Consider the data 'data.npy'. Assume X is distributed according to a normal,

$$f_X(x|\mu,\sigma) = \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}\frac{(x-\mu)^2}{\sigma^2}}$$

where

$$f_{prior}(\mu) = \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}\frac{(\mu_i-m)^2}{s^2}}$$

with

$$m = 4 \quad s = 2$$

and

$$f_{prior}(\sigma) = \frac{\beta^\alpha}{\Gamma(\alpha)}(1/x)^{\alpha+1}e^{-\beta/x}$$

with

$$\alpha = 2, \beta = 1$$

Estimate μ, σ as posterior averages (with errors given by posterior standard deviations) from the data, using Metropolis algorithm to sample. In other words, sample

$$f(\mu,\sigma|x) \propto f_X(x|\mu,\sigma) f_{prior}(\mu) f_{prior}(\sigma)$$

using Metropolis algorithm. The proposal step $T(\mu',\sigma'|\mu,\sigma)$ can be any random move

$$\mu \to \mu'$$

$$\sigma \to \sigma'$$

For instance, (μ',σ') are sampled normally around (μ,σ) with std. τ, $(\mu',\sigma') \sim \mathcal{N}((\mu,\sigma),\tau^2\mathbb{I})$.