

Network Science

#9 Homophily

© 2020 T. Erseghe

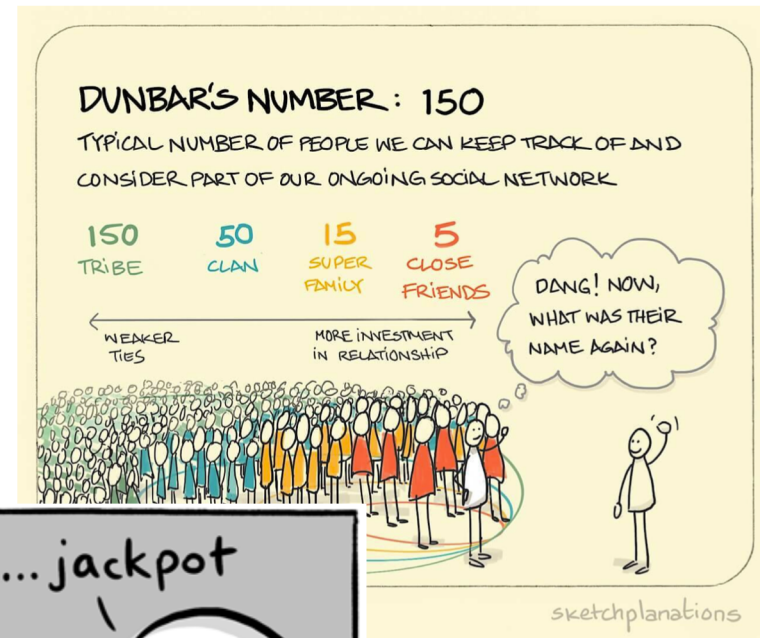
Humans and social media

We have access to an unlimited amount of information, but we follow a **limited** number of sources

Because we are...

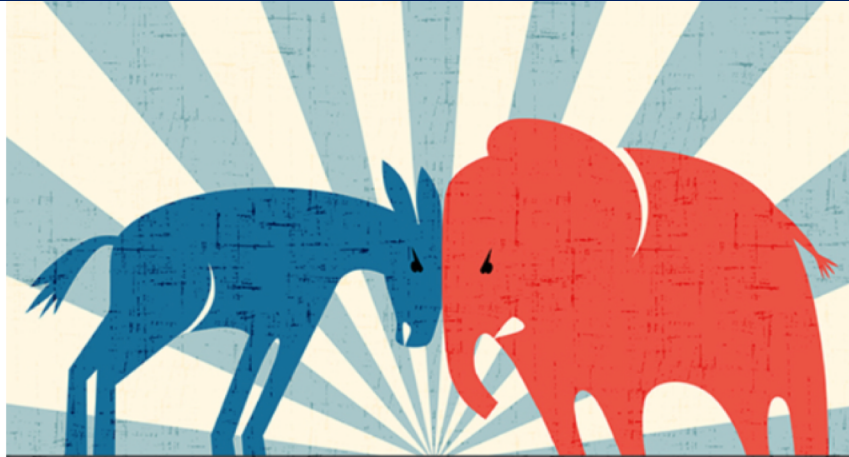
Bounded

Biased



Effects on online behaviour

Polarization



Homophily



Selective exposure

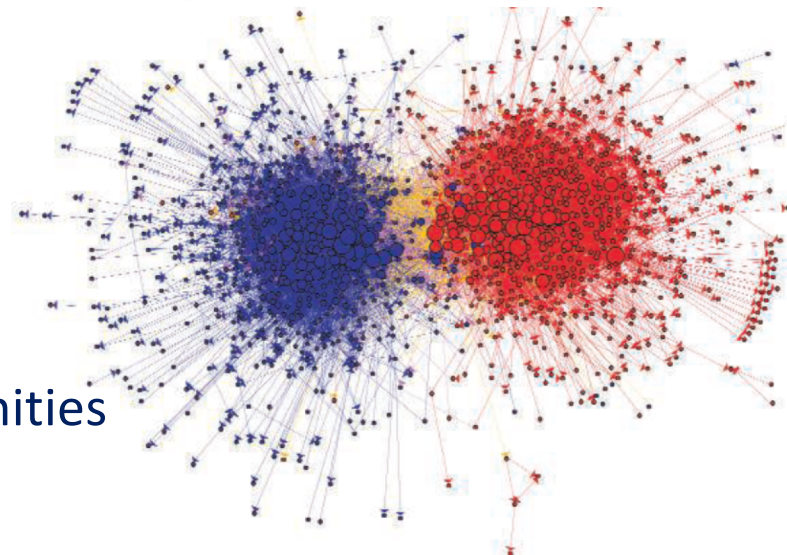


Homophily

Homophily

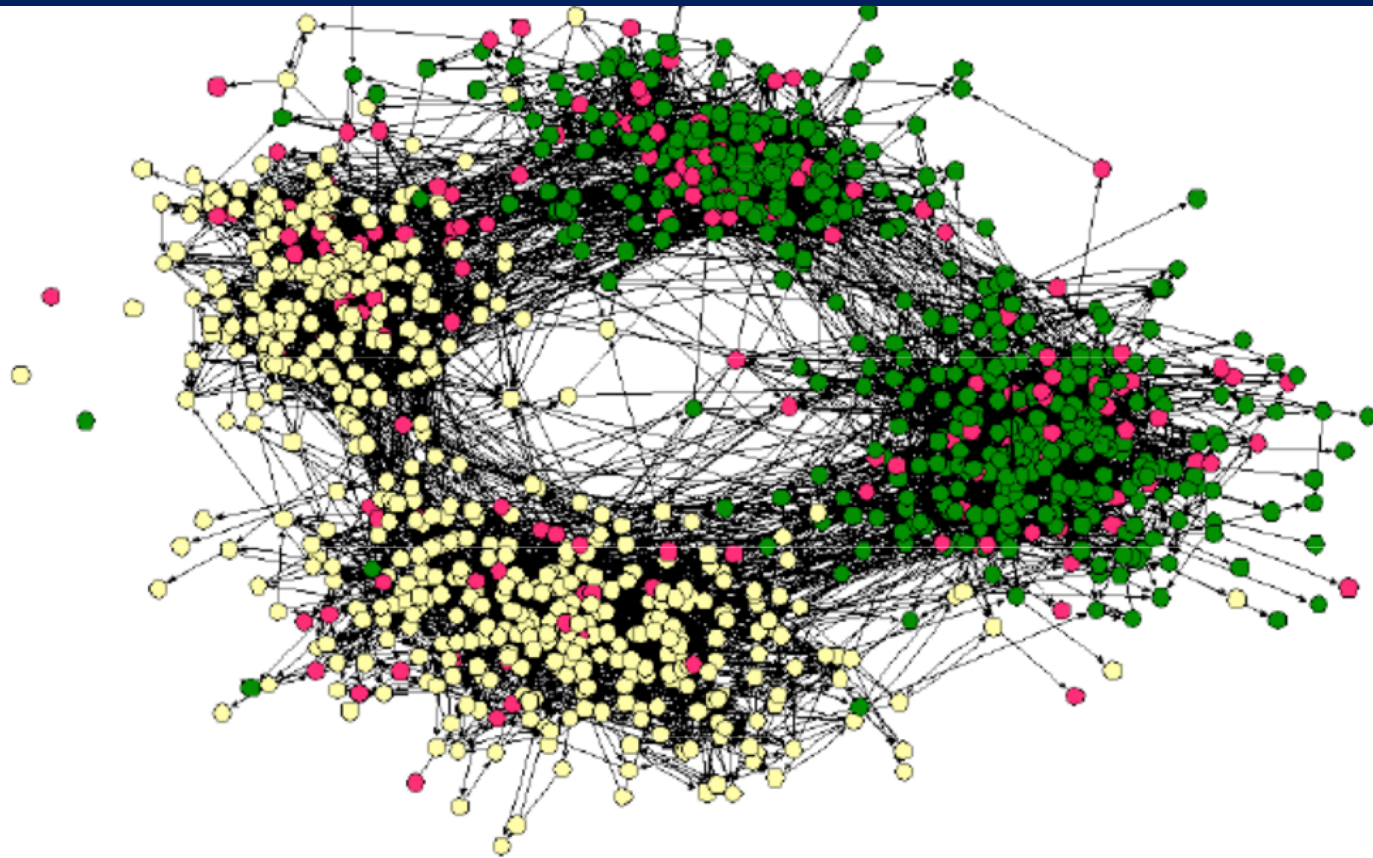
From Wikipedia, the free encyclopedia

Homophily (from **Ancient Greek**: *homou*, 'together' + *philē*, 'friendship, love') is the tendency of individuals to associate and bond with similar others, as in the proverb "birds of a feather flock together."^[1] The presence of homophily has been discovered in a vast array of network studies: over 100 studies have observed homophily in some form or another, and they establish that similarity is associated with connection.^[2] The categories on which homophily occurs include **age**, **gender**, **class**, and organizational role.



Political blog communities

Homophily at action: racial segregation

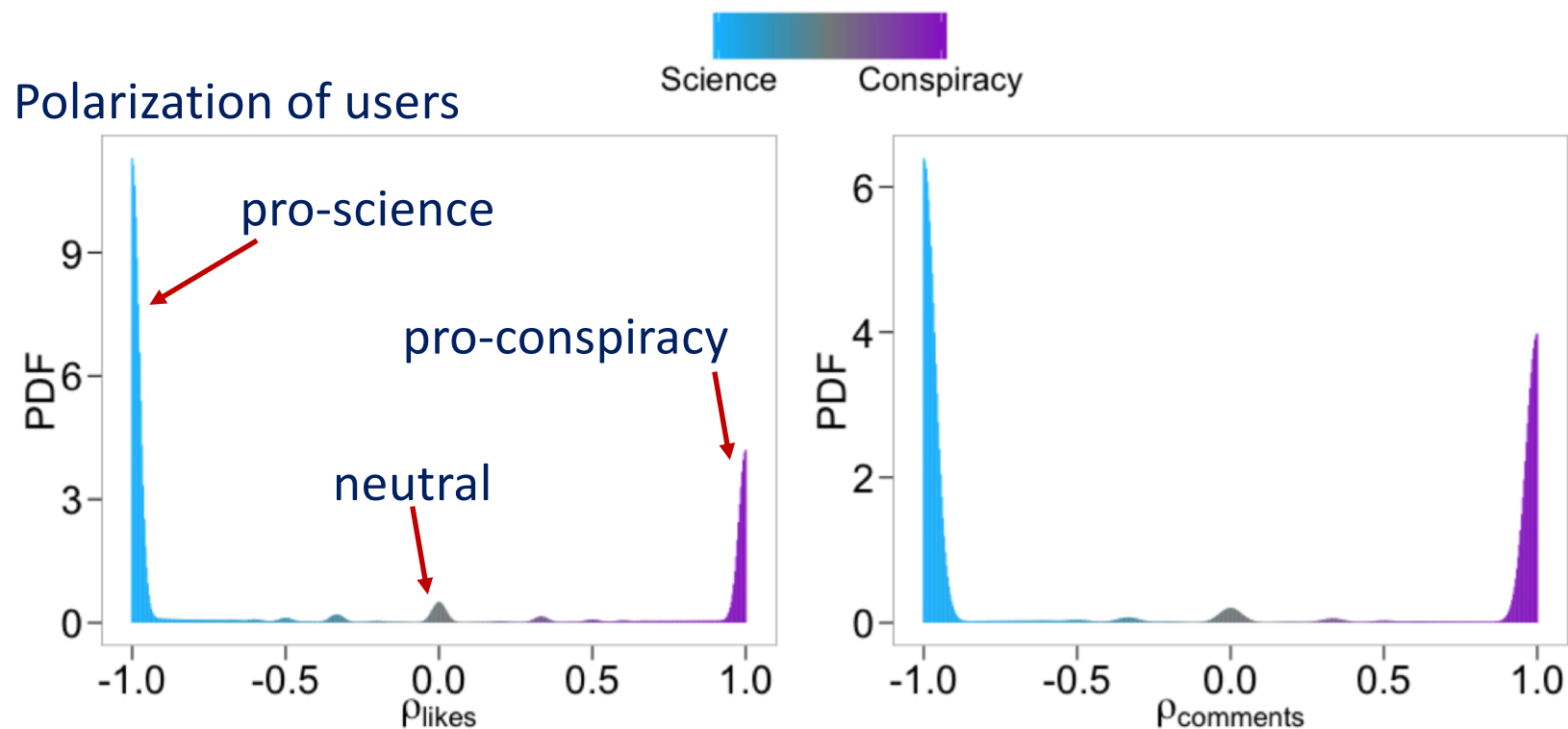


(Easley and Kleinberg, 2010)

Figure 4.1: Homophily can produce a division of a social network into densely-connected, homogeneous parts that are weakly connected to each other. In this social network from a town's middle school and high school, two such divisions in the network are apparent: one based on race (with students of different races drawn as differently colored circles), and the other based on friendships in the middle and high schools respectively [304].

Polarization

The extreme **segregation** of users into homogeneous communities based on their opinion on a controversial topic

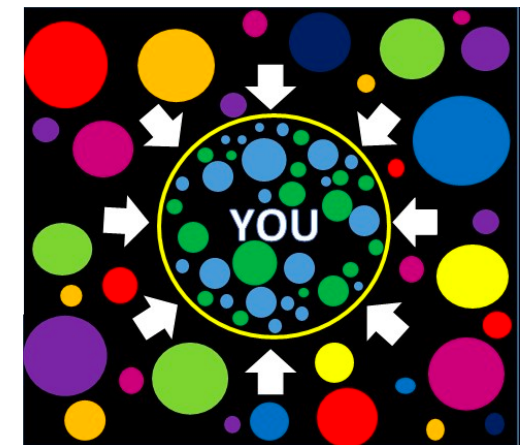


Eco chambers

Echo chamber (media)

From Wikipedia, the free encyclopedia

In **news media**, an **echo chamber** is a metaphorical description of a situation in which **beliefs** are amplified or reinforced by communication and repetition inside a closed system and insulates them from rebuttal.^[1] By visiting an "echo chamber", people are able to seek out information that reinforces their existing views, potentially as an unconscious exercise of **confirmation bias**. This may increase social and **political polarization** and **extremism**.^[2] The term is a metaphor based on the acoustic **echo chamber**, where sounds **reverberate** in a hollow enclosure. Another emerging term for this echoing and homogenizing effect on the Internet within social communities, such as Facebook, Instagram, Twitter, Reddit, etc; is **cultural tribalism**.^[3]



Filter bubbles

Filter bubble

From Wikipedia, the free encyclopedia

A **filter bubble** – a term coined by internet activist [Eli Pariser](#) – is a state of intellectual isolation^[1] that allegedly can result from [personalized searches](#) when a website [algorithm](#) selectively guesses what information a user would like to see based on information about the user, such as location, past click-behavior and search history.^{[2][3][4]} As a result, users become separated from information that disagrees with their viewpoints, effectively isolating them in their own cultural or ideological bubbles.^[5] The choices made by these algorithms are not transparent.^[6] |



The term was coined by internet activist [Eli Pariser](#) circa 2010

Assortativity (degree homophily)

A.L. Barabási, Network science, <http://barabasi.com/networksciencebook>

Ch.7 “Degree correlation”

Correlation between hubs

- In some networks, hubs frequently **connect** with other hubs

e.g., celebrity dating, actor networks



- In other cases hubs **avoid** connections with other hubs

e.g., metabolic graphs, food webs (predators tend to differentiate their diet)

Assortativity

- ❑ **Assortative** network: high degree nodes connect with each other avoiding low degree nodes (tend to cliques)
- ❑ **Disassortative** network: opposite trend, hubs tend to avoid each other
- ❑ **Neutral** network: one with random wiring, i.e., aside from the (marginal) degree distribution of nodes, there is no correlation

Assortativity

(dis)assortativity in sociology quantifies homophily in social networks, e.g., effects like:

- ❑ Rich people tend to be friends with each other
- ❑ People with the same education tend to hang out together

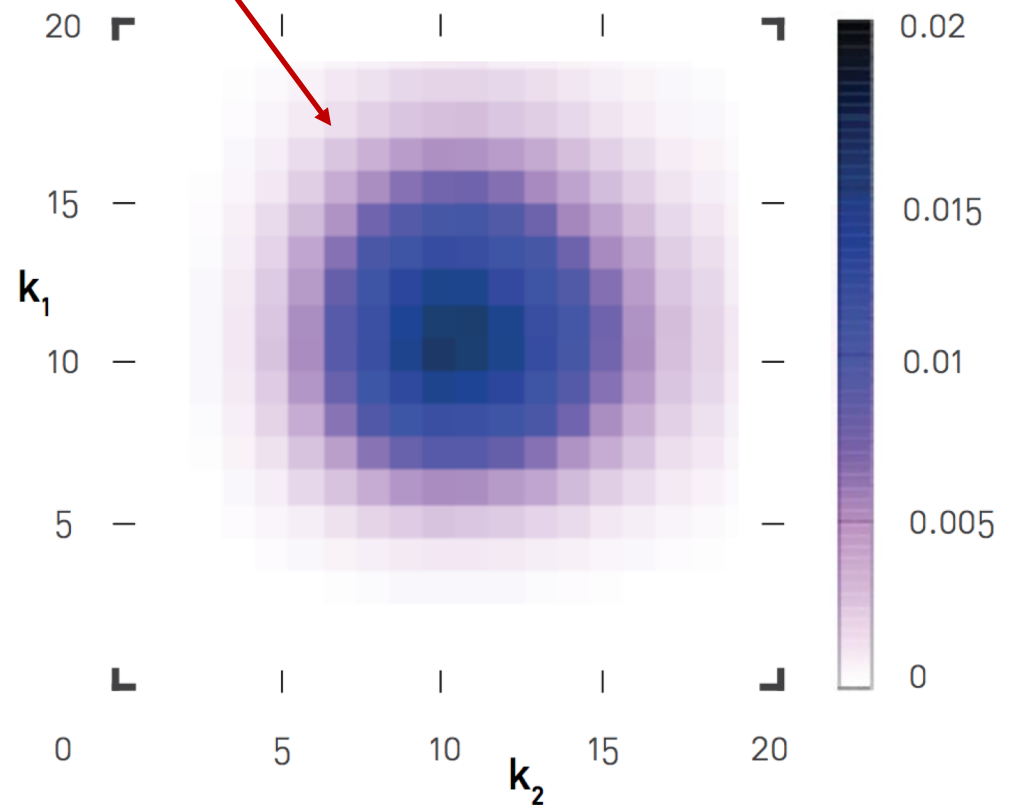
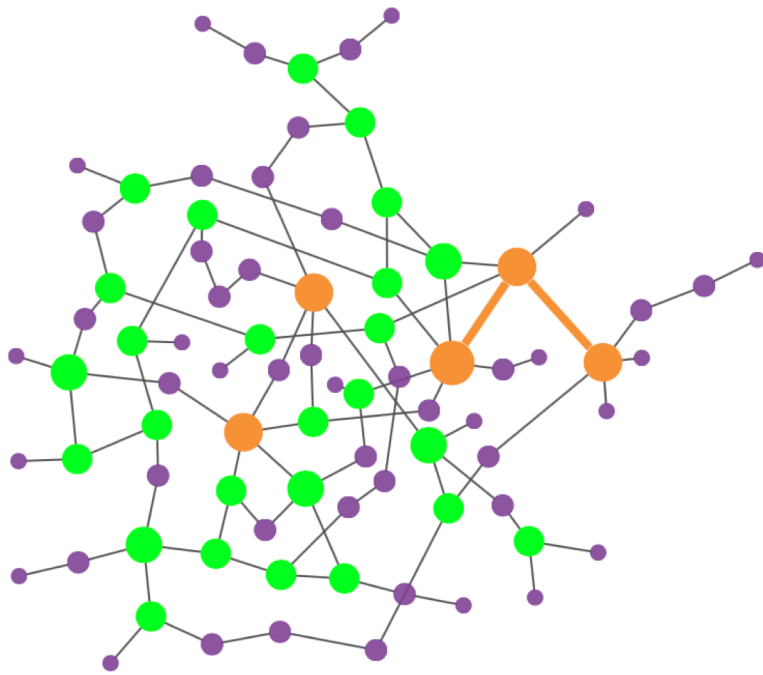
i.e., we expect social networks to be assortative

Neutral networks

The **degree correlation matrix** E_{k_1, k_2} is visually centred around the average degree

In the neutral case we expect $E_{k_1, k_2} = q_{k_1} q_{k_2}$, i.e., independence

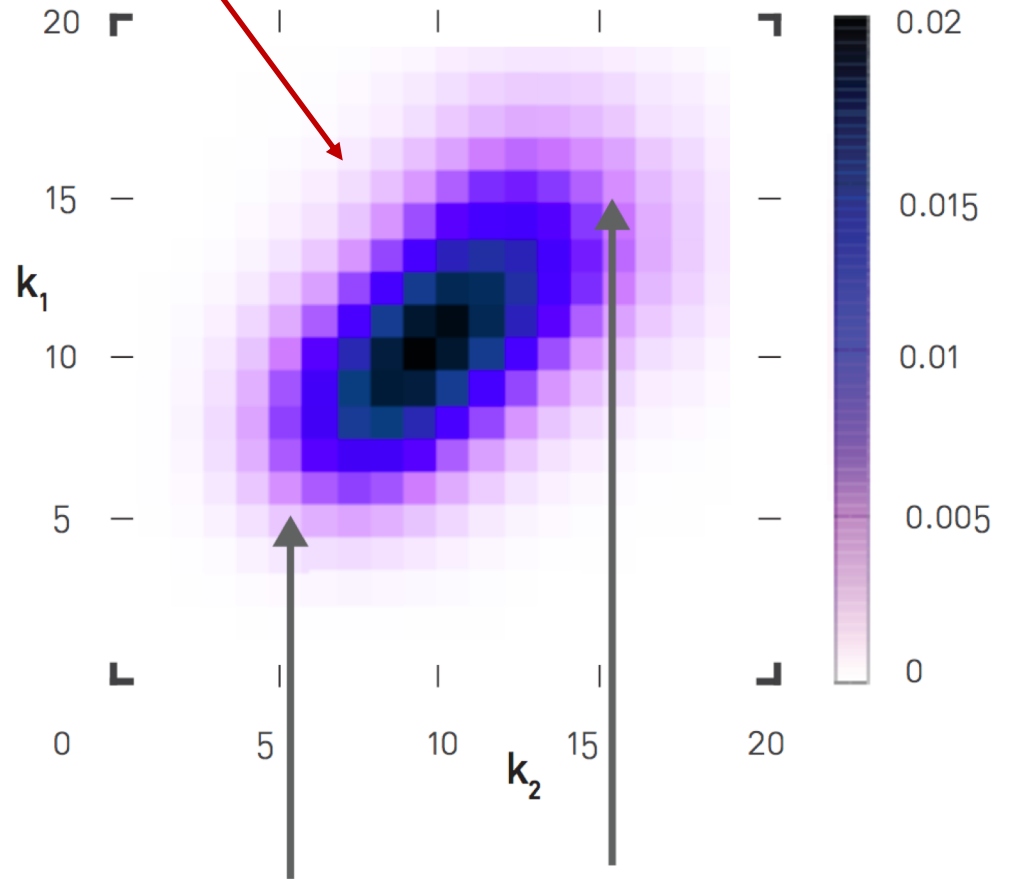
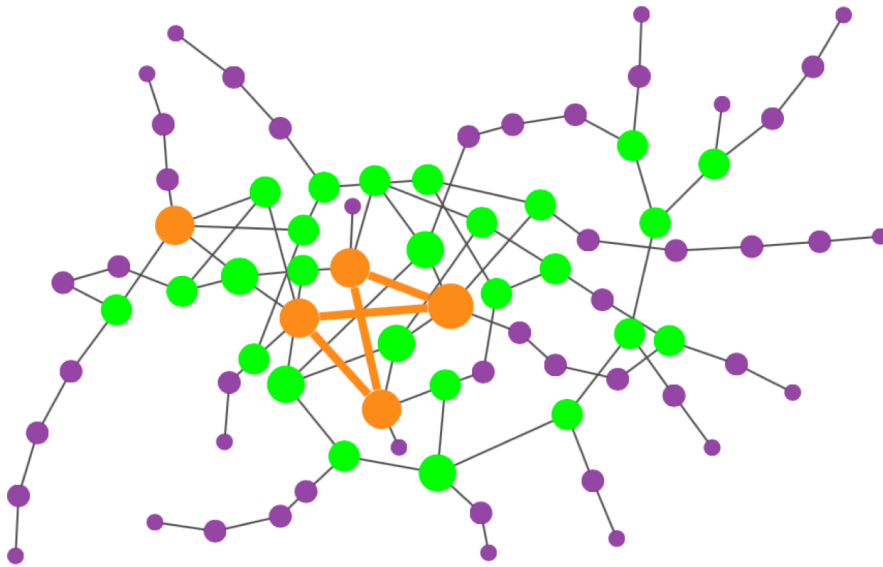
NEUTRAL



Assortative networks

The degree correlation matrix E_{k_1, k_2} is turning to the right

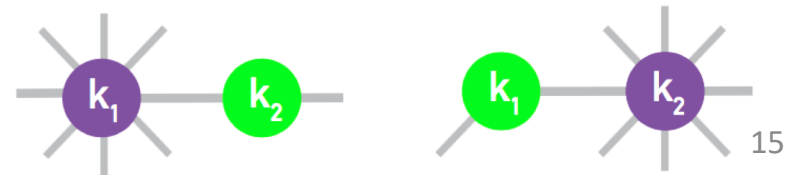
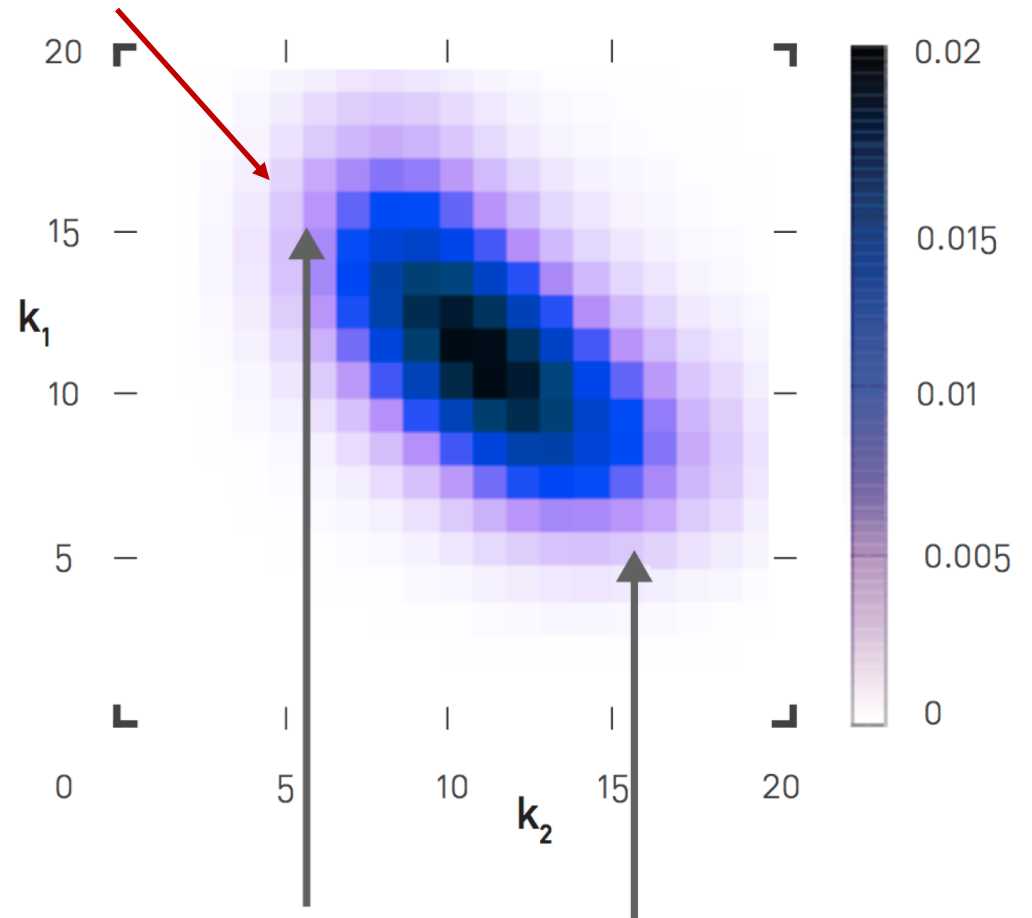
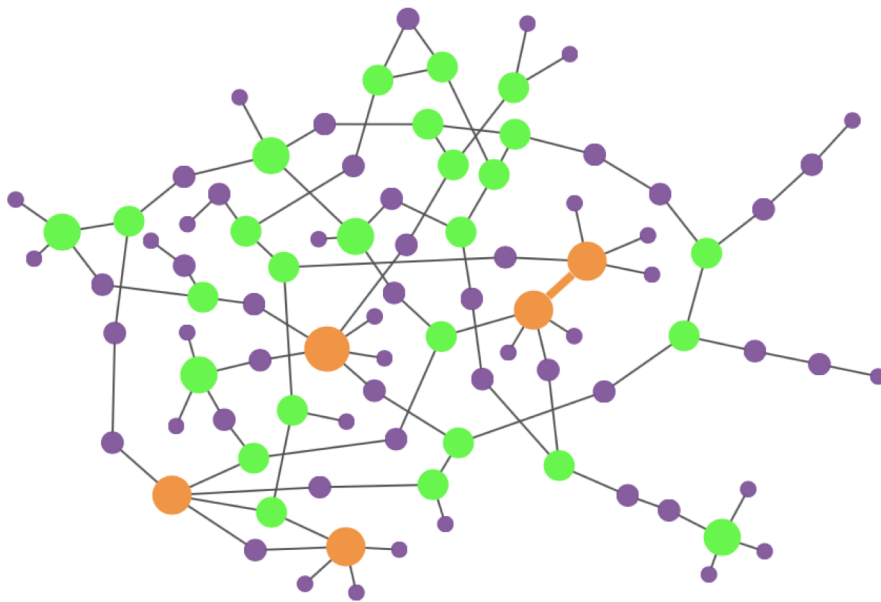
ASSORTATIVE



Disassortative networks

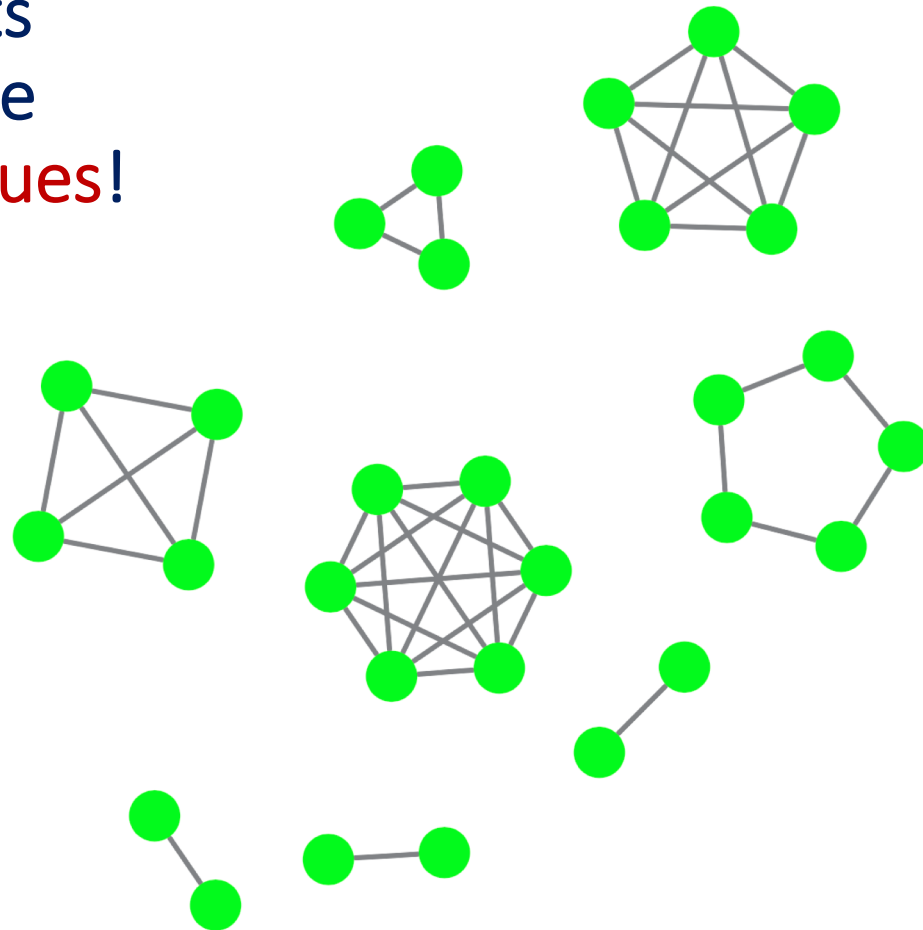
The degree correlation matrix E_{k_1, k_2} is turning to the left

DISASSORTATIVE



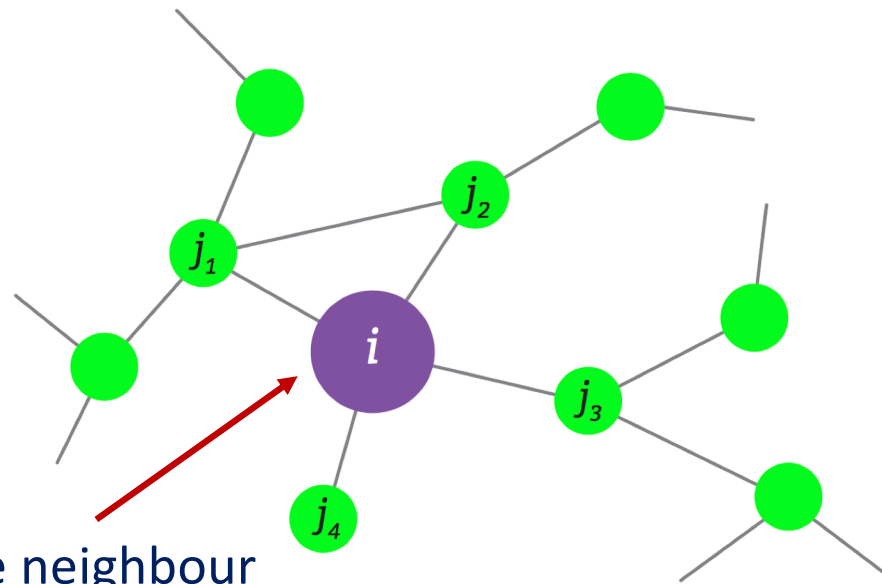
Perfect assortativity

- Each node connects only to nodes of the same degree = **cliques!**



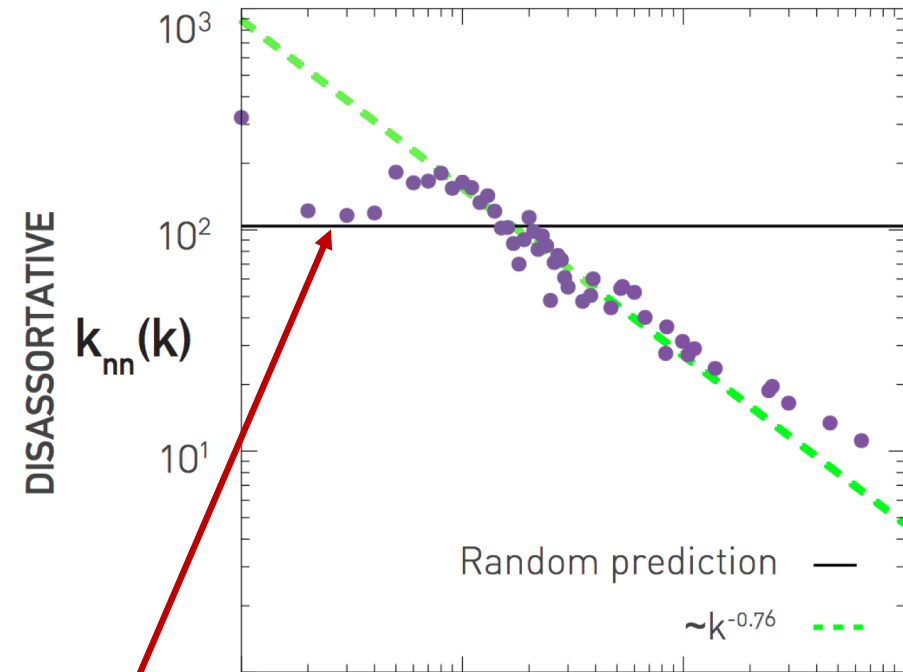
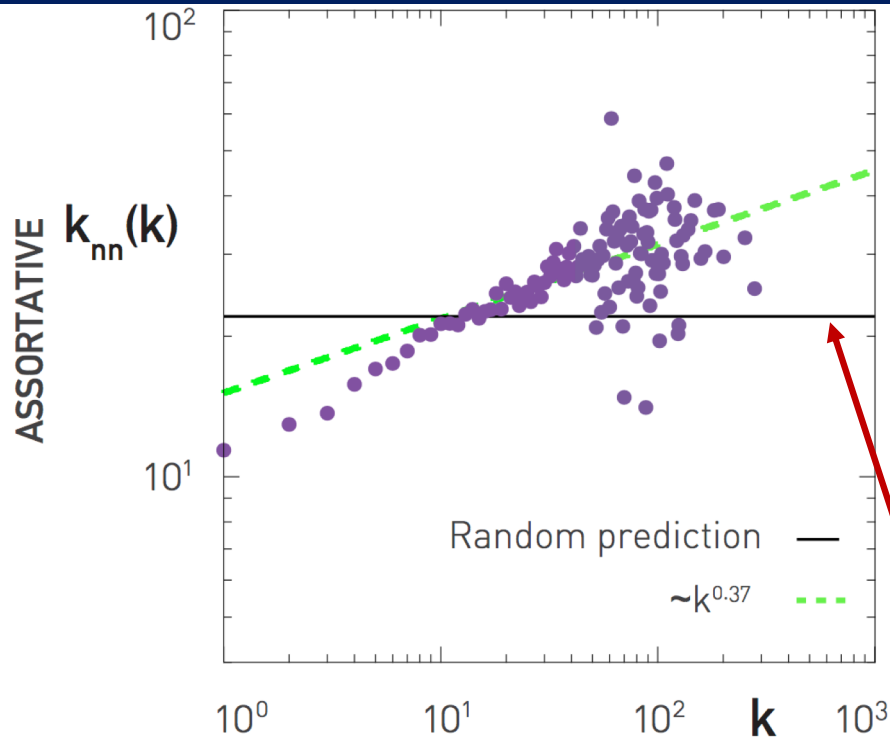
Nearest neighbour degree

- **Idea** : inspect the degrees of the **neighbouring** nodes (easier than matrices)



average neighbour
degree of node i is
 $\frac{1}{4} (4 + 3 + 1 + 3) = 2.75$

Examples



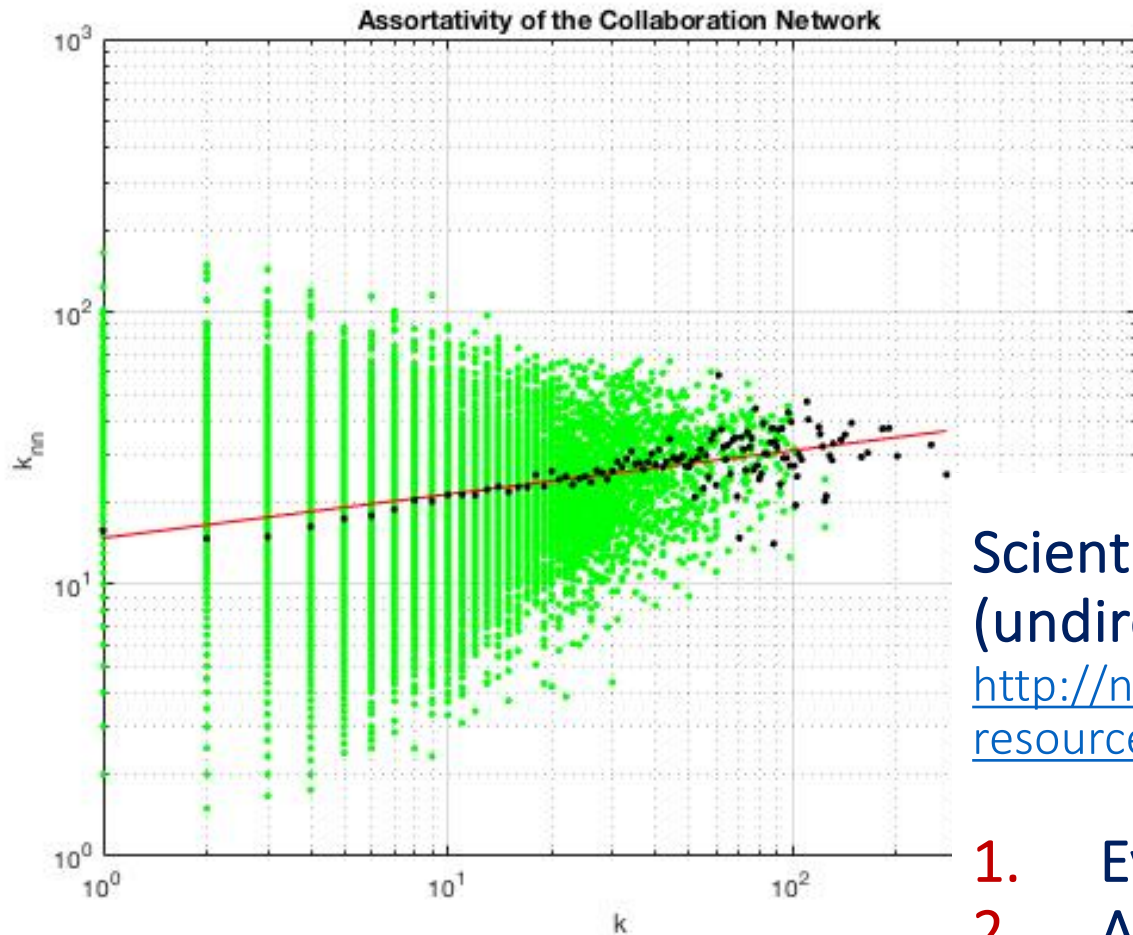
constant = independent of the degree (i.e., random = neutral)

$$\ln(k_{nn}) = \mu \ln(k_i) \quad \rightarrow$$

$\mu > 0 =$ assortative

$\mu < 0 =$ disassortative

Scientific collaboration network

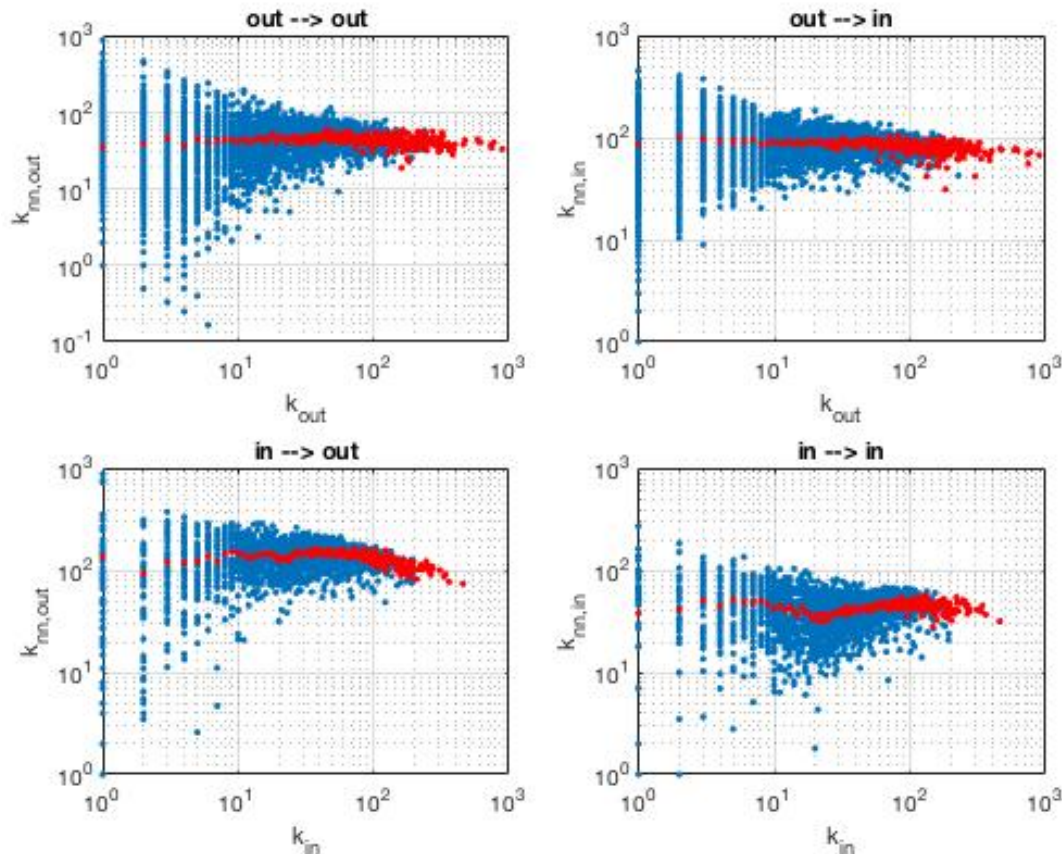


Scientific collaboration network
(undirected, assortative)

<http://networksciencebook.com/translations/en/resources/data.html>

1. Evaluate average neigh. deg. k_{nn}
2. Average w.r.t. k
3. Extract the assortativity value $\mu=0.16$

Wikipedia voting dataset



Wikipedia voting dataset
(directed, **neutral**)

<https://snap.stanford.edu/data/wiki-Vote.html>

averages are taken w.r.t. in/out degrees for in/out neighbours

μ	in	out
in	0.0127	-0.083
out	-0.063	-0.027

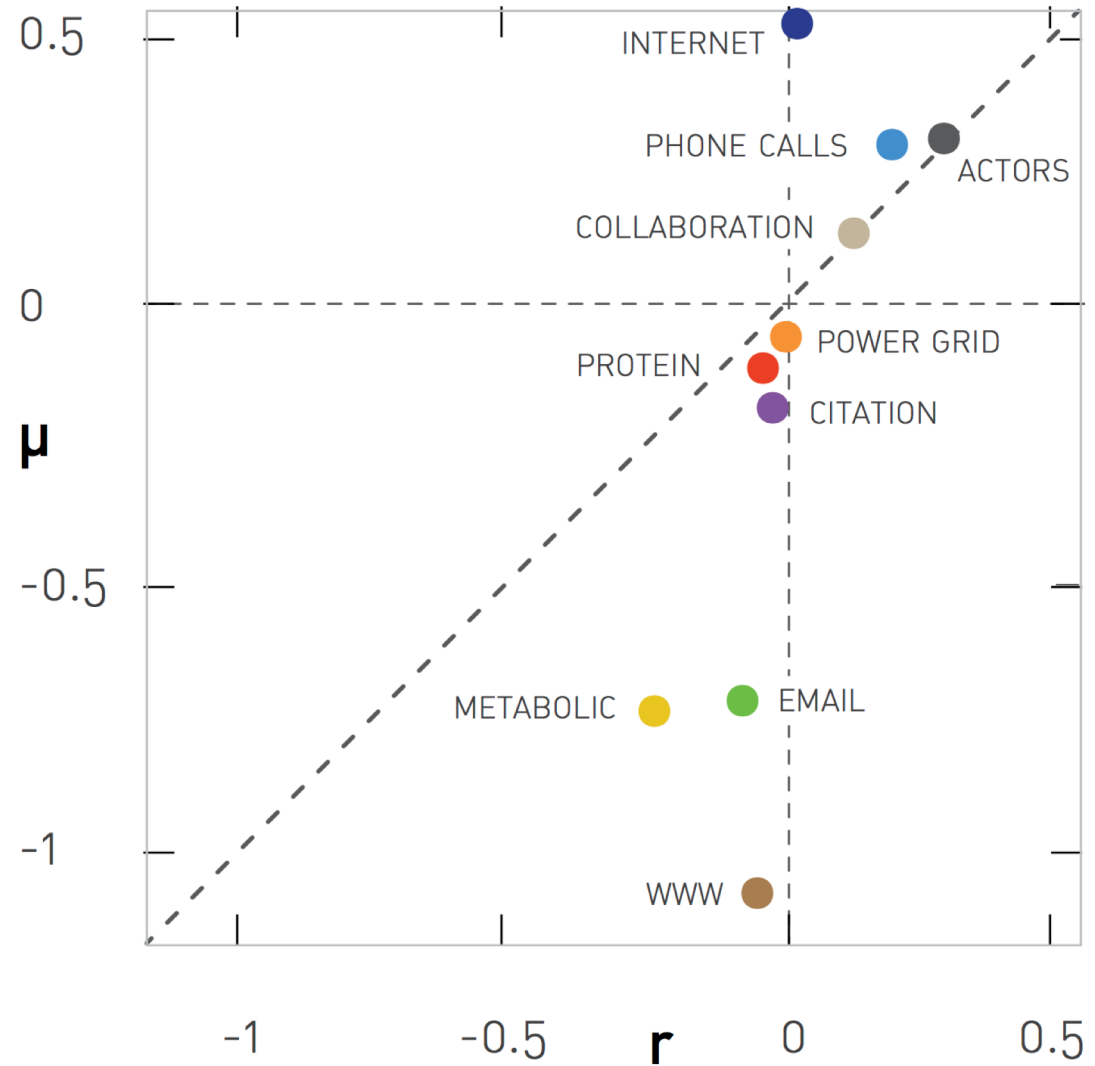
Alternative parameter

Pearson correlation coefficient $r = \text{cov}/\sigma^2$

- E_{ki} is the degree correlation matrix
- $q_k = \sum_i E_{ki}$ is the degree probability
- $m = \sum_k k q_k$ is the mean
- $\sigma^2 = \sum_k k^2 q_k - m^2$ is the variance
- $\text{cov} = \sum_{k,i} ki E_{ki} - m^2$ is the covariance

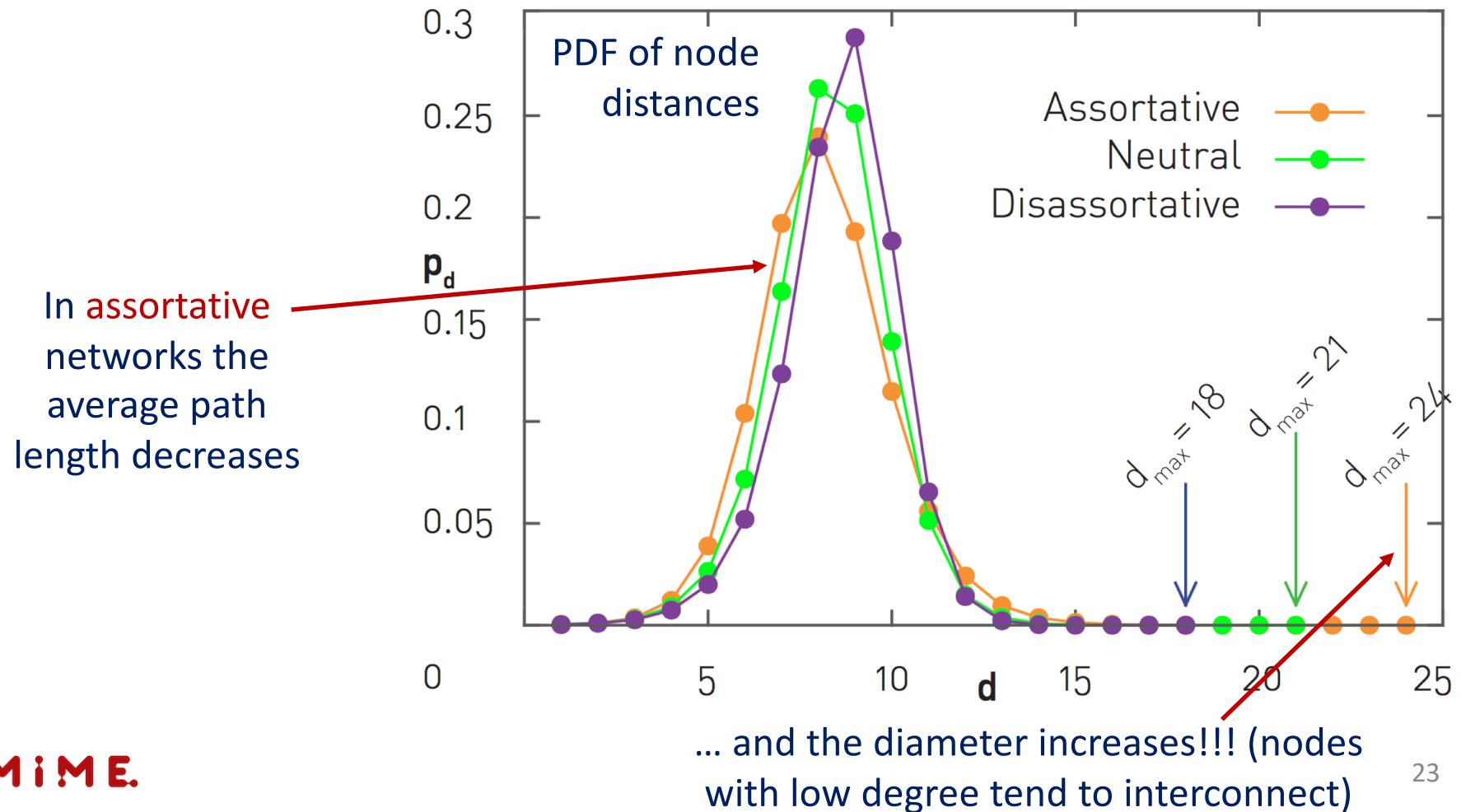
Comparing the views

- ❑ linear model
 $r = \mu k$? Not really
- ❑ Correlation between the signs of r and μ
- ❑ But μ is a more reliable measure



Implications of assortativity

(dis)assortativity influences the path length and the network diameter



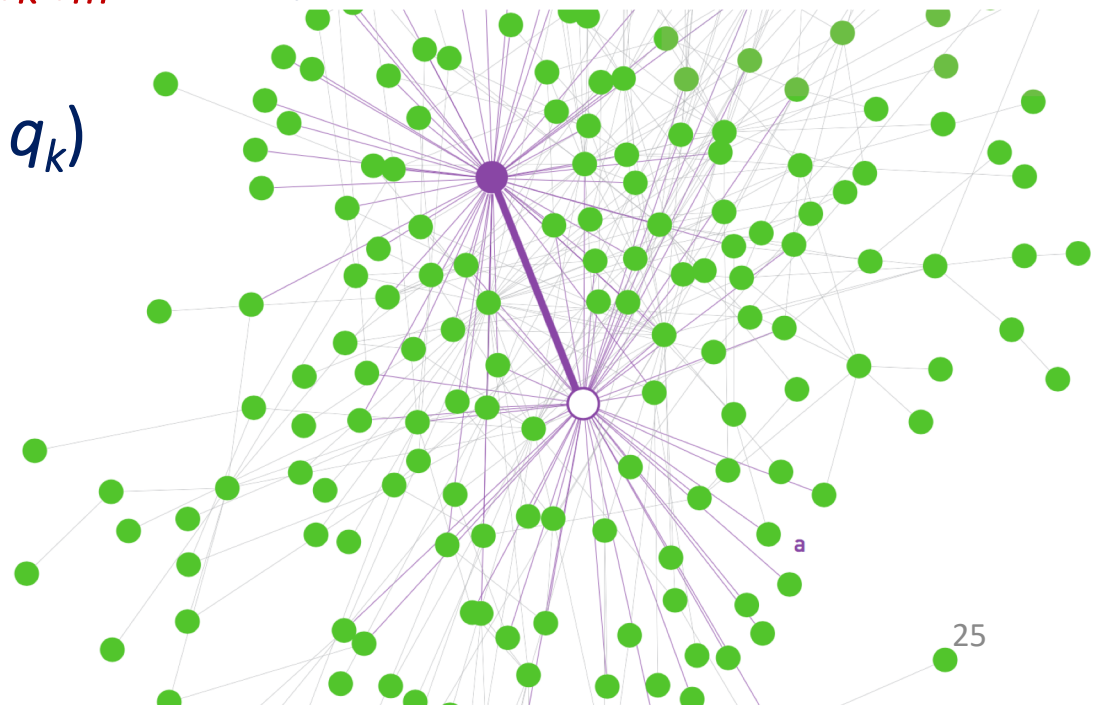
Structural Disassortativity

Rationale for (dis)assortativity

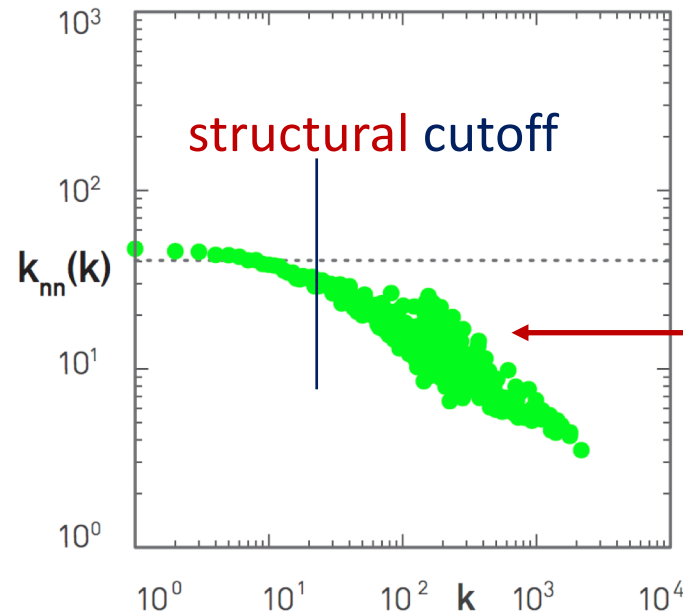
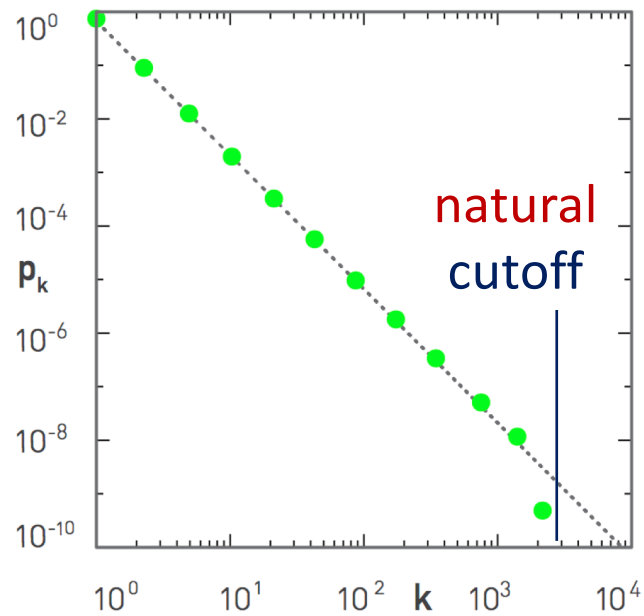
(dis)Assortativity can be linked to **structural** network properties:

- e.g., if no multi-links and self-loops allowed then the network cannot be **neutral**
- if neutral \rightarrow the # of expected links between nodes of degree k and m is $2L q_k q_m$, easily > 1 (i.e., multi-links)
- likely to happen with **hubs** (they have large q_k)

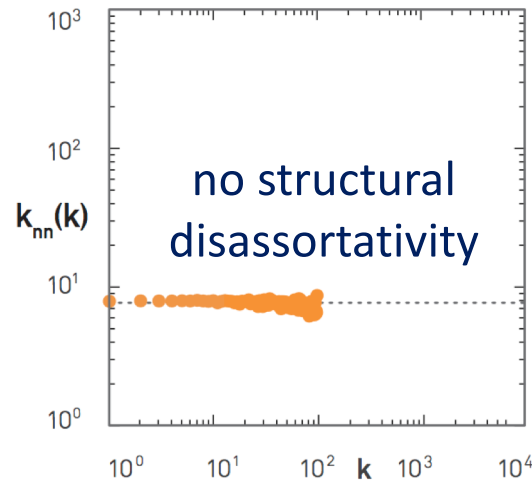
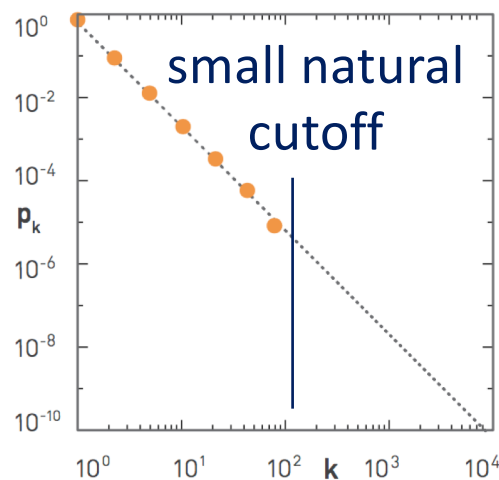
**structural
disassortativity**
when the effect is
seen on hubs



Structural vs natural cutoffs



structural disassortativity
large degrees cannot be supported by a neutral network



Approximate analysis

Structural **disassortativity** in the range $[k_s, k_{\max}]$

- ❑ $k_{\max} = k_{\min} N^{1/(\gamma-1)}$ **natural** cutoff (largest degree)
- ❑ k_s **structural** cutoff (practical limit after which the network cannot be neutral)

Structural cutoff

- ❑ Molloy-Reed model (easier to treat) ↗ trials
- ❑ probability of a link is $p_{ij} = k_i \cdot k_j / 2L$ ← probability of a trial
- ❑ depends on node **degrees** only = (much) larger for hubs
- ❑ link of **probability one** for hubs of degree

$$k_s = (2L)^{1/2} = (\langle k \rangle N)^{1/2}$$

Structural effect wrap-up

Natural vs structural cutoffs

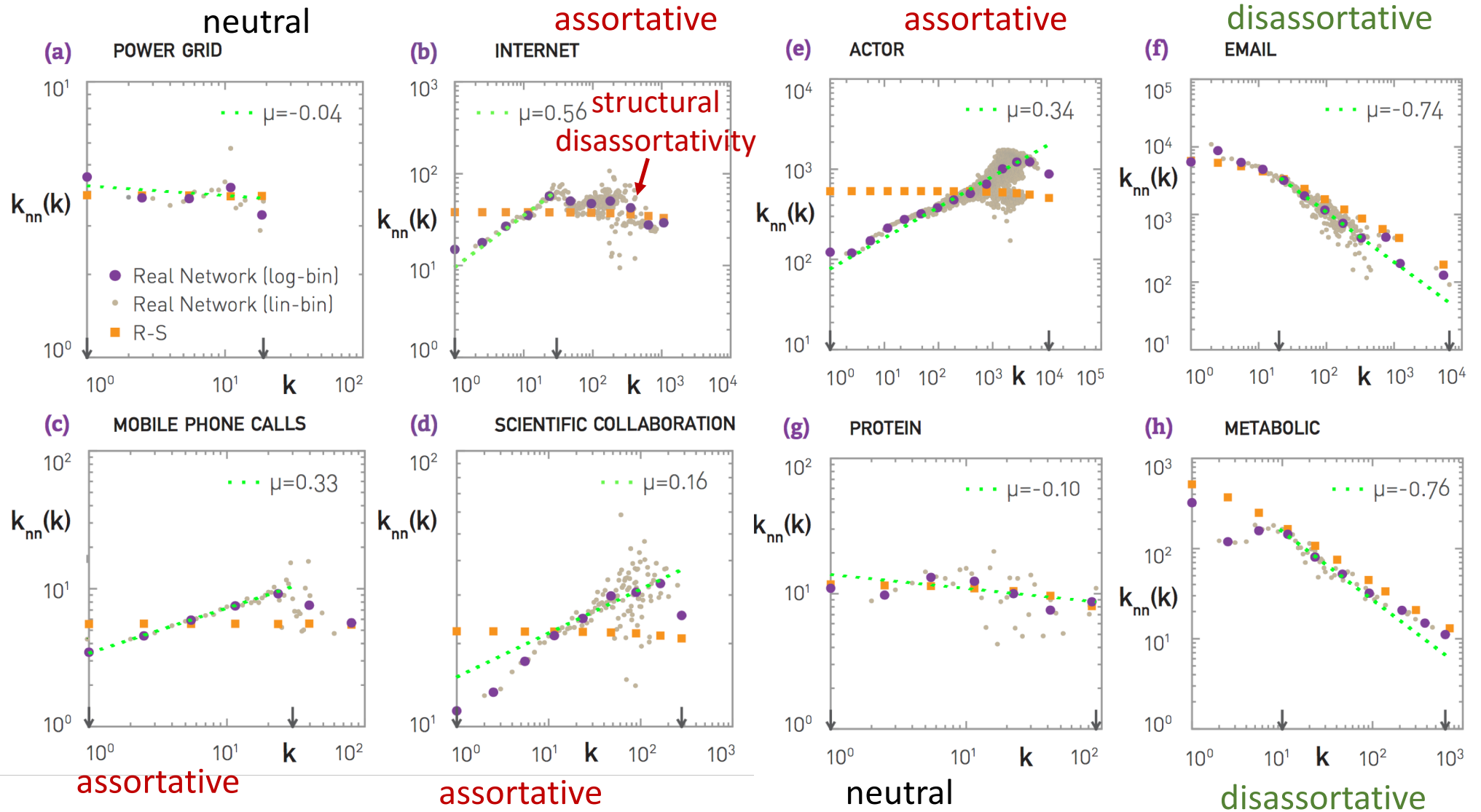
□ $k_{\max} = k_{\min} N^{1/(\gamma-1)}$

□ $k_S = (\langle k \rangle N)^{1/2}$

$k_S < k_{\max}$ for $\frac{1}{2} < 1/(\gamma-1)$, that is, $\gamma < 3$

- structural **disassortativity** is active only in the **ultra-small-world regime**
- **random** graphs ($\gamma \geq 3$) do not have structural cutoff, i.e., they are **neutral**

Real networks



Randomization curve

Real networks may look as disassortative because

- ❑ they really involve **disassortative** effects
- ❑ they **do not** but just have it as structural

Check with the yellow R-S curve (**null model/unbiased**):

- ❑ it is a **degree preserving** randomization
- ❑ at each randomization step we check that we do not have more than one link between any node pairs
- ❑ obtained for 100 independent trials
- ❑ If k_{nn} does not change → **disassortativity** is due to a **structural** reason (i.e., on the degree distribution)
- ❑ if something changes → deeper reasons

Eco-chamber effect

Cinelli, Morales, Galeazzi, Quattrociocchi, Starnini (2020)
Echo chambers on social media: A comparative analysis
<https://arxiv.org/pdf/2004.09603.pdf>

Definition of echo-chamber

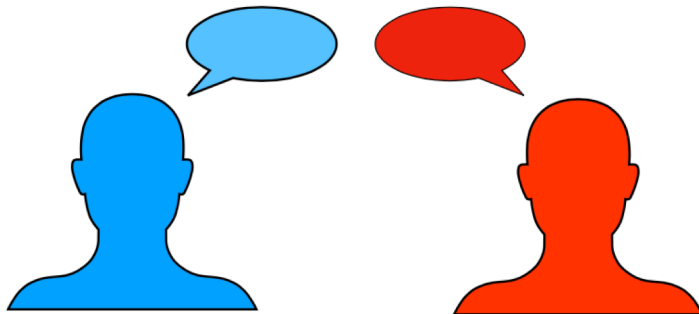
Coexistence of

- ❑ opinion **polarization** with respect to a controversial topic
- ❑ **homophily** in interactions

To assess **polarization**



Measure **individual leaning**



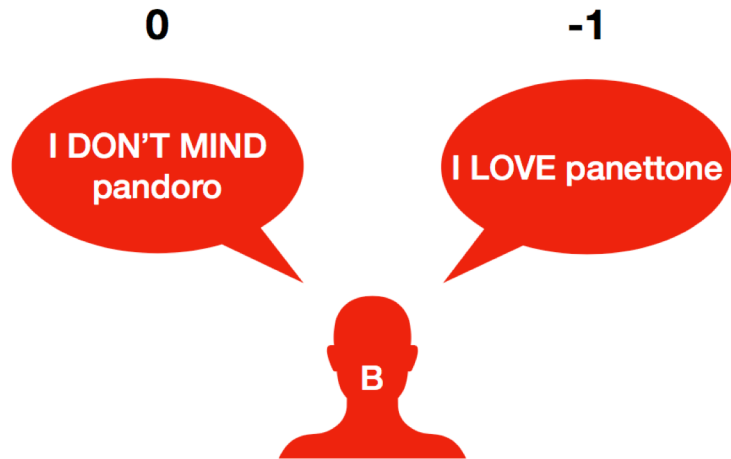
To quantify **homophily**



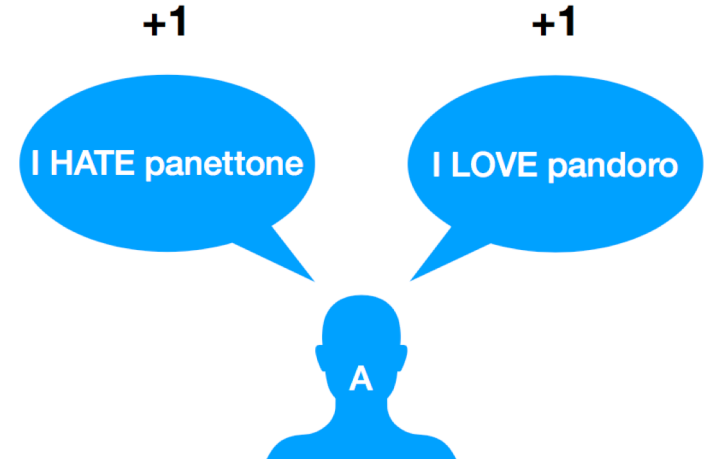
Build **interaction network**



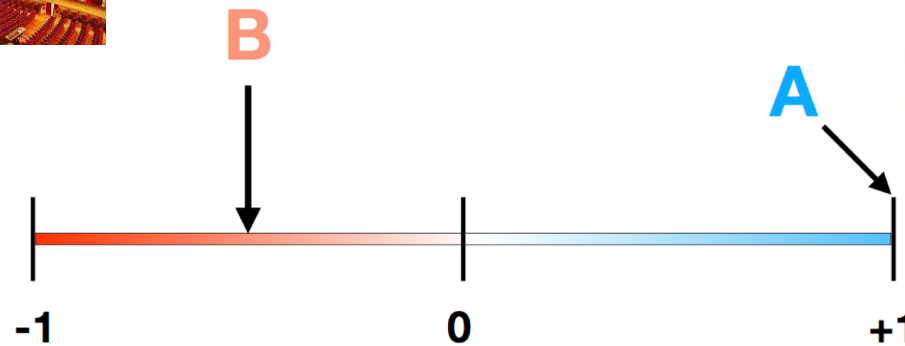
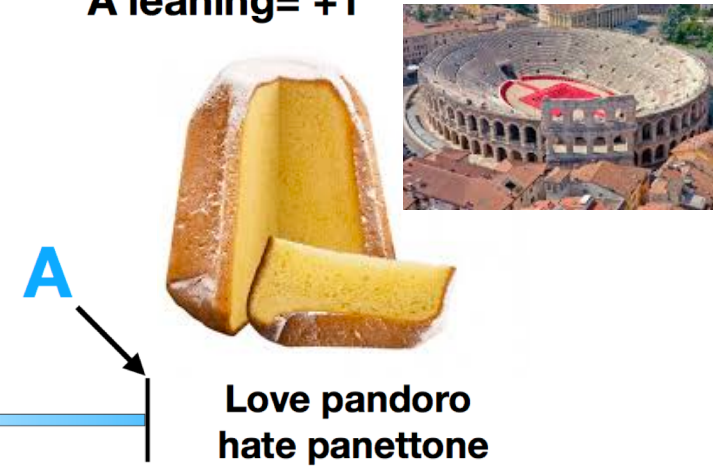
Users' leaning



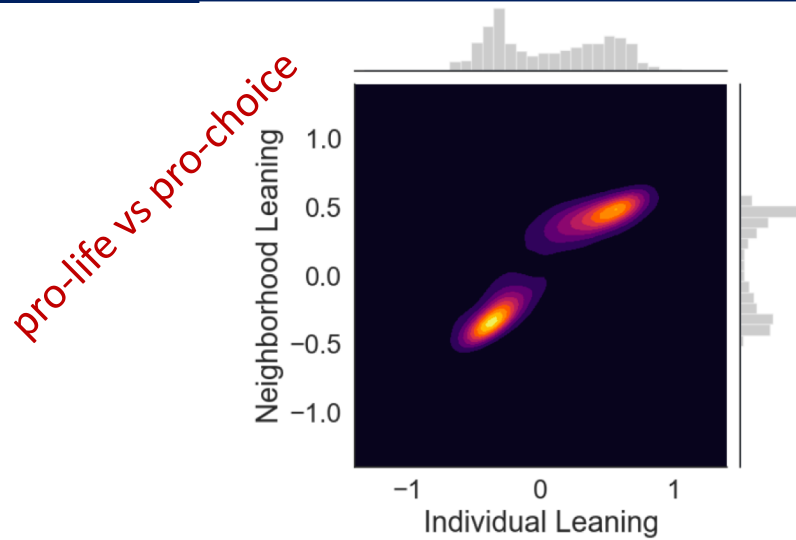
B leaning= -0.5



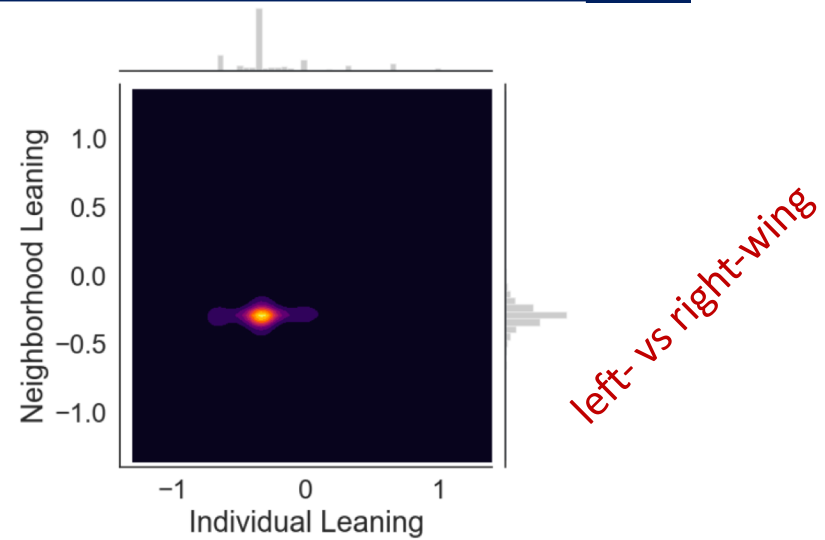
A leaning= +1



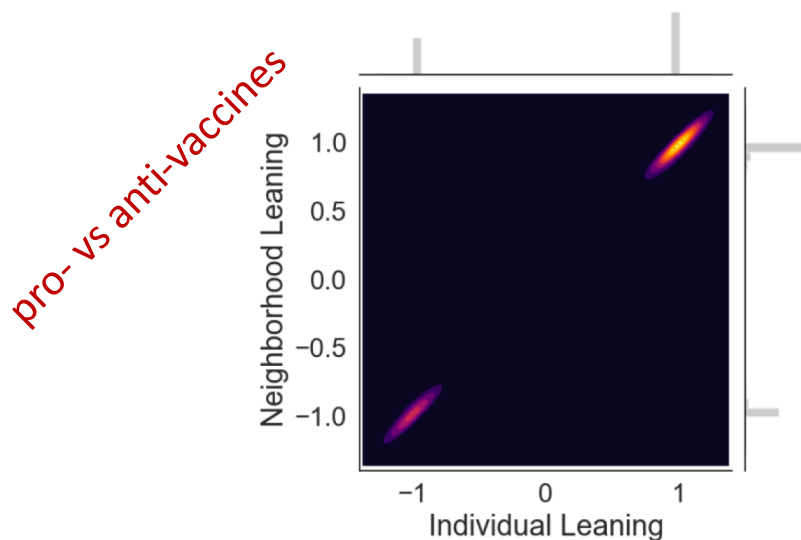
Echo-chamber effect in social networks



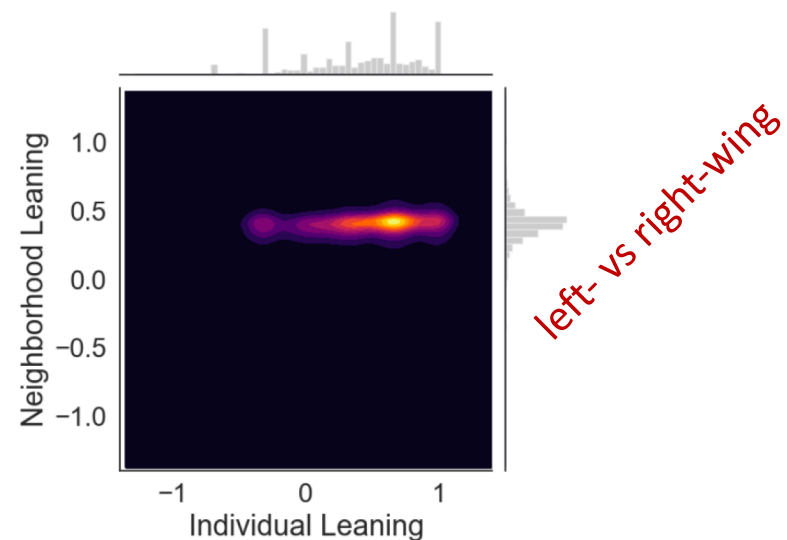
(a) Twitter



(b) Reddit



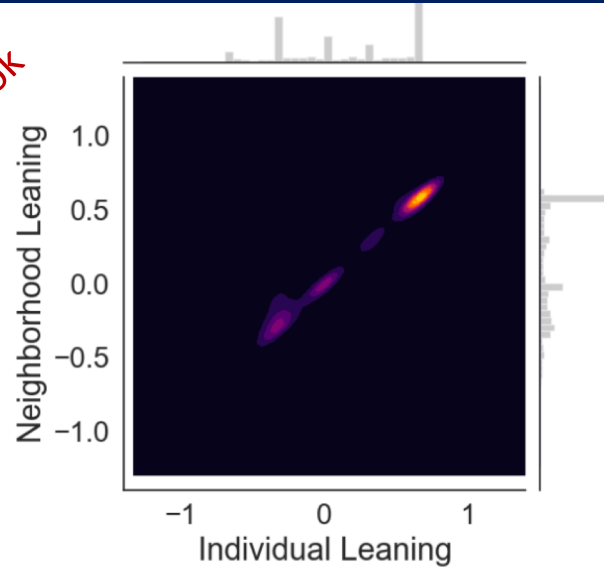
(c) Facebook



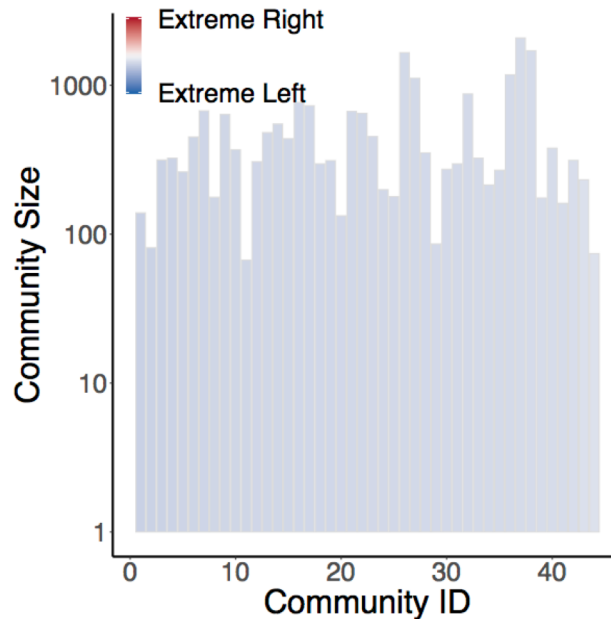
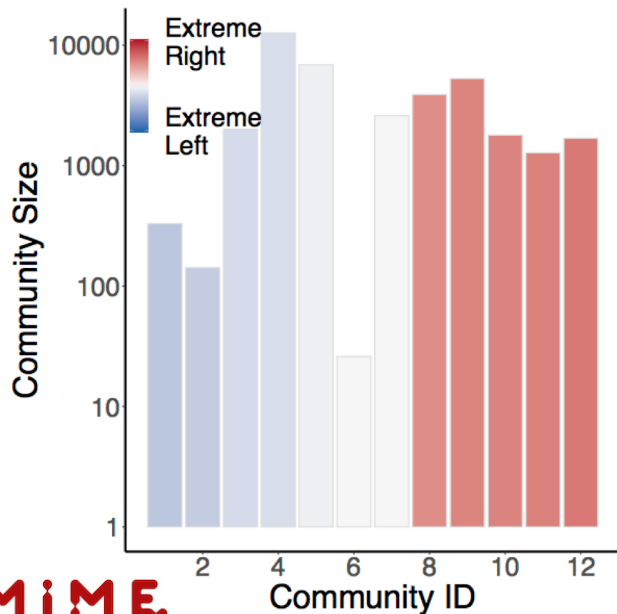
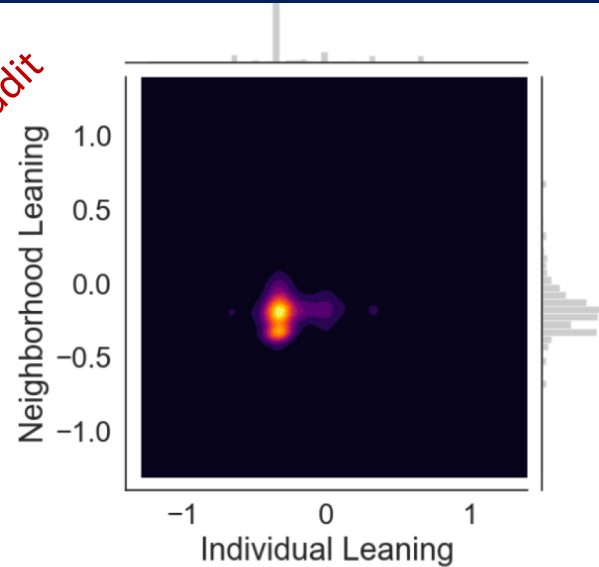
(d) Gab

Political leaning

FaceBook



Reddit



- ❑ Same Topic: **News**
- ❑ Same leaning assigned to **news sources**
- ❑ Different platforms: Facebook has a strong **social feeding algorithm**, Reddit has not
- ❑ Different characteristics: Facebook shows **segregation** among groups with different leaning, Reddit has one group

Polarization in pro-life/pro-choice networks

Lejla Dzanko, Giulia Rizzoli, Sanja Milijanovic, Sara Shena, Lara Malin Schwarz
IP3 2019/20

Background

Abortion is one of the most controversial topics in social public, political and scientific debates in different disciplines

Often debates result in reforms of the law → USA 2019

Two movements:

- ❑ **Pro-Life**: every human (embryo) has the right to live; abortion is murder → goal to ban it
- ❑ **Pro-Choice**: every woman should have the right to decide what to do with her body on her own → goal to keep abortion safe and legal

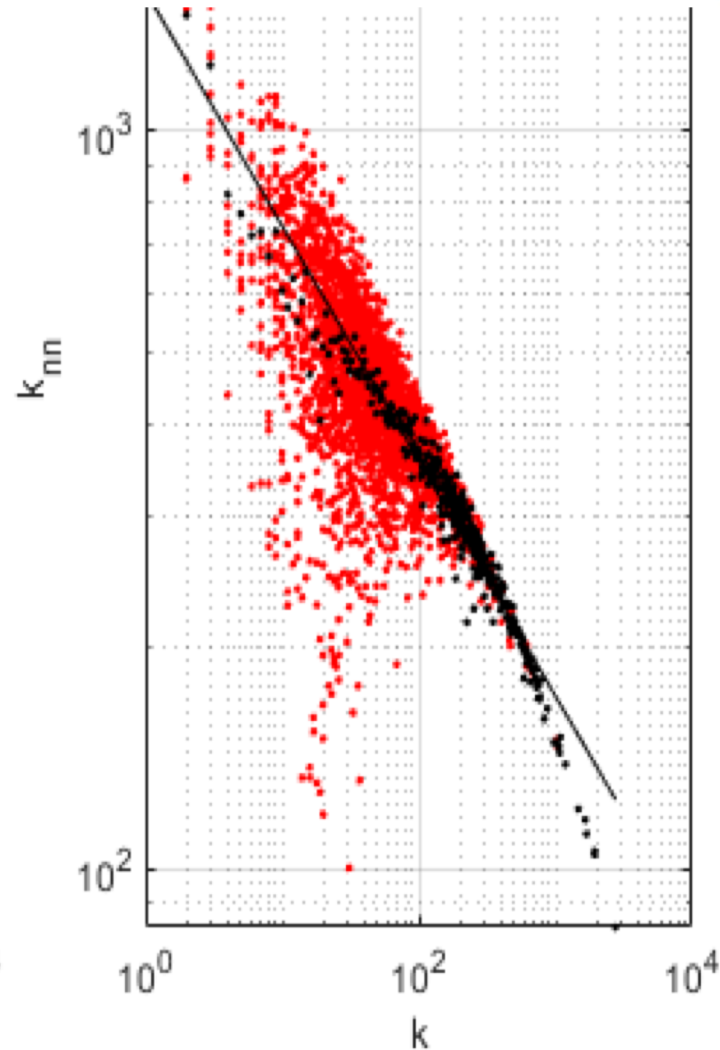
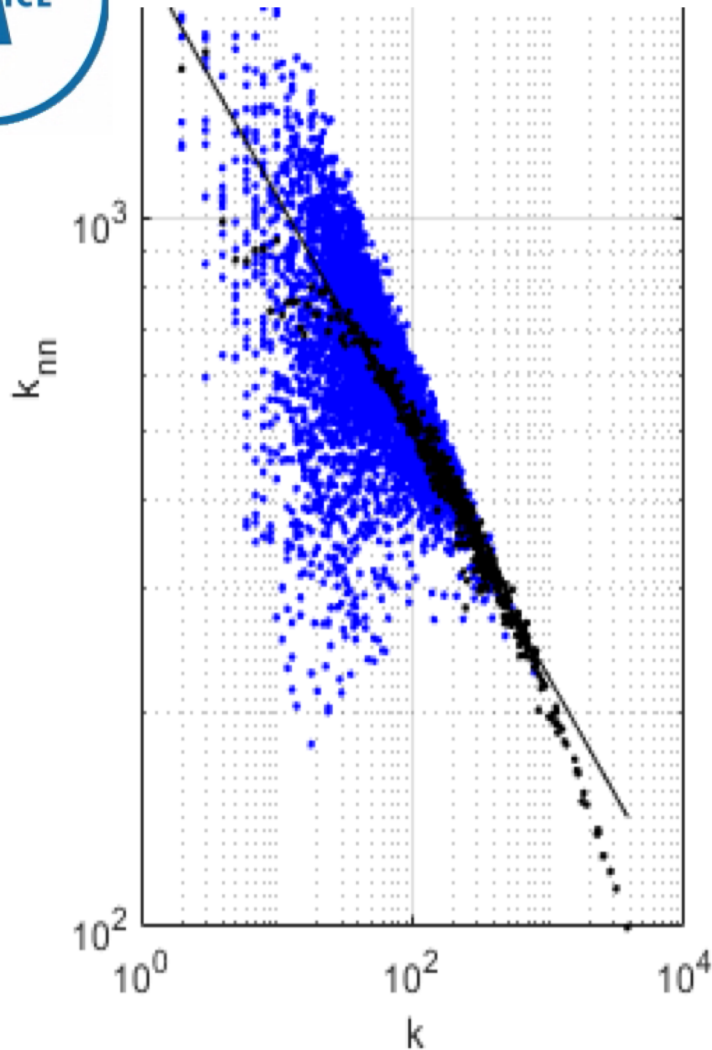


Data collection

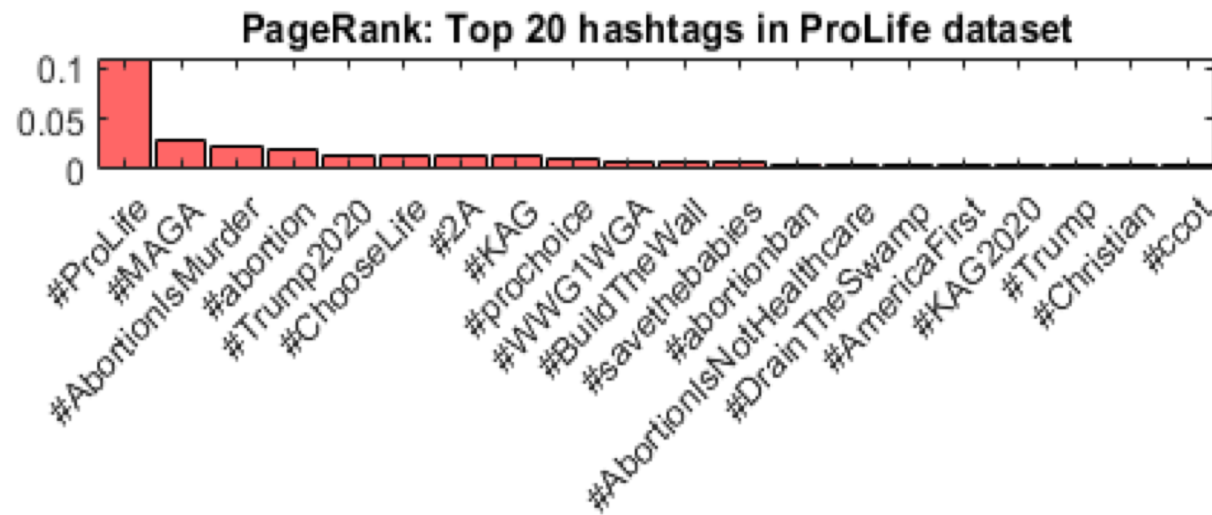
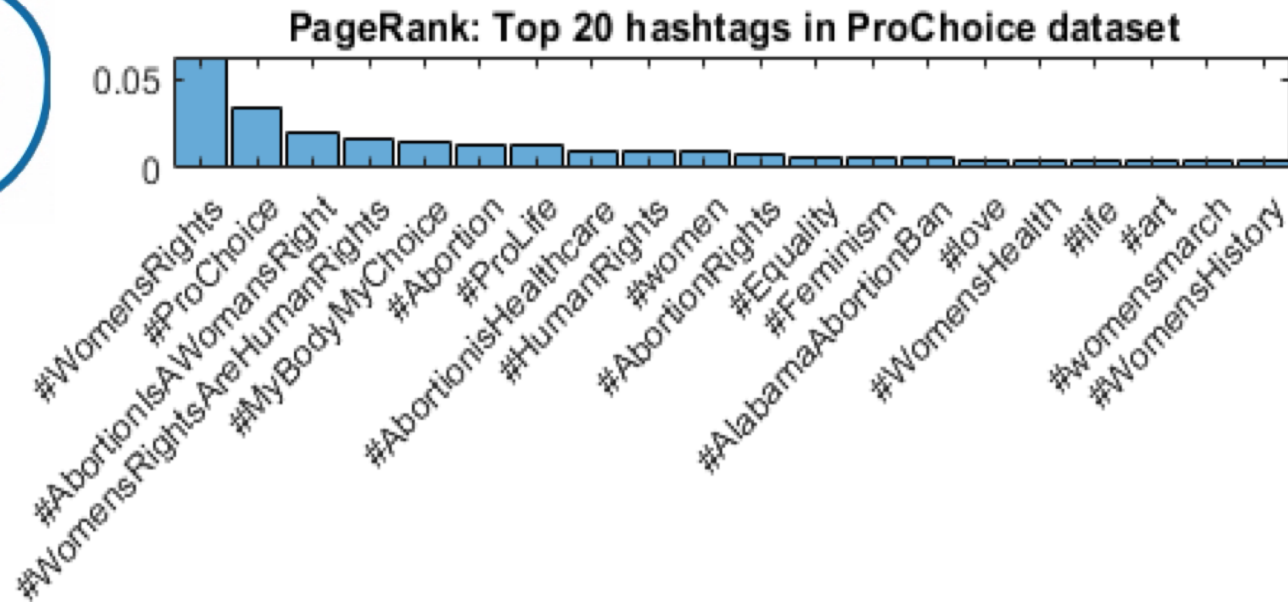


Pro-Choice	Pro-Life
<p>#prochoice #mybodymychoice #abortionishealthcare #abortionisawomansright #abortionrights #abortionismurder #abortionssupportnetwork #proabortion</p>	<p>#prolife #savethebabies #babiesarehuman #chooselife #abortionban #abortionismurder #lovethemboth #whywemarch</p>

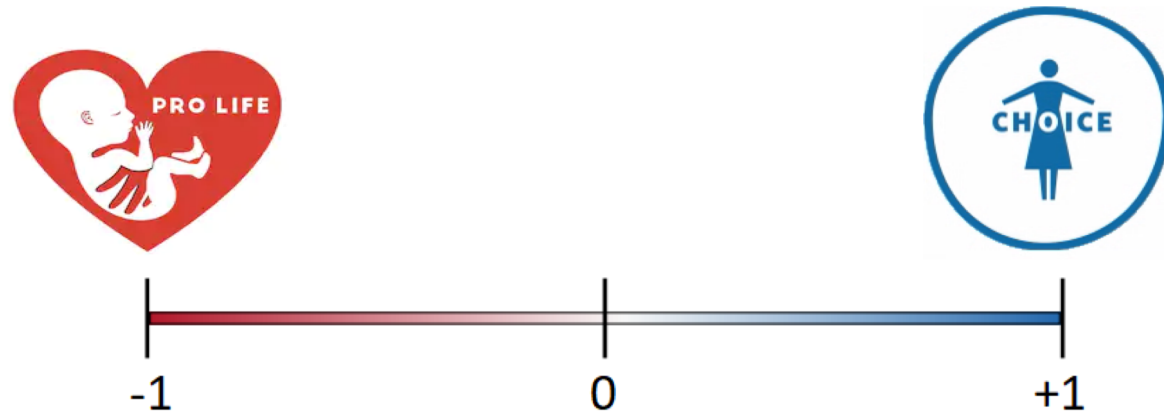
Hashtag network disassortativity



PageRank centrality



Hashtag polarization

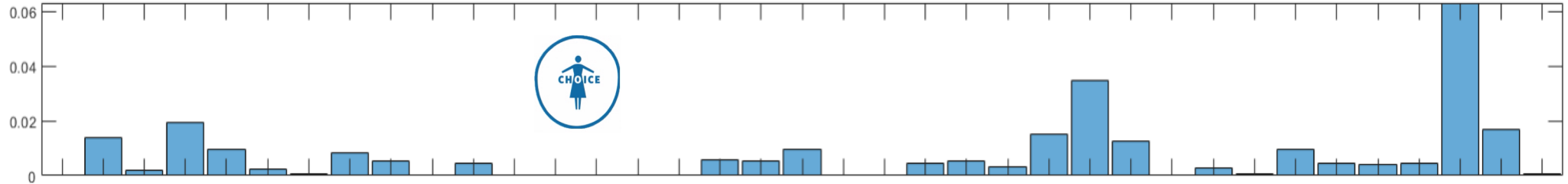


- Measure of hashtags centralities among the two dataset
- Extract which **opinion** an hashtag holds

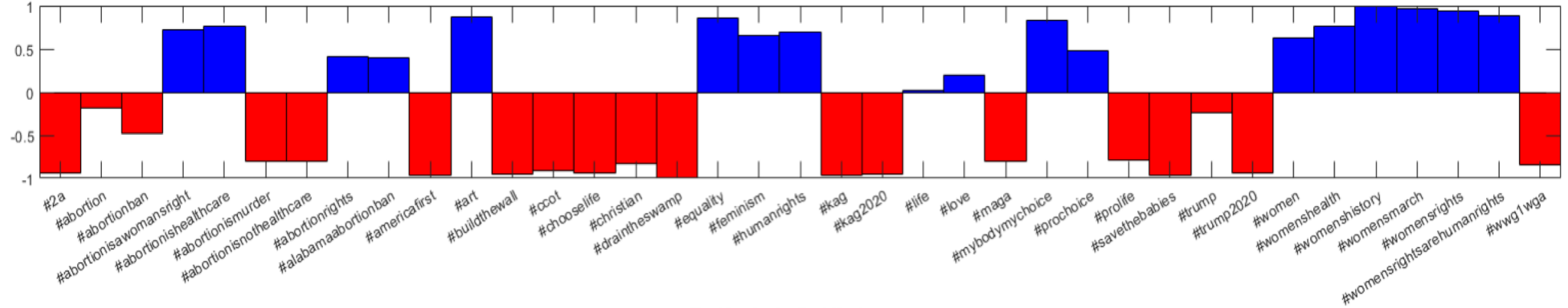
$$P_i = \frac{W_{pc_i} - W_{pl_i}}{W_{pc_i} + W_{pl_i}}$$

Hashtag polarization

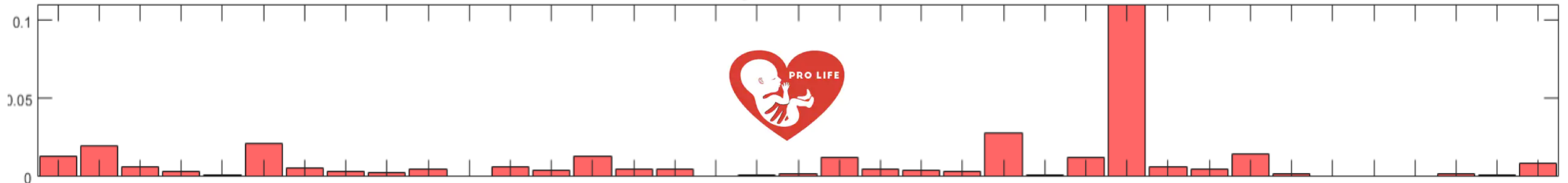
Ranking in the ProChoice dataset



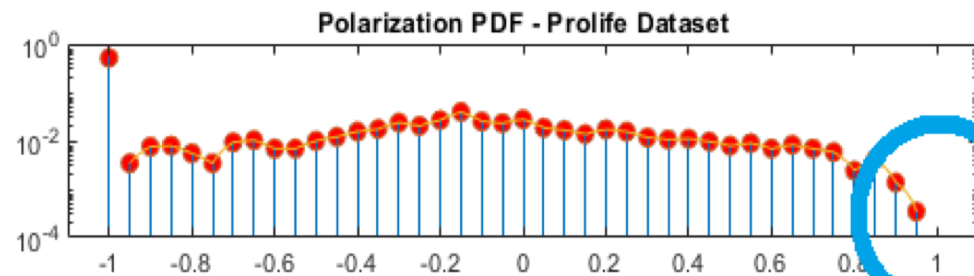
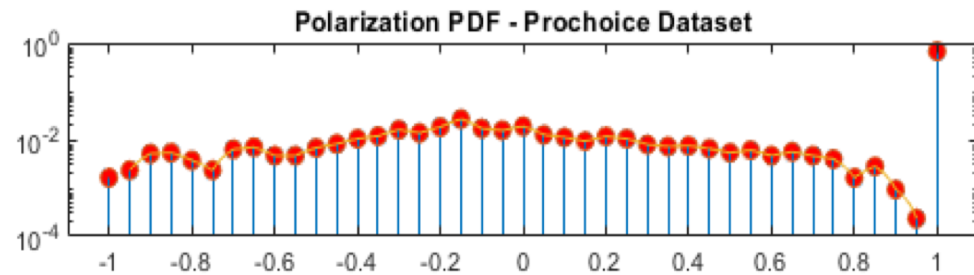
Polarization level



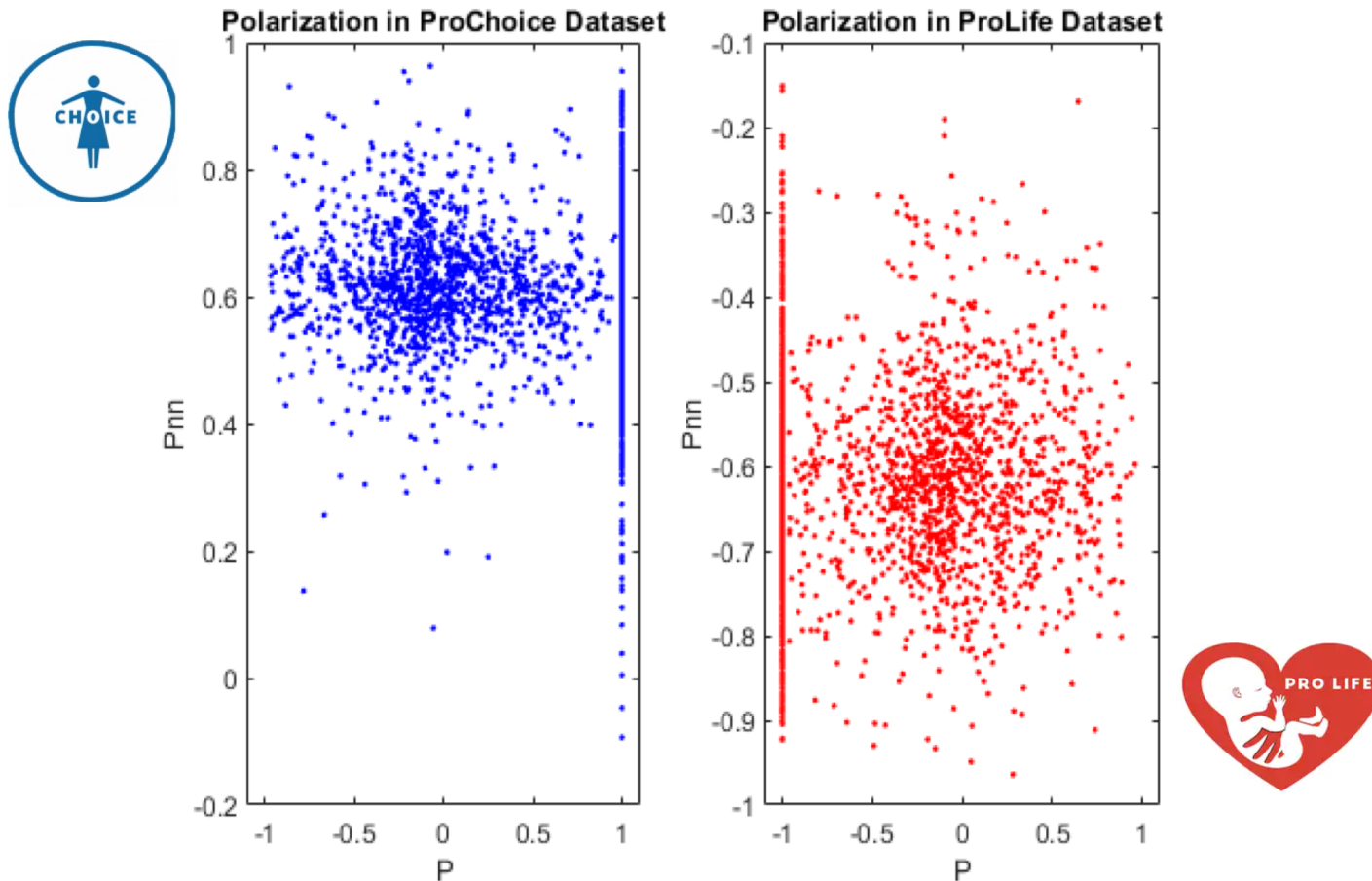
Ranking in the ProLife dataset



Polarization effects



Polarization effects



Absence of a debate?