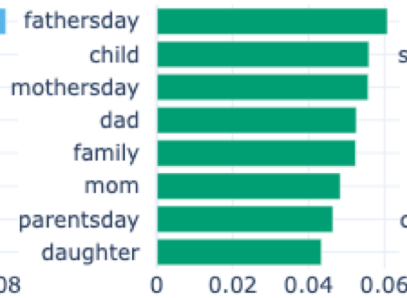
girlsinit



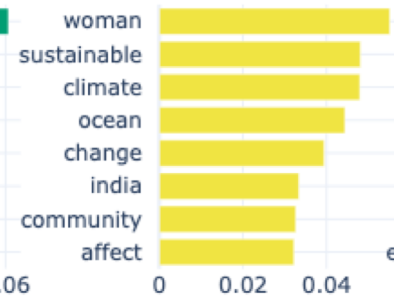
executive director



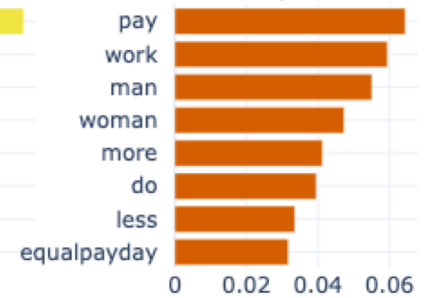
mothersday



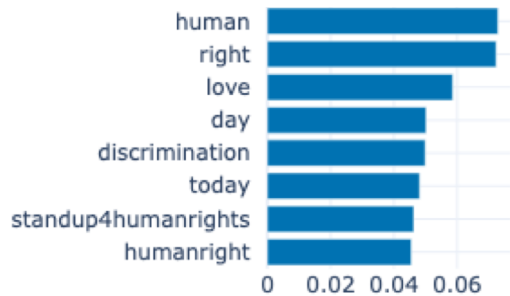
sustainability



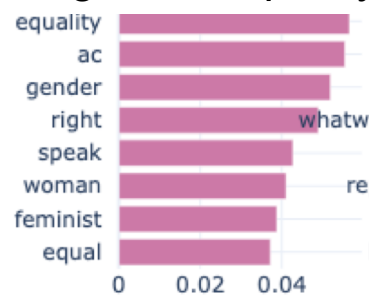
equal pay



discrimination



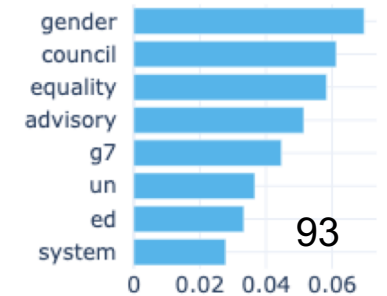
gender equality

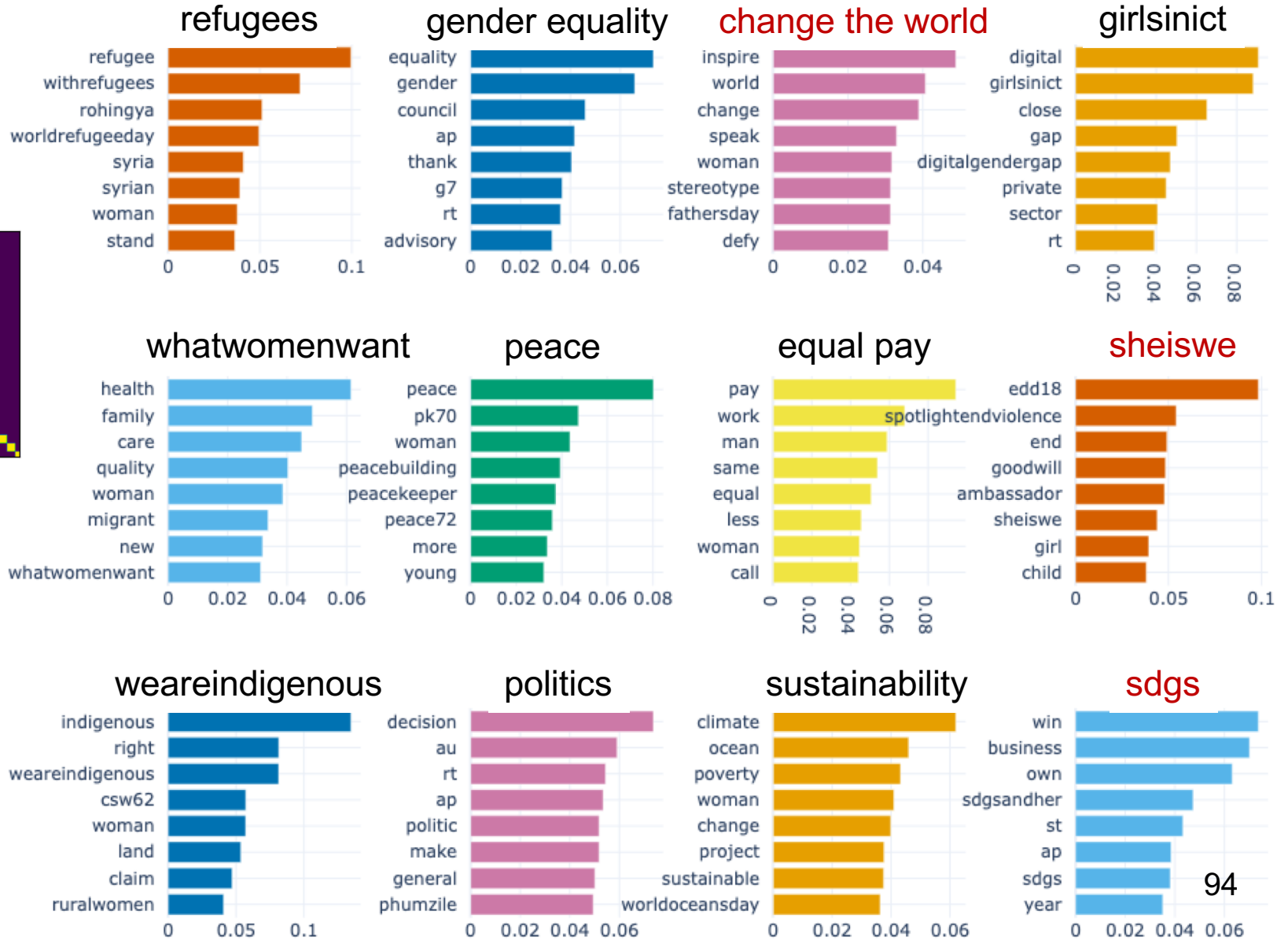
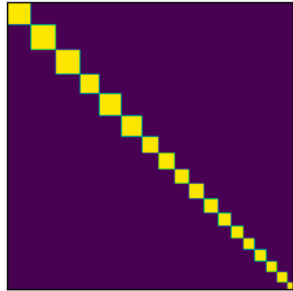


whatwomenwant



politics







How to use BERTopic barchart

with your own topic assignment **C** in python

```
def bertopic_overwrite(bert_model_in, docs, C):
    bert_model = copy.deepcopy(bert_model_in)

    # build the documents dataframe: 'Document' + "Topic"
    documents = pd.DataFrame(docs, columns=['Document'])
    tmp = np.array([C[i].argmax() for i in range(C.shape[0])])
    documents["Topic"] = tmp

    # update topic assignment
    bert_model.topics_ = tmp.tolist()

    # build cf-idf values
    documents_per_topic = documents.groupby(['Topic'],
                                             as_index=False).agg({'Document': ' '.join})
    c_tf_idf_, words = bert_model._c_tf_idf(documents_per_topic)
    bert_model.c_tf_idf_ = c_tf_idf_

    # extract words representations
    topic_representations_ = bert_model._extract_words_per_topic(words, documents)
    bert_model.topic_representations_ = topic_representations_
    bert_model.topic_labels_ = {key: f"{key}_" + "_".join([word[0] for word in values[:4]])
                                for key, values in
                                bert_model.topic_representations_.items()}

    # exit
    return bert_model
```



- ❑ Naturally provides a hard topic assignment
- ❑ **Useful** tool
- ❑ More readable output with deep cleaned text but same performance
- ❑ Comparison – with Louvain
 - weaker in general, especially in modularity
 - equivalent NMI** = relevant topics
 - lower modularity** = the documents that identify the topics are less distinguishable
 - higher complexity involved
 - less balanced topics, but generally meaningful
 - topics correlated with Louvain

Sentiment analysis

adding useful insights to your data



- ❑ Sentiment – e.g., positive, negative, neutral
enduring cognitive content that defines the affective state
- ❑ Emotion – e.g., anger, disgust, fear, joy, sadness
intense affective state of short duration with a precise cause
- ❑ Ingroup bias – e.g., use of pronouns I, we, us
tendency to favor one's own group over other groups
- ❑ Outgroup bias – e.g., use of pronoun they
tendency to dislike members of groups we don't identify with
- ❑ Agency – e.g., use of action verbs do, take, make
perception that an individual is able to contribute to/a group
can collectively reach a social change



UNIVERSITÀ
DEGLI STUDI
DI PADOVA

LIWC linguistic inquiry and word count

Tausczik, Pennebaker. "The psychological meaning of words:
LIWC and computerized text analysis methods." (2010)

<https://citeseerx.ist.psu.edu/document?repid=rep1&type=pdf&doi=79d2494cc10a9633c42115df84bb74ed447080f6>

LIWC HOME TRY IT NOW

INTRODUCING LIWC-22

A NEW SET OF TEXT ANALYSIS TOOLS AT YOUR FINGERTIPS

<https://www.liwc.app/>

- ❑ word count (or **dictionary**) methodology
- ❑ over 60 dictionaries coded and **validated** for their accuracy in reflecting psychological content
- ❑ **simplicity** of implementation and usage
- ❑ state-of-the-art in psychology
- ❑ **one licence** available in the instructor's PC 😊



Category	Examples	Words in Category	Psychological Correlates
<i>Linguistic processes</i>			
Word count			Talkativeness, verbal fluency
Words/sentence			Verbal fluency, cognitive complexity
Dictionary words	(Percentage of all words captured by the program)		Informal, nontechnical language
Words >6 letters	(Percentage of all words longer than 6 letters)		Education, social class
Total function words		464	
Total pronouns	I, them, itself	116	Informal, personal
Personal pronouns	I, them, her	70	Personal, social
First-person singular	I, me, mine	12	Honest, depressed, low status, personal, emotional, informal
First-person plural	We, us, our	12	Detached, high status, socially connected to group (sometimes)
Second person	You, your, thou	20	Social, elevated status
Third-person singular	She, her, him	17	Social interests, social support
Third-person plural	They, their, they'd	10	Social interests, out-group awareness (sometimes)

ingroup



outgroup





Category	Examples	Words in Category	Psychological Correlates
Indefinite pronouns	It, it's, those	46	Use of concrete nouns, interest in objects and things
Articles	A, an, the	3	
Common verbs	Walk, went, see	383	Informal, passive voice Focus on the past
Auxiliary verbs	Am, will, have	144	
Past tense	Went, ran, had	145	
Present tense	Is, does, hear	169	Living in the here and now
Future tense	Will, gonna	48	Future and goal oriented
Adverbs	Very, really, quickly	69	Education, concern with precision
Prepositions	To, with, above	60	
Conjunctions	And, but, whereas	28	Inhibition
Negations	No, not, never	57	
Quantifiers	Few, many, much	89	
Numbers	Second, thousand	34	Informal, aggression,
Swear words	Damn, piss, fuck	53	
<i>Psychological processes</i>			
Social processes	Mate, talk, they, child	455	Social concerns, social support
Family	Daughter, husband	64	Emotionality
Friends	Buddy, friend, neighbor	37	
Humans	Adult, baby, boy	61	
Affective processes	Happy, cried, abandon	915	

focus on

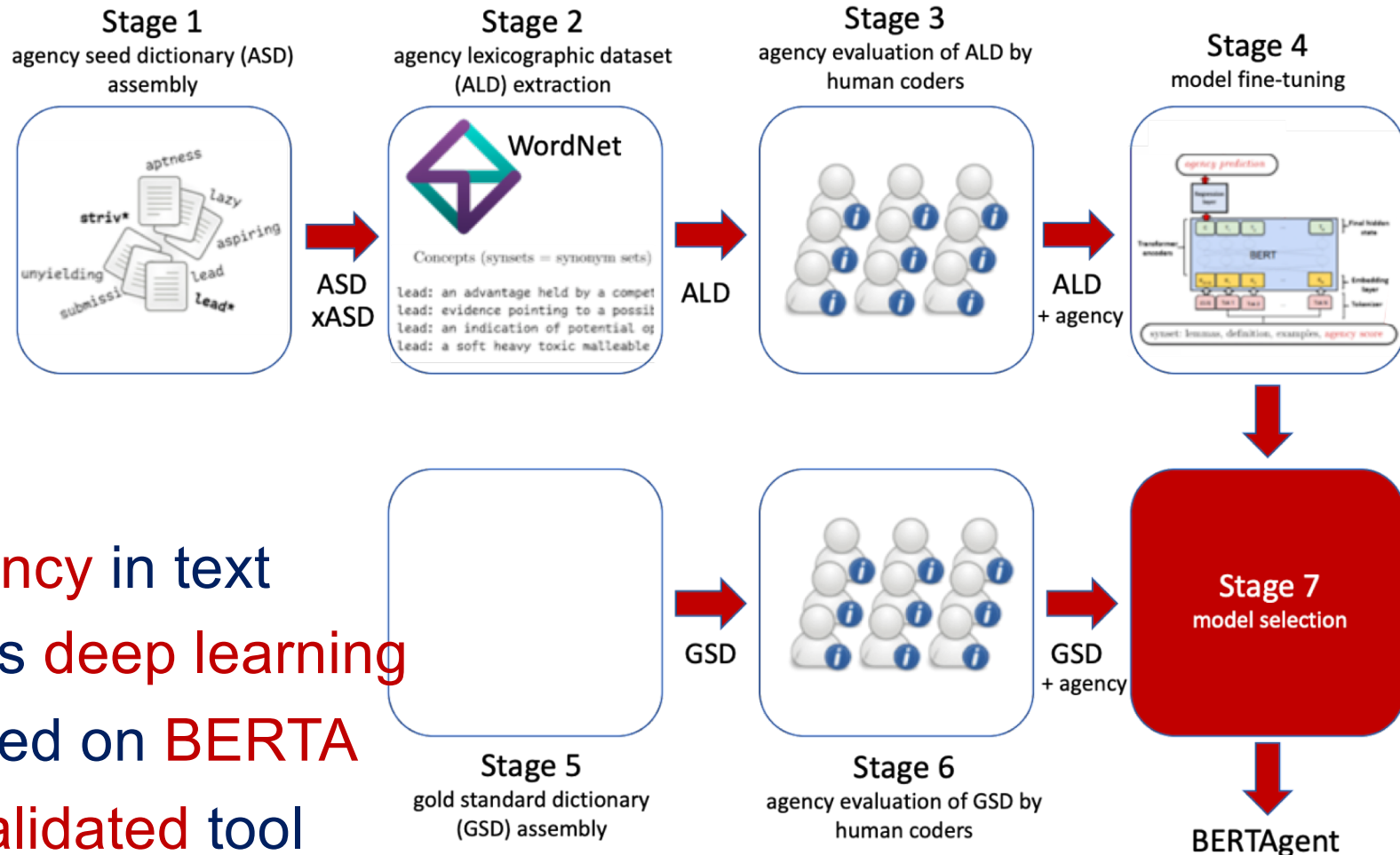
past, present

or future



WC	Analytic	Clout	Authentic	Tone	WPS	Sixltr	Dic	function	pronoun
ppron	i	we	you	shehe	they	ipron	article	prep	auxverb
adverb	conj	negate	verb	adj	compare	interrog	number	quant	affect
posemo	negemo	anx	anger	sad	social	family	friend	female	male
insight	cause	discrep	tentat	certain	differ	percept	see	hear	feel
bio	body	health	sexual	ingest	drives	affiliation	achieve	power	reward
risk	focus past	focus present	focus future	relativ	motion	space	time	work	leisure
home	money	relig	death	informal	swear	netspeak	assent	nonflu	filler
AllPunc	Period	Comma	Colon	SemiC	QMark	Exclam	Dash	Quote	Apostro
Parenth	cogproc								

Choose the ones of **interest** to your project!



- ❑ agency in text
- ❑ uses deep learning
- ❑ based on BERT
- ❑ a validated tool
- ❑ available on Python

BERTAgent
<https://pypi.org/project/bertagent/>



Validation of BERTAgent

deep learning wins versus DWC = dictionary word count

Variable	<i>M</i>	<i>SD</i>	1	2	3	4	5	6	7	8
1. HumEval	0.12	1.54								
2. PietA	0.05	0.05	.17** [.06, .28]		-1.25	0.28	0.05	5.35**	-1.78	-10.95**
3. PietB	0.02	0.03	.25** [.14, .35]	.40** [.30, .49]		1.27	1.16	6.58**	-0.70	-10.00**
4. PietC	0.05	0.05	.17** [.06, .28]	.99** [.99, 1.00]	.40** [.30, .49]		0.03	5.34**	-1.80	-10.93**
5. NicoPos	0.03	0.04	.17** [.05, .27]	.18** [.07, .29]	.23** [.12, .34]	.17** [.06, .28]		5.49**	-3.81**	-11.08**
6. NicoNeg	0.01	0.03	-.28** [-.38, -.17]	-.10 [-.21, .01]	-.01 [-.12, .11]	-.10 [-.21, .02]	-.03 [-.14, .09]		-5.73**	-13.40**
7. NicoCom	0.02	0.05	.30** [.19, .40]	.20** [.09, .31]	.19** [.08, .30]	.19** [.08, .30]	.82** [.78, .85]	-.60** [-.67, -.52]		-10.38**
8. BATot	0.09	0.35	.78** [.73, .82]	.21** [.10, .31]	.24** [.13, .34]	.20** [.09, .31]	.22** [.11, .33]	-.42** [-.51, -.33]	.42** [.33, .51]	

Human
evaluation

BERTAgent

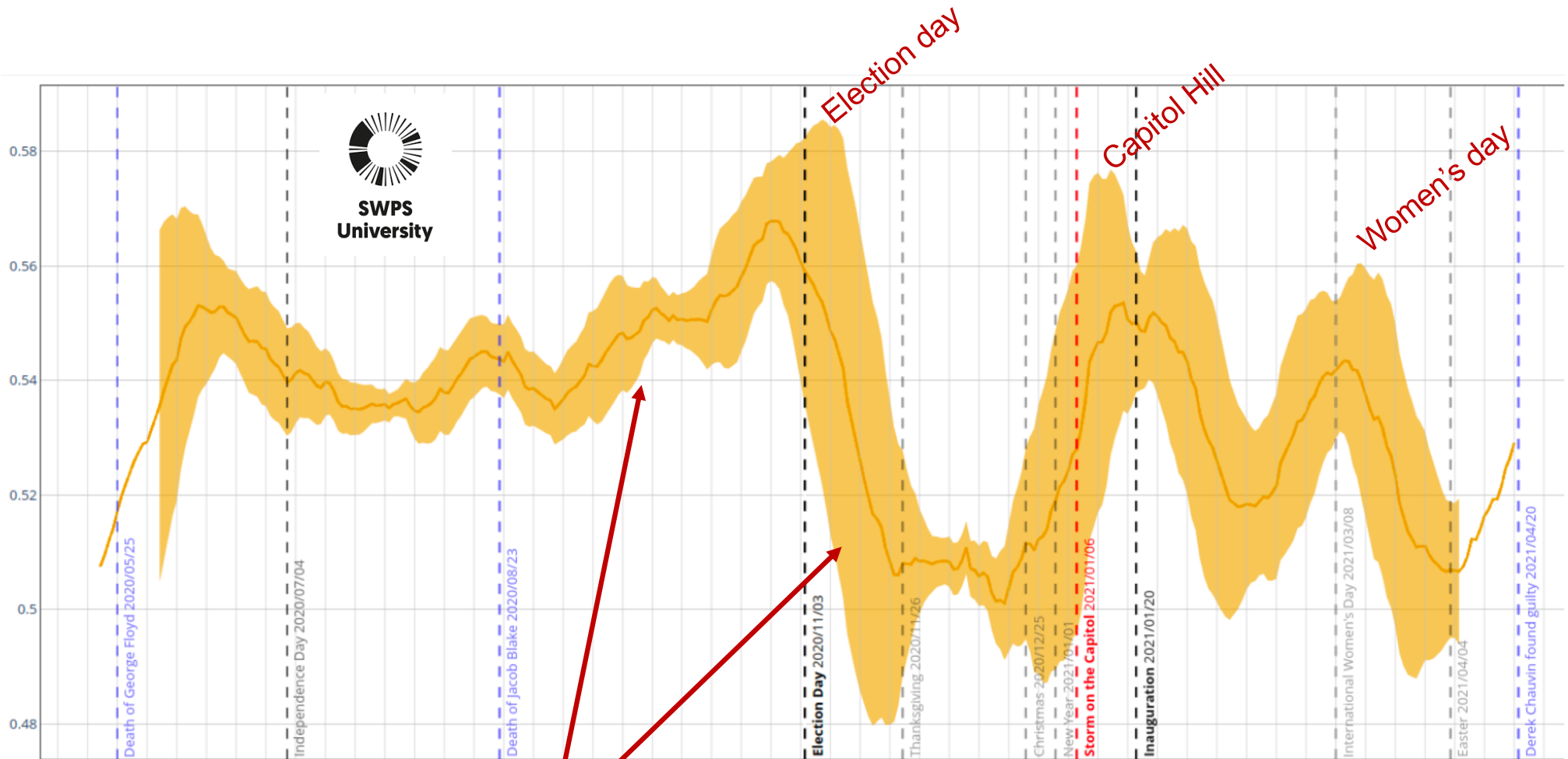
best correlation with
Human evaluation

Z-statistics:
correlation is statistically
more relevant than DWC



Agency in US elections

Twitter, 2020-2021
by Jan Nikadon @ swps



agency raises before elections than drops





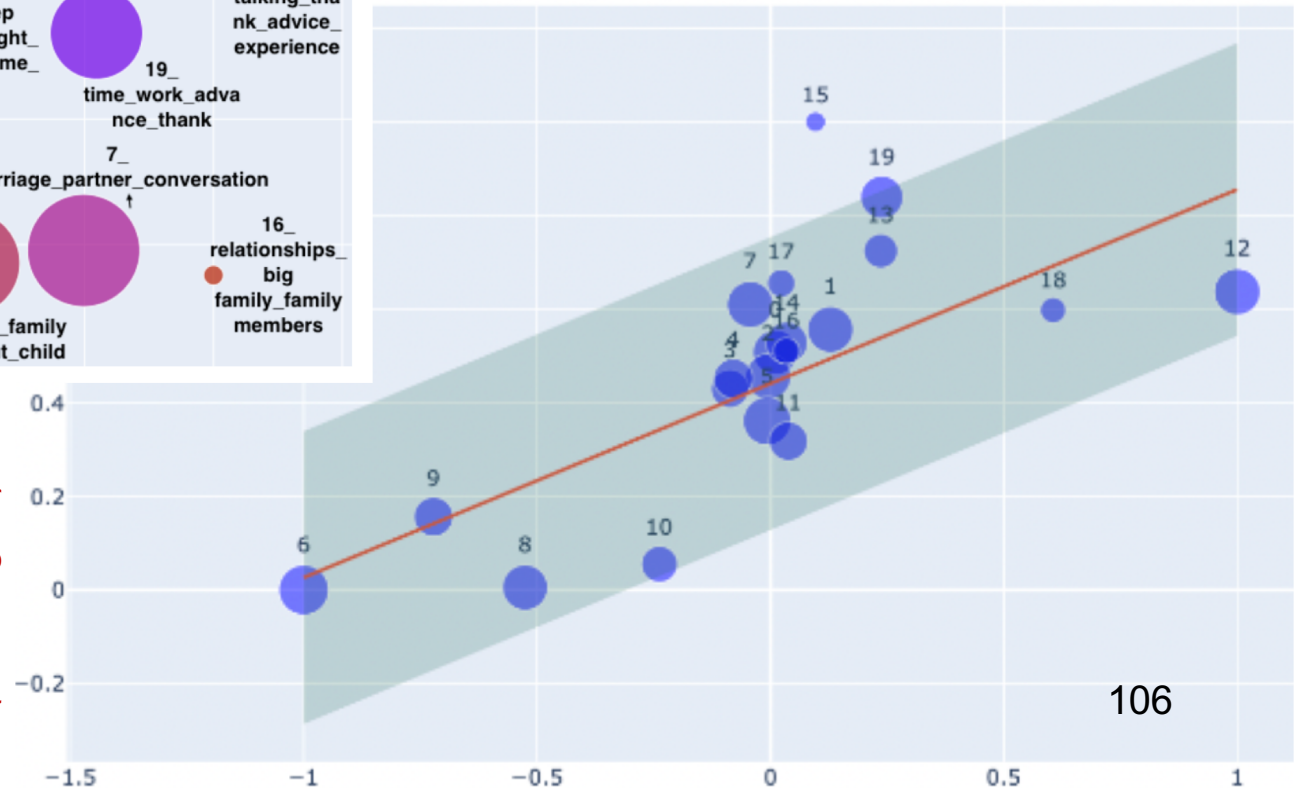
Agency in postpartum depression

Reddit Posts 2021
by Selen Arslan @ unipd/swps



composite emotion score
(LIWC, EmoPos - EmoNeg)

semantic agency
(BERTAgent)





BERTAgent in Python

Free software: GNU General Public License v3

PyPi: <https://pypi.org/project/bertagent/>

```
[1] !pip install bertagent
```

install, import,
set instance

```
▶ from bertagent import BERTAgent  
ba0 = BERTAgent()
```

input sentences must
be superficially cleaned



```
▶ # provide example sentences
```

```
sents = ["hardly wo  
"hard work  
"striving  
"strugglin  
"strugglin  
"unable to  
"this car  
"this car  
"this poli  
]
```

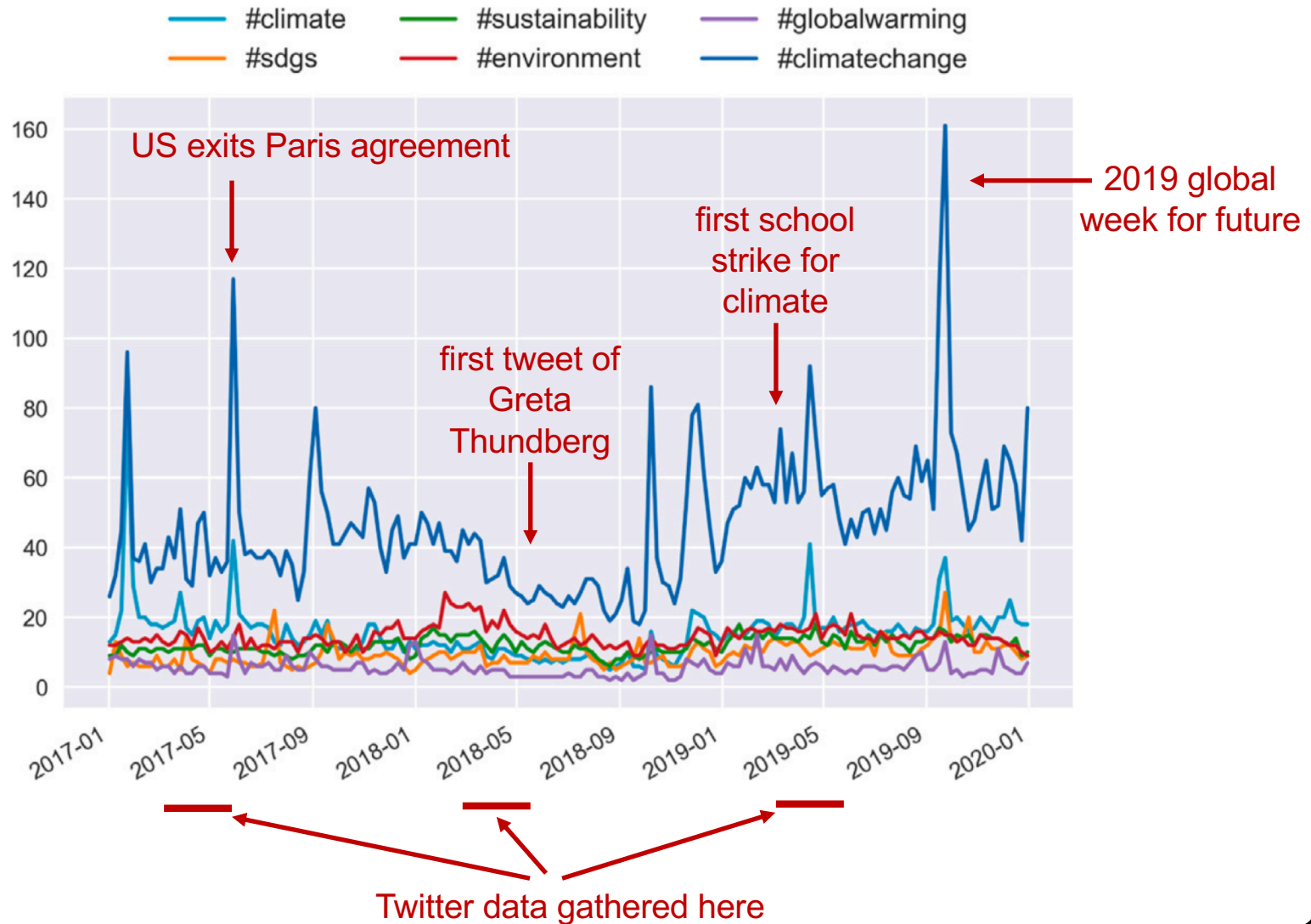
'hardly working individual' : -0.57	BERTAgent output
'hard working individual' : 0.44	
'striving to achieve my goals' : 0.73	
'struggling to achieve my goals' : -0.67	
'struggling to survive' : -0.52	
'unable to survive' : -0.57	
'this car runs on gasoline with lead' : -0.03	
'this car runs on gasoline and it will lead us' : 0.09	
'this politician runs for office and he will lead us' : 0.58	

```
# assign agency  
vals = ba0.predict(sents)  
# print results  
for item in zip(sents, vals):  
    print(f" {item[0]!r} : {item[1]:.2f}")
```

run BERTAgent

Using sentiment analysis

an overview on how it can be useful in your projects



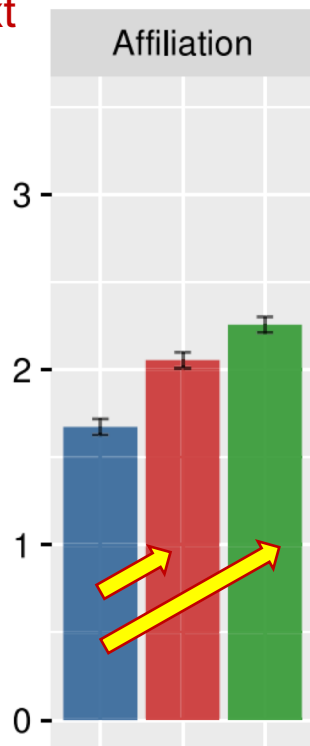


Socio-psychological linguistic markers

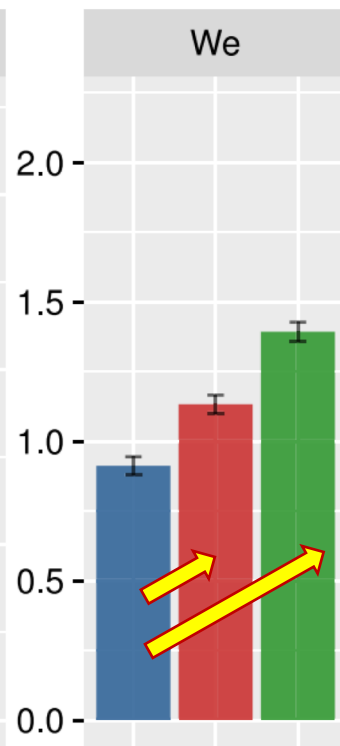
a view on the entire tweets corpus

■ 2017 ■ 2018 ■ 2019

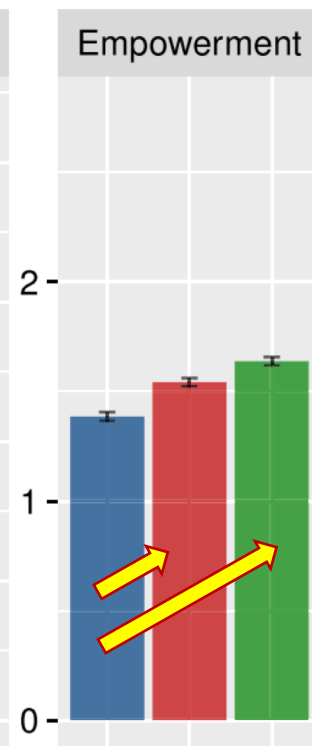
ingroup community
orientation within
the text



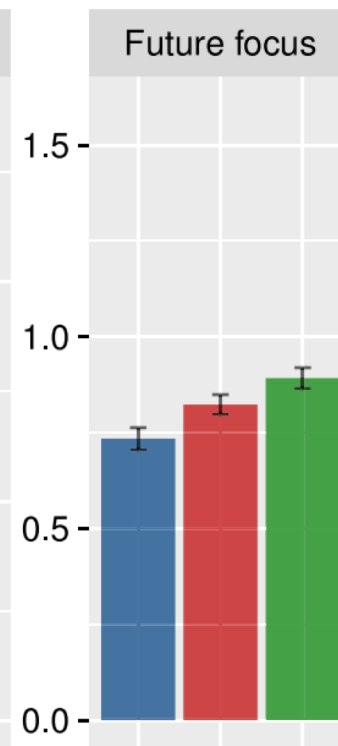
salience of
group
membership,
sense of
belonging



a person's
striving to be
independent to
assert, protect
and expand
one's self



orientation of tweets to the
past or future



only a few
statistically
relevant
changes



☰ Student's *t*-test

[Article](#) [Talk](#)

From Wikipedia, the free encyclopedia

A ***t*-test** is a type of statistical analysis used to **compare the averages of two groups** and determine whether the differences between them are more likely to arise from random chance. It is any **statistical hypothesis test** in which the **test statistic** follows a **Student's *t*-distribution** under the **null hypothesis**. It is most commonly applied when the test statistic would follow a **normal distribution** if the value of a **scaling term** in the test statistic were known (typically, the scaling term is unknown and is therefore a **nuisance parameter**). When the scaling term is estimated based on the **data**, the test statistic—under certain conditions—follows a Student's *t* distribution. **The *t*-test's most common application is to test whether the means of two populations are different.**



Assumption:

the **average** values of the two populations being compared should follow a **normal distribution** (e.g., with many samples)

Hypothesis (to be tested):

H0 - the two sets have **equal** average value, $m_x = m_y$

H1 - the two sets have different average value, $m_x \neq m_y$

Test statistic: $t = \frac{\bar{x} - \bar{y}}{\sqrt{\frac{s_x^2}{N_x} + \frac{s_y^2}{N_y}}} \sim t_\nu$

sample averages

unbiased estimator of variance

samples sizes

Student's t distribution with ν degrees of freedom (an approximation under H0)

estimate of ν (degrees of freedom) used for calculations

$$\hat{\nu} = \frac{\left(\frac{s_x^2}{N_x} + \frac{s_y^2}{N_y}\right)^2}{\frac{(s_x^2/N_x)^2}{N_x-1} + \frac{(s_y^2/N_y)^2}{N_y-1}}$$



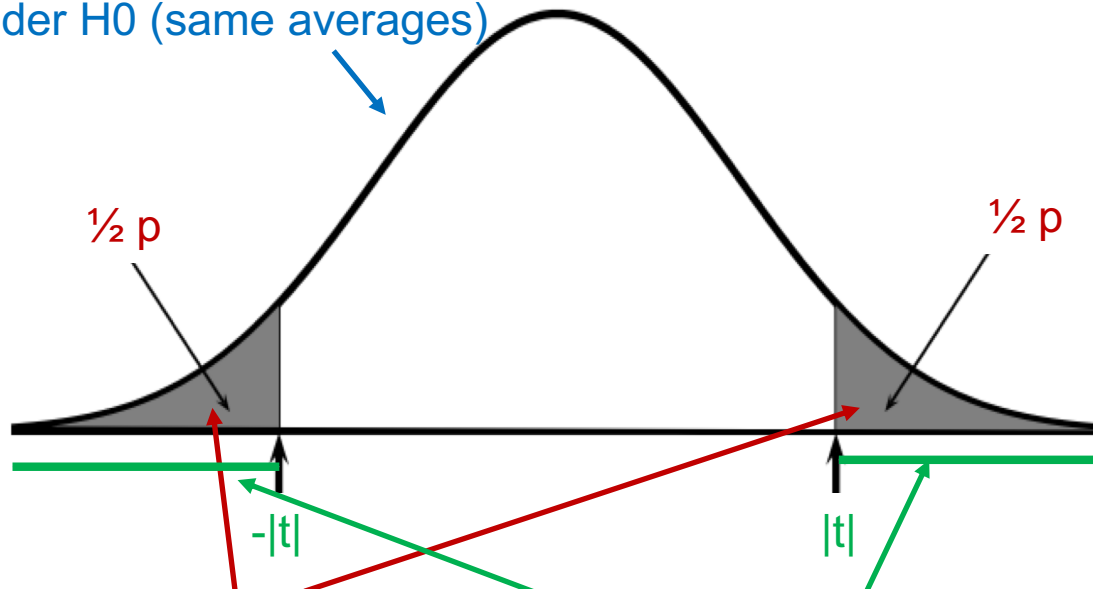
Student/Welch t-test

p value = probability of error under H_0

we declare different average values H_1

p-value	evidence
$< .01$	very strong evidence against H_0
$.01 - .05$	strong evidence against H_0
$.05 - .10$	weak evidence against H_0
$> .1$	little or no evidence against H_0

Student-t PDF with ν degrees of freedom under H_0 (same averages)



probability p that, by confirming H_1 , we are making errors on H_0

(conservative) region choice to declare H_1 from the t value

the p value informs on whether a difference exists (statistically)

it is a false positive rate



Cohen's d-value

evaluating effect sizes

$$\text{Cohen's } d = \frac{\bar{x} - \bar{y}}{\sqrt{a s_x^2 + (1-a) s_y^2}}$$

$$a = \frac{N_x - 1}{N_x + N_y - 2}$$

Relative size	Effect size
	0.0
Small	0.2
Medium	0.5
Large	0.8
	1.4

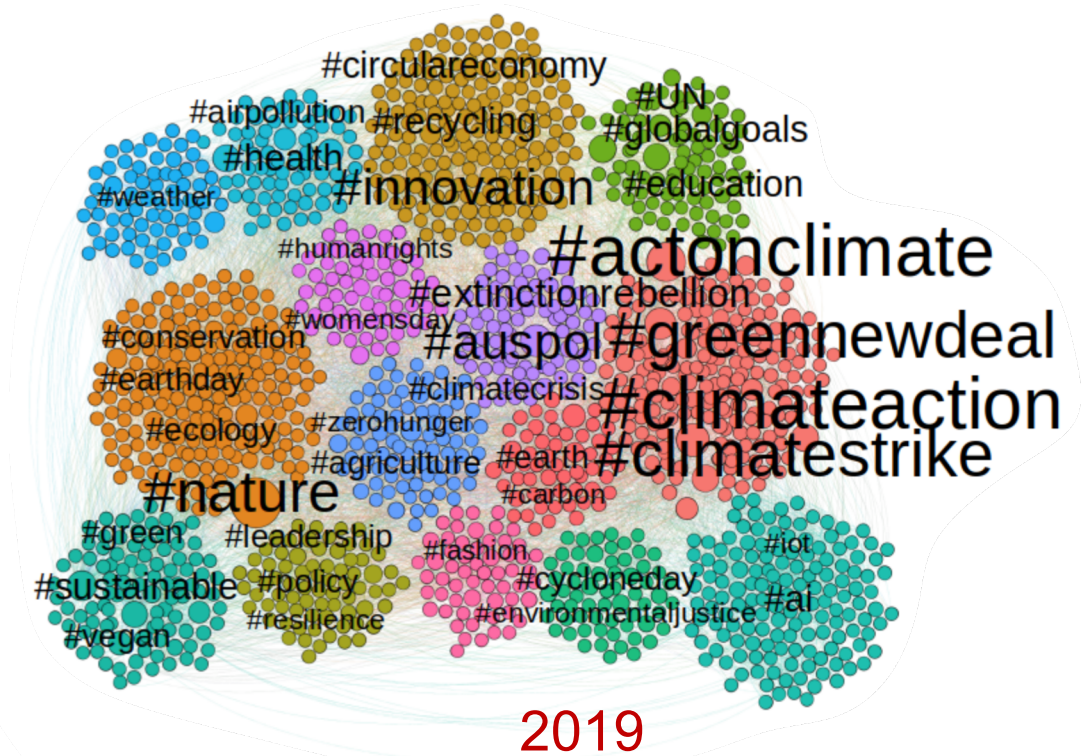
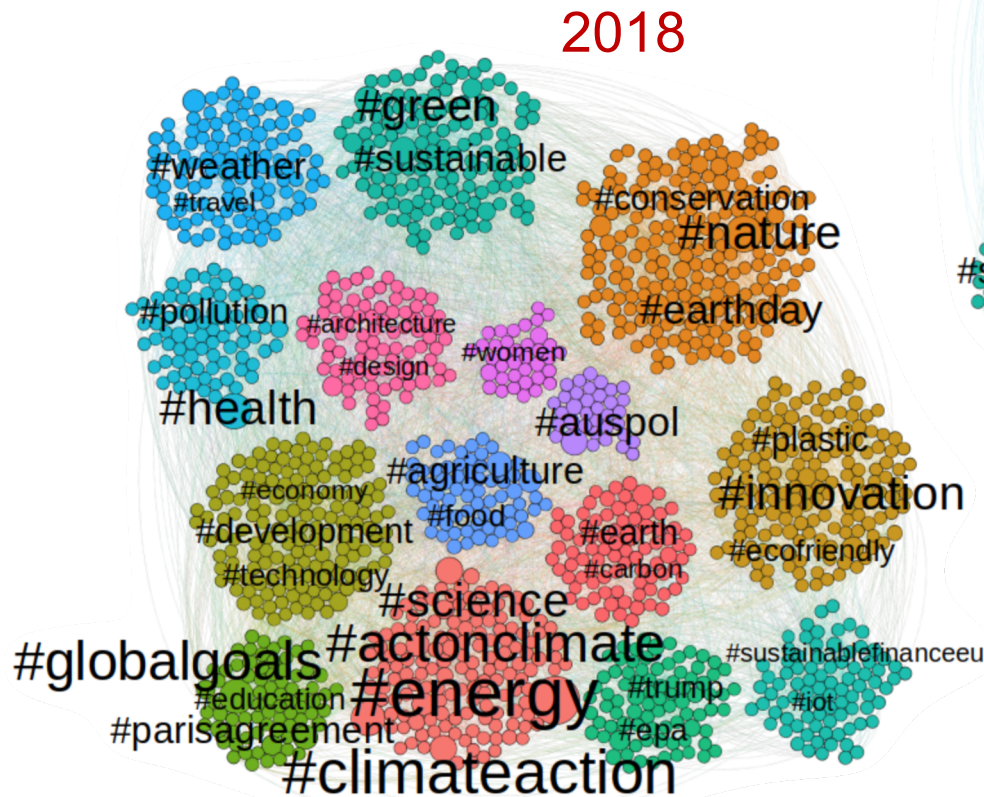
we confirm H1



the *d* value
informs on the
size of the effect

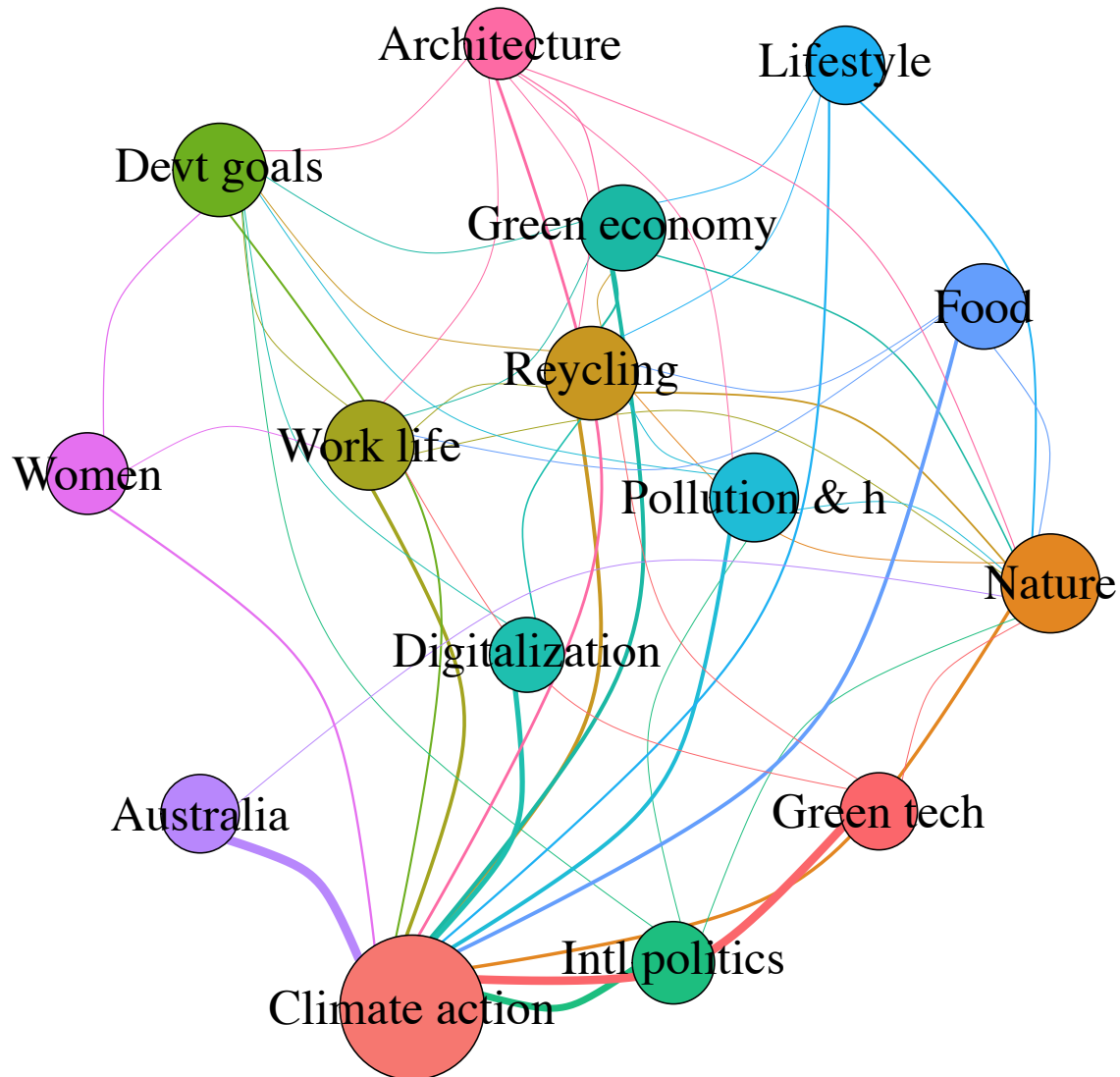


Topics in #climateaction on Twitter in 2017, 2018, 2019





Topics interdependencies



projecting the
adjacency matrix on
topics

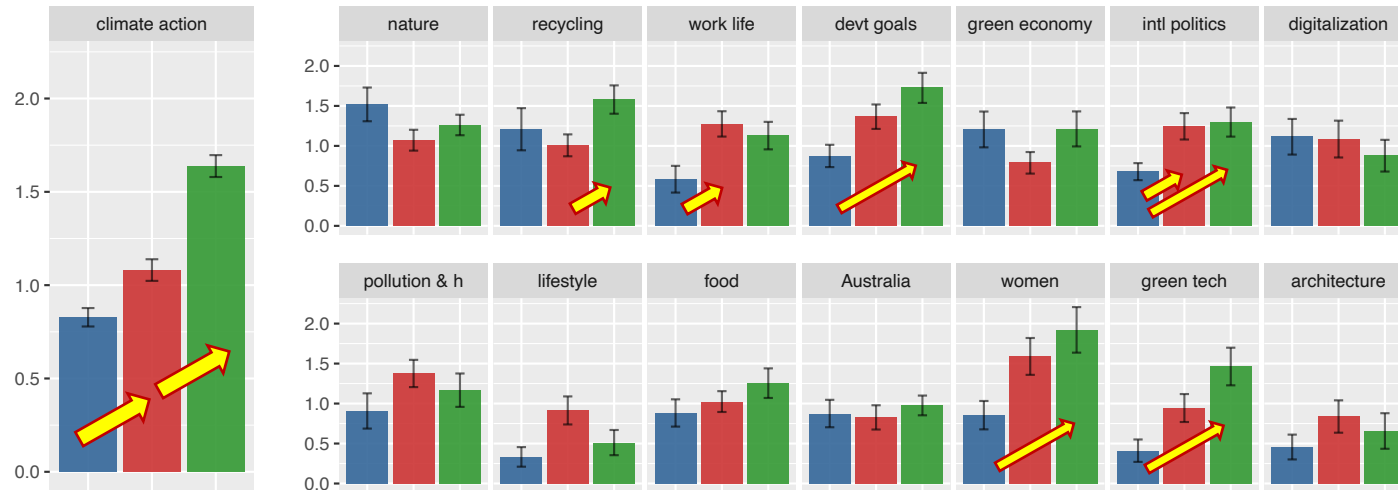
P_{11}	P_{12}	P_{13}
P_{21}	P_{22}	P_{23}
P_{31}	P_{32}	P_{33}



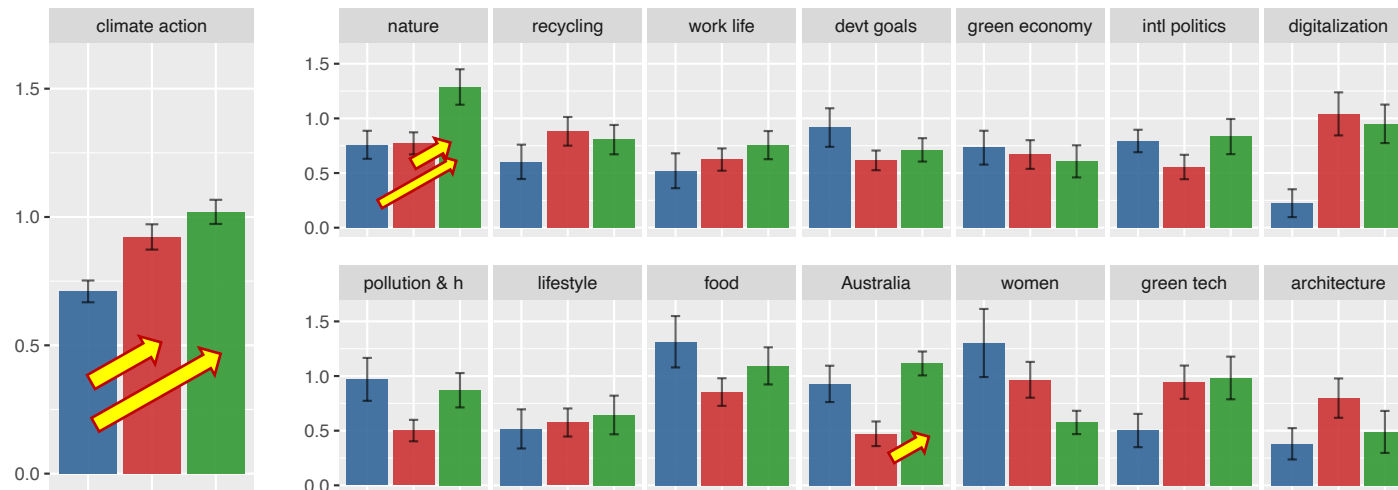
Socio-psychological linguistic markers a view inside topics

2017 2018 2019

(b) We



(d) Future focus



relevant
statistically
changes of
we-future
only in the
climate
action
community

Wrap-up

on topic detection



❑ What available tools should be used

Louvain & BERTopic

compare their performance through NMI, modularity, etc.

LIWC & BERTAgent

to enrich your analysis under a socio-psychological lens

❑ What available tools should **NOT** be used

InfoMap, NMF & LDA

they show poor performance

❑ What would be nice to see implemented

soft Louvain made fast

performance of BigCLAM and SMBs

NFTM VAE and its performance